

T10 SOLUTIONS (WAITZ)

$$a) \frac{T_T}{T} = 1 + \frac{\gamma-1}{2} M^2 = 1 + 0.2(4) = 1.8$$

$$\therefore \boxed{T_T = 390.6 \text{ K}, T = T_{atm} = 217 \text{ K}}$$

$$\frac{P_T}{P} = \left[\frac{T_T}{T} \right]^{\gamma/(\gamma-1)} = [1.8]^{1.4/0.4} = 7.82$$

$$\therefore \boxed{P_T = 176.8 \text{ kPa}, P = P_{atm} = 22.6 \text{ kPa}}$$

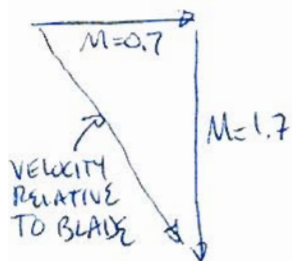
b) T_T & P_T ARE THE SAME AS ABOVE INLET IS

ADIABATIC AND Q-S SO STAG. QUANTITIES ARE CONSTANT AND WE HAVEN'T CHANGED REFERENCE FRAMES)

$$T = \frac{T_T}{1 + \frac{\gamma-1}{2} M^2}, M = 0.7 \Rightarrow \boxed{T = 355.7 \text{ K}}$$

$$P = \frac{P_T}{\left[1 + \frac{\gamma-1}{2} M^2 \right]^{\gamma/(\gamma-1)}}, M = 0.7 \Rightarrow \boxed{P = 127.5 \text{ kPa}}$$

c) FLOW IN INLET IS $M = 0.7$ (AXIAL) WITH $T = 355.7 \text{ K}$.
BLADE MOVING AT $M = 0.7$ (TANGENTIALLY)



VELOCITY RELATIVE TO BLADE = 1.84 Mach

$$T_T = T \left(1 + \frac{\gamma-1}{2} M^2 \right)$$

$$T_T = 355.7 \left(1 + \frac{\gamma}{2} (1.84)^2 \right) = \boxed{596 \text{ K}}$$

$$P_T = \frac{127.5 \text{ kPa}}{p = \beta} \left(1 + \frac{\gamma-1}{2} (1.84)^2 \right)^{\gamma/(\gamma-1)} = \boxed{779 \text{ kPa}}$$

$$P_T = \beta$$

d) $T_{\text{vessel}} = 300\text{K}$ ACCELERATE TO $M=2$

$$T_{\text{test section}} = \frac{T_T}{1 + \frac{\gamma-1}{2} M^2} = \frac{300}{1.8} = \boxed{166.7\text{K} = T_{\text{test section}}}$$

FOR $T_{\text{test section}} = 217\text{K}$ (flight temp)

AND $MACH = 2$, THEN MUST HEAT

$$\text{VESSEL TO } 1.8 \cdot 217\text{K} = \boxed{390.6\text{K}}$$