20.453J / 2.771J / HST.958J Biomedical Information Technology Fall 2008

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# Molecular Network Comparison

Image: Dewey Lab, MIT.

### Nothing in Biology Makes Sense Except in the Light of Evolution

Theodosius Dobzhansky (1900-1975)



# **Evolution in Biology**

### Mutations and rearrangement in genomic DNA

Changes in protein structures, abundances, and modification states

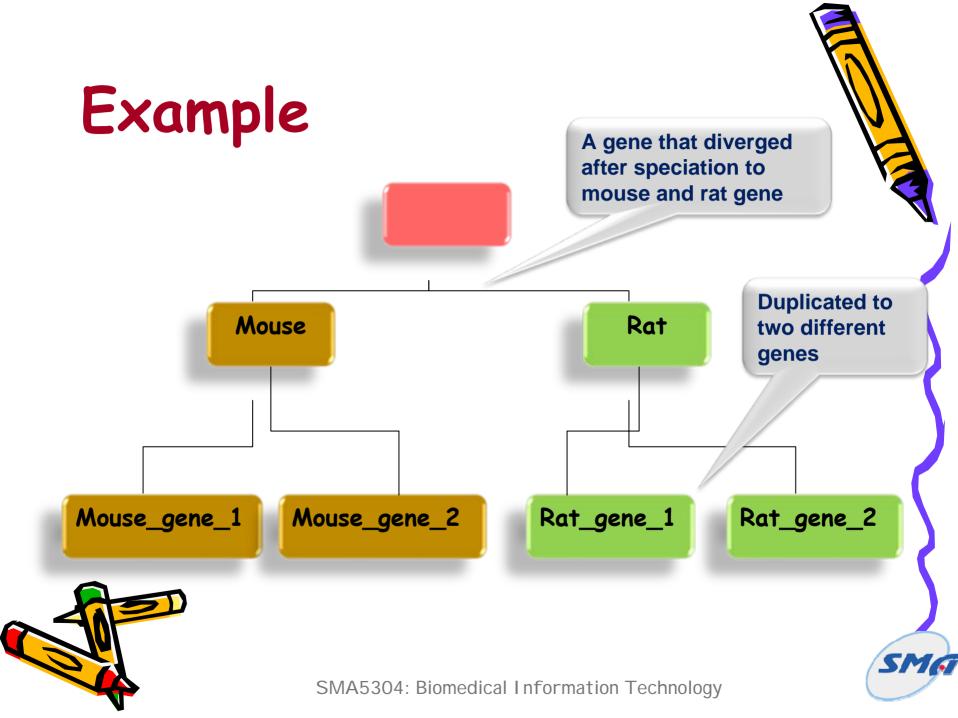
### Variation at the protein level

- Impact proteins interaction with one another, with DNA, and with small molecules
- Affects signaling, regulatory, and metabolic networks

### Changes in network organization

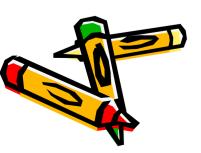
Affects cellular function, tissue-level responses,
 behavior and morphology of whole organisms





# Metrics for Evolutionary Change

- Gene and protein sequences
- Why?
  - Fundamental level of biological variation
  - Readily available through automated sequence technology
- Network of protein interactions as metric?

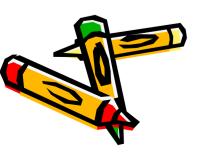




### Protein-Protein Interaction

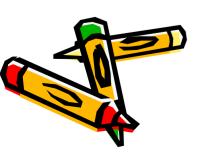
- Often, proteins interact with other proteins to perform their functions
- Backbone of molecular activity within the cell
  Cell can be understood as a complex network of interacting proteins

Image removed due to copyright restrictions. See: "MAPK/ERK in Growth and Differentiation." http://focosi.altervista.org/mapkmap2.html.



# Why?

- Increased complexity (function) is not explained simply by variations in gene (or protein) count
- Exponential growth in data
  - Mass spectrometry
  - Genome-wide-chromatin immunoprecipation
  - Yeast two-hybrid assays
  - Combinatorial reverse genetic screens
  - Literature mining





# Questions in evolutionary and comparative biology

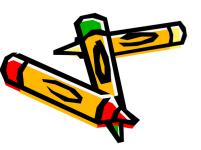
Given that protein sequences and structures are conserved in and among species, are networks of protein interactions conserved as well?

