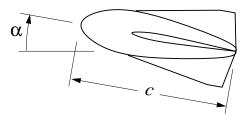
1. (30 %) A proposed winged blimp design flies at some angle of attack α , and uses both aerodynamic lift and aerostatic lift (buoyancy) to generate its total lift force L. The blimp has a given shape, but its length c is as yet undecided.



a) In addition to the given α and c, list all the remaining physical parameters which significantly influence L.

$$g(L, \alpha, c, \ldots) = 0$$

- b) Determine a set of nondimensional parameters (or Pi products) which describe this situation.
- c) Identify the nondimensional parameter which determines whether or not the aerodynamic force is significant compared to the buoyancy force.

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MINIMUM set

Parameter

not likely to be important for slow blimp)

CL = C(X, Re, Fr, Mos)

, Mo not likely to be important

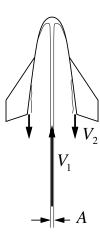
Froude number)

aerodynamic lift p V o c 2

Gerostatic lift p g c 3

The (Fronde number) indicates the relative magnitude of acrodynamic lift & buoyancy lift

2. (40 %) A toy rocket traveling at steady speed is propelled by a thin water jet with velocity V_1 and cross-sectional area A directed into the rocket's open bottom end. The water then pours out of the bottom at speed V_2 . These velocities are as seen by an observer moving alongside the rocket.

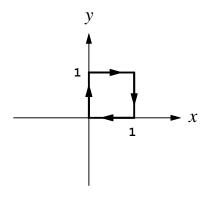


- a) Draw a suitable control volume for analyzing this flow situation. Determine the mass and momentum flows for your chosen control volume.
- b) What is the vertical thrust force imparted by the water? You may neglect the effect of gravity on the water velocities.

3. (30 %) A 2-D velocity field is given by

$$u(x,y) = x \qquad , \qquad v(x,y) = -y$$

- a) Determine and sketch the streamline pattern.
- b) Determine the circulation around the unit-square curve shown (Note: This is curve is $\underline{\text{not}}$ a streamline of this flow)



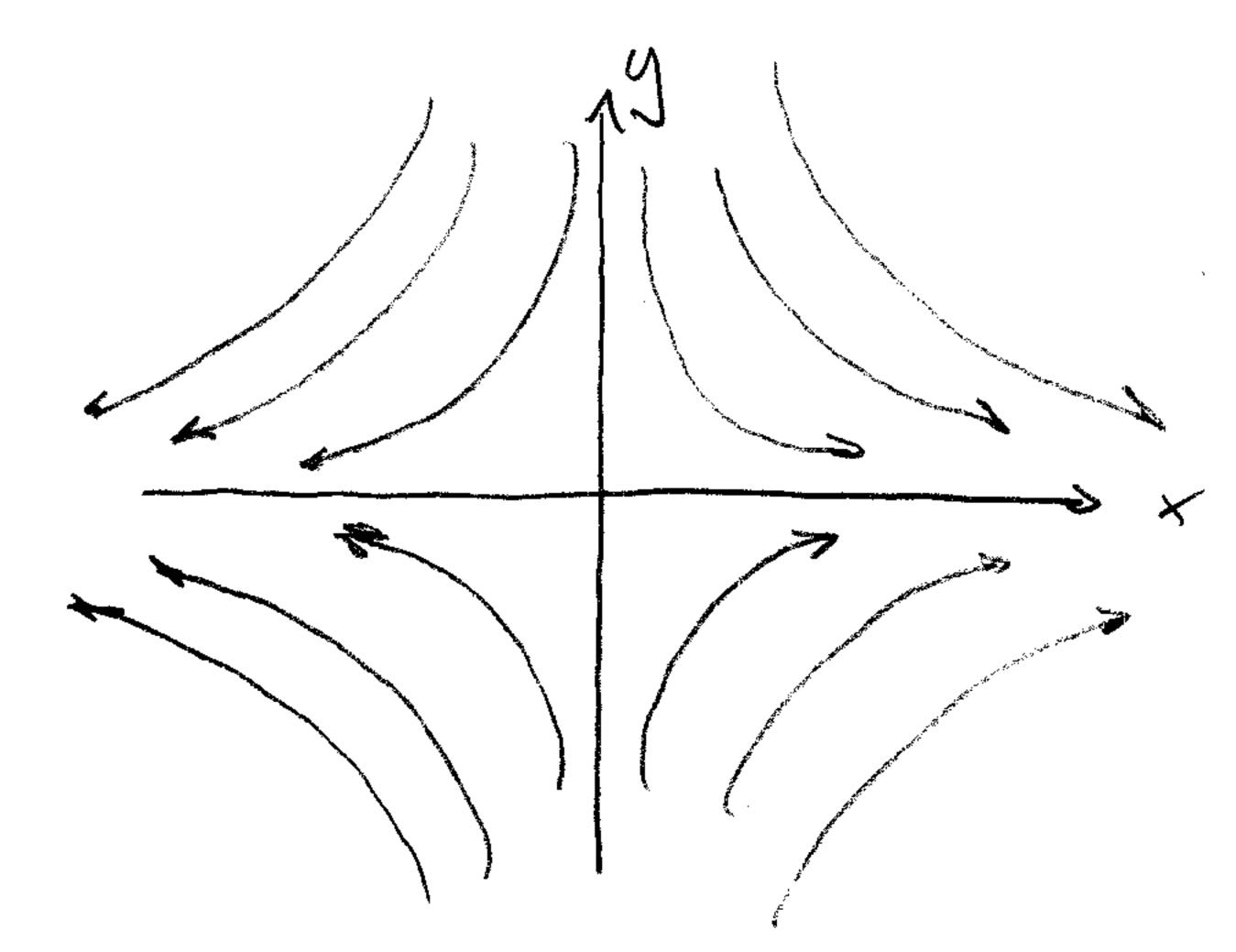
Question 3 Solution

a)
$$\frac{dy}{dx} = \frac{-y}{x}$$

$$\frac{dy}{dx} = -\frac{dx}{x}$$

$$\frac{dy}{dy} = -\frac{dx}{x} + C$$

$$y = C$$



11 corner flow

$$b) \Gamma = - \oint \vec{V} \cdot d\vec{s} = - \iint \vec{s} dA$$

A A

Easiest to note that $3 = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = 0 - 0 = 0$

$$- = \iint 3 dA = 0$$

For example, for side 1: $d\vec{s} = 1 dx$, $\vec{V} = u\hat{1} = x\hat{1}$ $\vec{V} \cdot d\vec{s} = x dx$ $\vec{V} \cdot d\vec{s} = x dx$ $\vec{V} \cdot d\vec{s} = -\frac{1}{2}x^2 / \vec{v} = -\frac{1}{2}$ Similarly for sides 2, 3, 4