

↪ from C.D.L.

$$a) 0.4 \text{ hp} \cdot 745.7 \text{ W/hp} = \boxed{298.3 \text{ W}}$$

$$298.3 \text{ W} / (1.356 \text{ W/ft-lb/s}) = \boxed{220.0 \text{ ft-lb/s}}$$

$$b) \text{ heat flow } \dot{H} = 3 \cdot \text{Power} = \boxed{894.9 \text{ W}}$$

$$\text{heat capacity of water } c = 4.2 \text{ J/g} \cdot ^\circ\text{K} = \underline{4200 \text{ J/kg} \cdot ^\circ\text{K}}$$

$$\text{typical body mass } m = \underline{70 \text{ kg}} \quad (155 \text{ lb})$$

$$\text{rate of temperature increase } \dot{T} = \frac{\dot{H}}{m c} = \frac{894.9 \text{ W}}{70 \text{ kg} \cdot 4200 \text{ J/kg} \cdot ^\circ\text{K}} = \underline{0.003^\circ\text{K/s}}$$

Human body can't tolerate more than a few degrees of temperature rise.

$$\text{Say } \Delta T_{\text{max}} = 3^\circ\text{K} = \dot{T} \Delta t_{\text{max}}$$

$$\Rightarrow \Delta t_{\text{max}} = \frac{\Delta T_{\text{max}}}{\dot{T}} = \frac{3^\circ\text{K}}{0.003^\circ\text{K/s}} = \boxed{1000 \text{ s}} = \boxed{16.7 \text{ minutes}}$$

c) dimensions, using SI units for example:

$$\rho \sim \text{kg/m}^3, \quad V \sim \text{m/s}, \quad S \sim \text{m}^2, \quad c \sim \text{m}$$

$$L \sim N = \text{kg} \cdot \text{m/s}^2 \quad (\text{force}), \quad M \sim N \cdot \text{m} = \text{kg} \cdot \text{m}^2/\text{s}^2 \quad (\text{moment})$$

$$\text{equation: } L = \frac{1}{2} \rho V^2 S c_L$$

$$\text{units} \rightarrow \underline{\text{kg} \cdot \text{m/s}^2} \sim (\text{kg/m}^3) (\text{m/s})^2 \text{m}^2 c_L \sim \underline{\text{kg} \cdot \text{m/s}^2} c_L$$

so c_L is dimensionless

$$\text{equation: } M = \frac{1}{2} \rho V^2 S c_M$$

$$\text{units} \rightarrow \underline{\text{kg} \cdot \text{m}^2/\text{s}^2} \sim (\text{kg/m}^3) (\text{m/s})^2 \text{m}^2 c_M \sim \underline{\text{kg} \cdot \text{m}^2/\text{s}^2} c_M$$

so c_M is dimensionless

d) geometric dimensions scaled by $1/2$, with same airflow

$$\rho \rightarrow \rho \text{ same}, \quad V \rightarrow V \text{ same}, \quad S \rightarrow \frac{1}{4} S, \quad c \rightarrow \frac{1}{2} c, \quad c_L, c_M \text{ same}$$

$$\text{so } \boxed{L \rightarrow \frac{1}{4} L}, \quad \boxed{M \rightarrow \frac{1}{8} M}$$