Is there some minimal set of interaction pathways required for all species?

Can we measure evolutionary distance at the level of network connectivity rather than at the level of DNA or protein sequence?

# Molecular Network Comparison

Process of contrasting two or more interaction networks, representing different species, conditions, interaction types or time points.





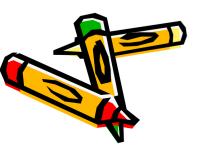
Why proteins, protein interactions and groups of interactions are likely to have equivalent functions across species?

Based on these similarities, can we predict new functional information about proteins and interactions that are poorly characterized?

What do these relationships tell us about the evolution of proteins, networks and whole species?

### Answer To

Given that systematic screens for protein interactions may report large numbers of falsepositive measurements, which interactions represent true binding events?



# Types of Network Comparison

### Network alignment

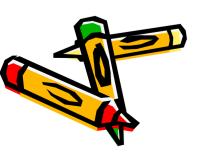
process of globally comparing two networks, identifying regions of similarity and dissimilarity

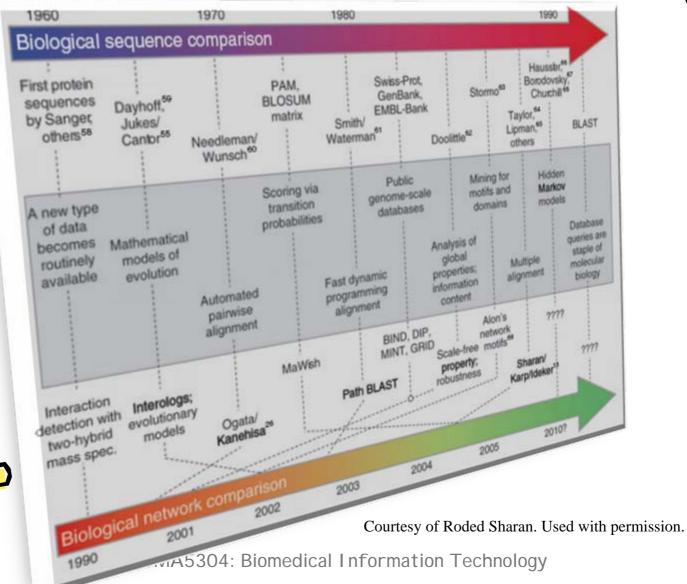
### Network integration

process of combining several networks, encompassing interactions of different types over the same set of elements, to study their interrelations.

#### Network querying

a given network is searched for subnetworks that are similar to a subnetwork query of interest





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#### **Sequence Comparison**

 Sequence alignment methods were proposed long before large sequence databases were widely available.

#### **Network Comparison**

 Large network and interaction databases have been available from the late 1990s onwards, three to four years before the first network comparisons were performed.



#### **Sequence Comparison**

- Computational searches for Occurred early in the field motifs and systematic characterization of global properties arose relatively late in the history of sequence analysis.
- Local sequence alignment can be solved efficiently

#### **Network Comparison**

of network comparison.

Analogous problem of identifying conserved protein modules is computationally hard



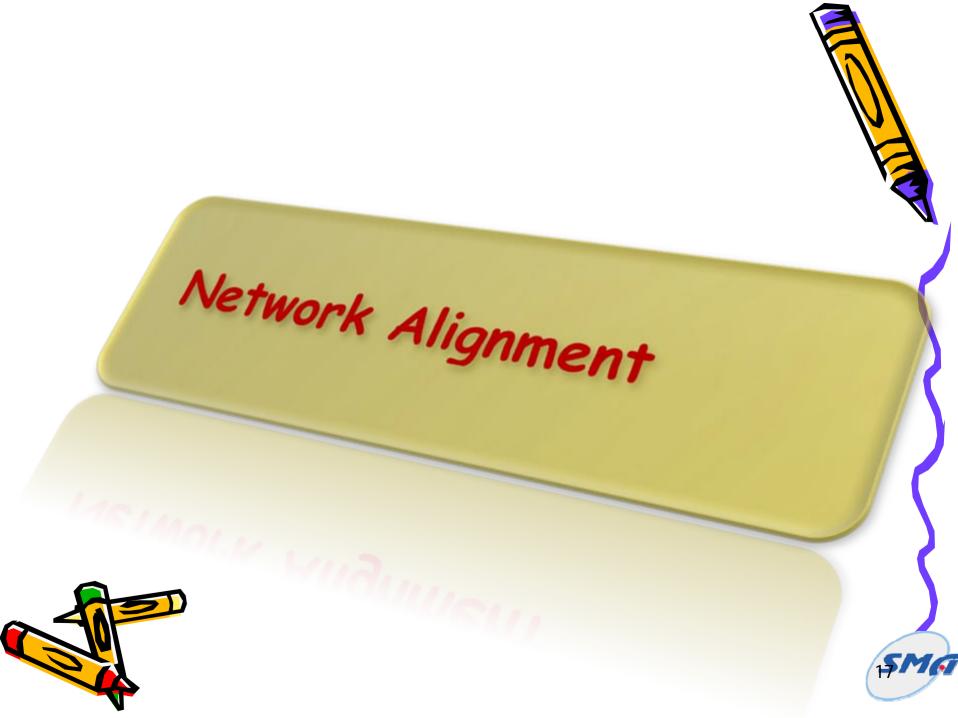
#### **Sequence Comparison**

 Integrating biological sequences data types (nucleotides or amino acids) has not posed a major problem.

#### **Network Comparison**

 Integrating different data types of molecular networks is a challenging problem

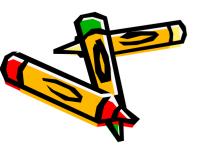




### Protein-Protein Interaction Network (PPI)

An undirected graph G(V, E) where V denotes the set of proteins and  $(u, v) \in E$  denotes the interaction between proteins u and v

interaction between proteins u and v



### **Network Alignment** Problem

•The problem of finding conserved subnetworks in a

•We can reduce it to subgraph-isomorphism

Given k different PPI networks belonging to different species, we wish to find conserved subnetworks within these networks

Solution

these networks

We can reduce it to

group of networks is NP-Hard

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·A heuristic approach is required

### Usefulness

### Functional Annotation

Assign roles to unknown proteins

### Annotation transfer

Assigns to a protein of unknown function the annotation of a protein to which it is aligned

### Landmark extension

If a protein of unknown function appears as part of an alignment together with a "landmark" protein of known function, we can label the protein with a similar annotation

### Usefulness

### Compute functional orthologs

- Proteins which perform the same function across species
- Separating true protein-protein interactions from false positives
- Organizing large-scale interaction data into models of cellular signaling and regulatory machinery
- Identify novel modules by detecting unusual conserved subnetworks

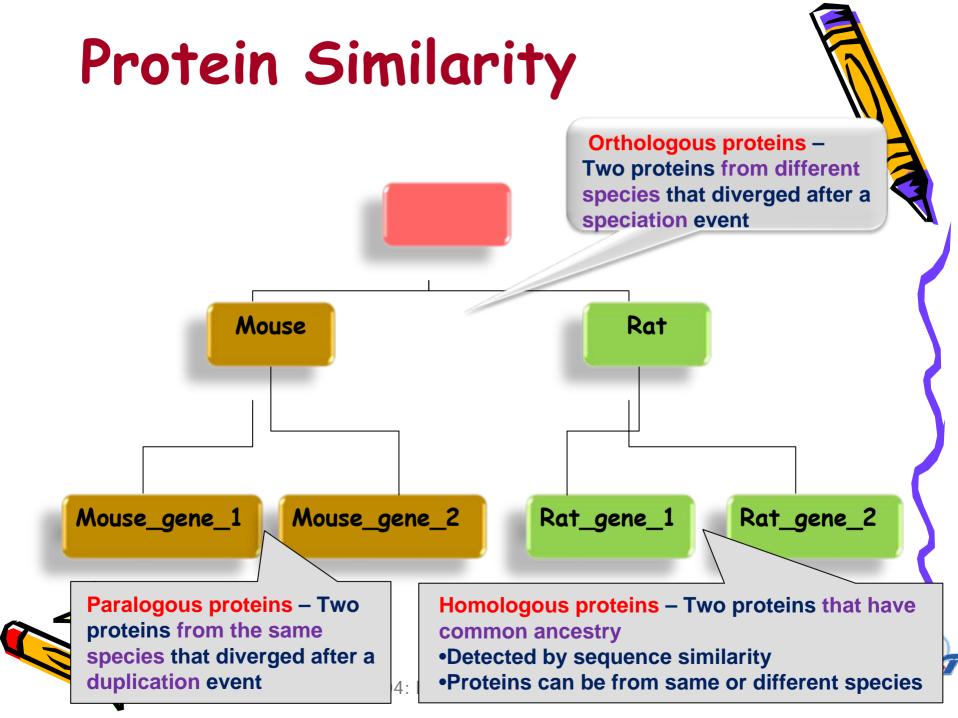


### **Core Problems**

A scoring framework that captures the knowledge about module evolution

Identify high scoring alignments (conserved functional modules) from among exponentially large set of possible alignments



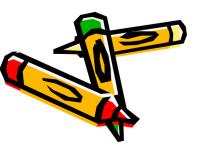


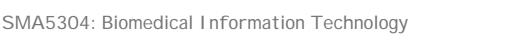
### Overview

- B. P. Kelley et al. Pathblast: a tool for alignment of protein interaction network PNAS., 2003.
- M. Chen, R. Hofestaedt. PathAligner: Metabolic Pathway Retrieval and Alignment Applied Bioinformatics, 3(4), 241–252, 2004.
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- M. Kalaev, V. Bafna, R. Sharan. Fast and Accurate Alignment of Multiple Protein
  Networks. In Proc. of ACM RECOMB, 2008.

### PathBlast

 Implements a scoring function and search algorithm to find high probability pathway alignments between two protein interaction networks





# Pathway Alignment

- Consists of two paths one from each network (N1 and N2)
- Proteins in the first path pair with putative homologs occurring in the same order in the second path
  - A homologous protein pair may not occur more than once per pathway alignment
- May include nonhomologous proteins
  - Using gaps and mismatches

# Gaps and Mismatches

### • Why?

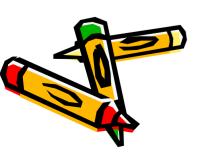
Overcome noisy PPI data as well as evolutionary variations

### Gap

Occurs when a protein interaction in one path skips over a protein in the other

### Mismatch

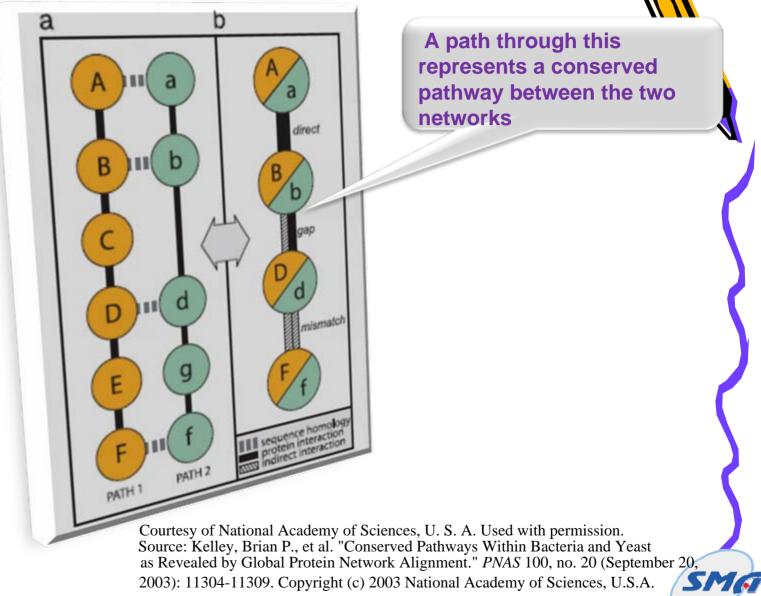
- Occurs when two proteins at the same position in the alignment do not share sequence homology
- Neither gaps nor mismatches may occur consecutively





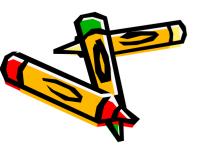
# Global Alignment Graph





### Similarity Between Proteins

- In order to build the global alignment graph, similarity between proteins need to be measured
  - Using BLAST
- Quantifies the similarity
- Assigns it a p-value
  - probability of observing such similarity at random
- E-value or Expectation value
  - Inumber of different sequence pairs with score equivalent or better than this hit's score that are expected to result by a random search
  - Unalignable proteins are assigned max E-value of 5



# Log Probability Score

Probability of true homology within the protein pair represented by v in P Probability that the proteinprotein interaction represented by e is real (not false positive error)

Expected values of p(v) over all vertices and edges in G

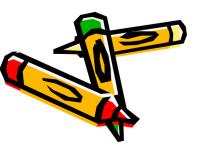
 $S(P) = \sum_{v \in P} \log_{10} \frac{p(v)}{p_{\text{random}}} + \sum_{e \in P} \log_{10} \frac{\overline{q(e)}}{q_{\text{random}}}$ 

Expected values of q(e) over all vertices and edges in G



# Alignment Algorithm

- Identify the highest-scoring pathway alignment
  P\* of fixed length L (L vertices and L -1 edges).
- If G is directed and acyclic,
  - Linear time (in the number of edges)
  - using dynamic programming





# Alignment Algorithm

The highest-scoring path of length I = 2...L ending in vertex v will have score

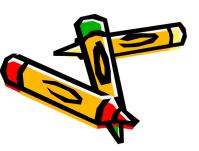
$$S(v,l) = \underset{u \in parents(v)}{\operatorname{arg\,max}} \left[ S(u,l-1) + \log \frac{p(v)}{p_{random}} + \log \frac{q(e_{u \to v})}{q_{random}} \right]$$

$$S(v,1) = \log \frac{p(v)}{p_{random}}$$
 Base Case

# Alignment Algorithm

### • G is generally not acyclic

- First construct a sufficient number (5L!) of directed acyclic subgraphs
- Use the dynamic programming method to compute the highest-scoring paths for each.
- Lan be done in linear time





### Experiments

• Yeast (S. cerevisiae) vs. Bacteria (H. pylori)

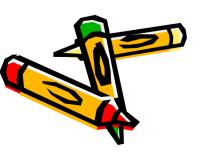
**4** Orthologous pathways between the networks of two species.

#### Yeast vs. Yeast

Paralogous pathways within the network of a single species, by aligning the yeast PPI network versus itself.

#### Yeast vs. Yeast

Interrogating the protein network with pathway queries, by aligning the yeast PPI network versus simple pathways.



### Comparison between Yeast and Bacteria GAGs to the corresponding randomized networks

Edas

Gap

260

68.8 ± 23.8

NIA

NIA

Direct

2.5 ± 1.9

1,380 62.3 ± 29.4

Graph size and best pathwayalignment scores were significantly larger for the real aligned networks

Mismatch

1,769 437.7 ± 110.3

N/A

NIA

CPU, min

0.38

0.4 ± 0.02

7.08

 $6.9 \pm 0.2$ 

Both species indeed share conserved interaction pathways

Vertices

Total

2,036 509.0 ± 128.0

1,380

62.3 ± 29.4

(homologs)

820

5,500

11.0  $-15.3 \pm 6.5$ 

7.5

 $4.8 \pm 0.7$ 

Best 501

Score

Best\*

8.1

 $6.1 \pm 0.8$ 

11.9

-4.1 ± 9.5



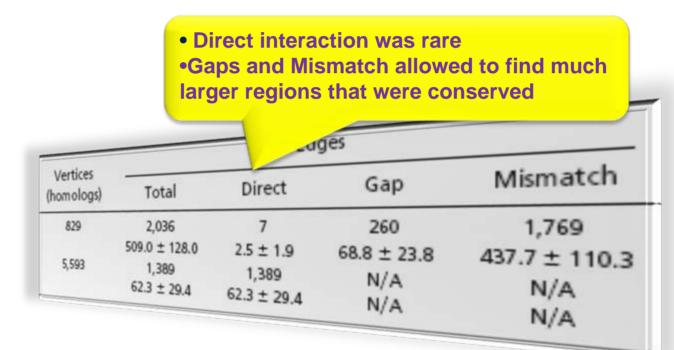
east vs. H. Pylon (Econt = 10-3)

Random: mean ± 50 east vz. jeast (Execut = 10-10)

Random: mean ± 50

Courtesy of National Academy of Sciences, U.S. A. Used with permission. Source: Kelley, Brian P., et al. "Conserved Pathways Within Bacteria and Yeast as Revealed by Global Protein Network Alignment." PNAS 100, no. 20 (September 20, 2003): 11304-11309. Copyright (c) 2003 National Academy of Sciences, U.S.A.

#### Comparison between Yeast and Bacteria GAGs to the corresponding randomized networks



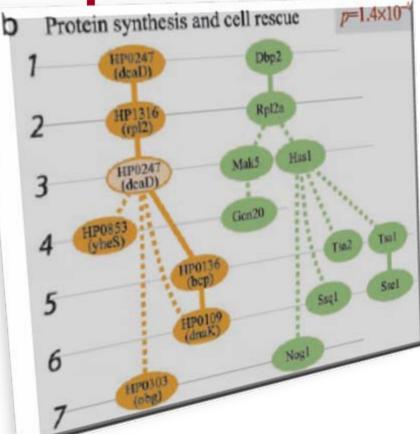


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# Relation between seemingly unrelated processes



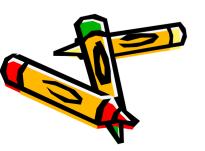


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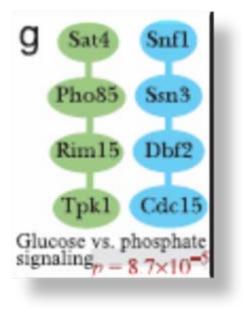
#### Yeast vs Yeast

- Search for paralogous pathways
- Constructing a GAG merging the yeast protein interaction network with an identical copy of itself
  - Only direct edge permitted
  - Proteins were not allowed to pair with themselves or their network neighbors
  - Obtain 300 highest scoring pathway alignments of length 4 (level of significance p <= 0.0001)</p>





# Paralogous Pathways



- Both have DNA binding activity, they act in two distinct processes
- Msh2/3/6 is involved in mismatch repair during meiosis and vegetative growth
- Msh4/5 facilitates crossing over during homologous recombination and is specific to meiosis

Msh2

Msh6

Mismatch repair vs. crossing-over machinery

Msh5

Msh4

Msh4

Msh5

SMA

Msh2

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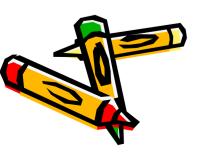
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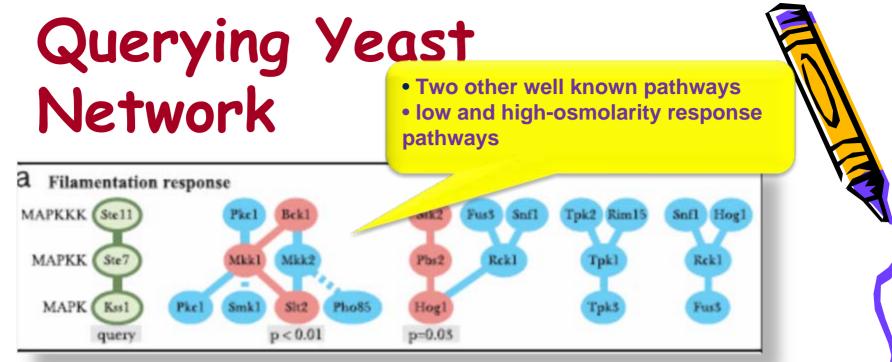
 $1 \times 10$ 



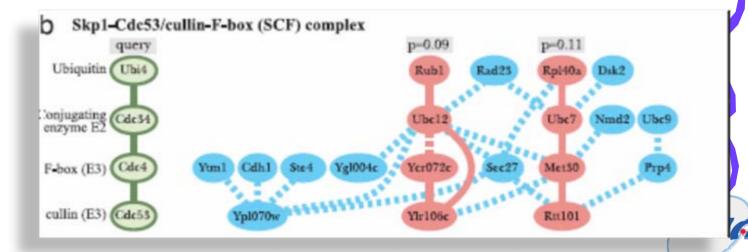
# Pathway Queries

- Query a single protein network with specific pathways of interest
  - Similar to using BLAST to query a sequence database with a short nucleotide or amino acid sequence query
- Query Yeast network with a MAPK pathway associated with filamentation response





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C+- 20 4-+1

. . . . . . .

#### Alignment 1 6.835

Query YHR023W (MY01)	Hatch YKI.129C	Punction Query: STe2U-ACTI-MyOI myosin I	
YFL039C (ACT1)	YJR065C	actin-related gene	
YHL.007C (STE20	) YDR523C	dispensable for mitosis, involved in middle/late stage of meiosis, required for spore wall formation	

#### Alignment 2 6.835

Query YHL007c (STE20)	Hatch YDR523C	Function dispensable for mitosis, involved in middle/late stage of meiosis, required for spore wall formation
YFL039C (ACT1)	ZJR065C	actin-related gene
YHR023W (MY01)	2KL1290	myosin I

#### Alignment 3 6.768

	ery R023¥	(MZ01)	Hatch YKL129C	Function myosin I													
YP	L <b>0</b> 39C	(ACT1)	YJR065C	actin-rel	Lated	genc											
¥Ю	L <b>007</b> C	(STE20)	YPL140C	Member of	е мар	kinase	pathway	involving	PKC1,	BCK1,	and S	SLT2.	Shows	functional	redundancy	with MARI	





#### **Graphical Display**

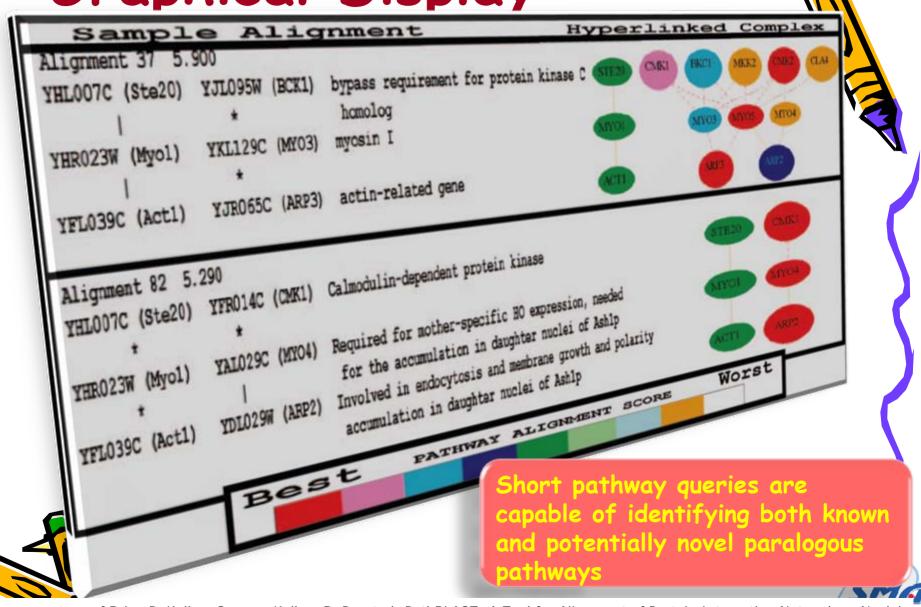
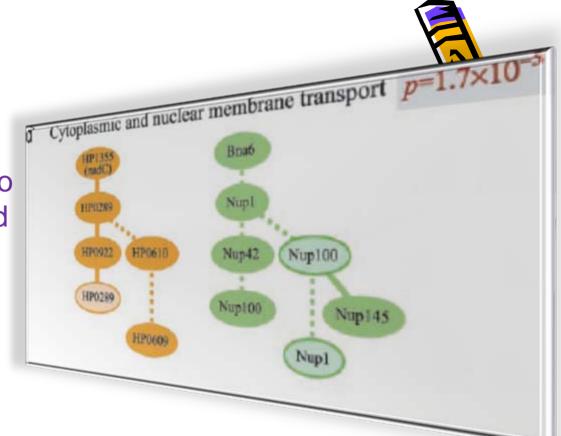


Image courtesy of Brian P. Kelley. Source: Kelley, B. P., et al "PathBLAST: A Tool for Alignment of Protein Interaction Networks." *Nucleic Acids Res* 32, web server issue, (July 1, 2004): W83-W88. © the authors, published by Oxford University Press under open access.

#### Summary

- Pathways from a well studied network is used to shed light on their aligned counterparts from a less well characterized ones
- HP0609 is adjacent to HP0610 and HP0289, which localize to the bacterial outer membrane, and opposite yeast Nup1, which localizes to the nuclear



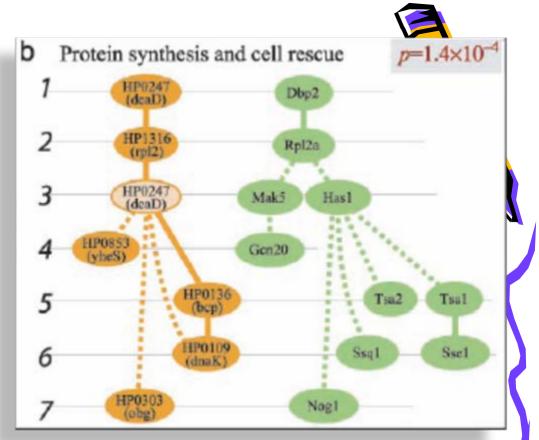


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#### HP0609 is also membrane-specific and that the bacterial pathway shares homology with the yeast nuclear pore complex

#### Summary

- Single pathways in bacteria frequently correspond to multiple pathways in yeast
- Yeast has undergone or more whole-genome duplications relative to bacteria



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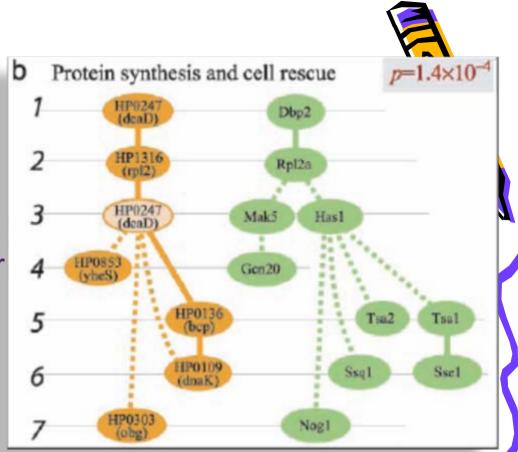


A single bacterial RNA helicase (deaD) occupies the same pathway position, and perhaps functional role, as three different helicases in yeast (Dbp2, Mak5, and Has1).

#### Summary

- Proteins within highscoring pathway alignments did not necessarily pair with their best sequence matches in other pathway
- Bcp and Tsa1 are functional orthologs despite weak sequence similarity





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Best match for bcp is Dot5 and not Tsa1 Best match for Tsa1 is TsaA

### Limitations

Proteins may occur more than once in an identified matched pathway

biologically implausible

- The algorithm provides limited support for identifying nonexact pathway matches
  - supporting no more than a single consecutive deletion of proteins from the query pathway
  - 4 no more than a single consecutive insertion of proteins to the matched pathway
- The running time of the algorithm involves a factorial function of the pathway length



#### Multiple Alignment (Sharan et al, 2005)

- Three-way alignment of the protein—protein interaction networks
  - 4 Caenorhabditis elegans
  - 4 Drosophila melanogaster
  - **4** Saccharomyces cerevisiae.
- Protein interaction data were obtained from the Database of Interacting Proteins

4 14,319 interactions among 4,389 proteins in yeast

43,926 interactions among 2,718 proteins in worm

20,720 interactions among 7,038 proteins in fly

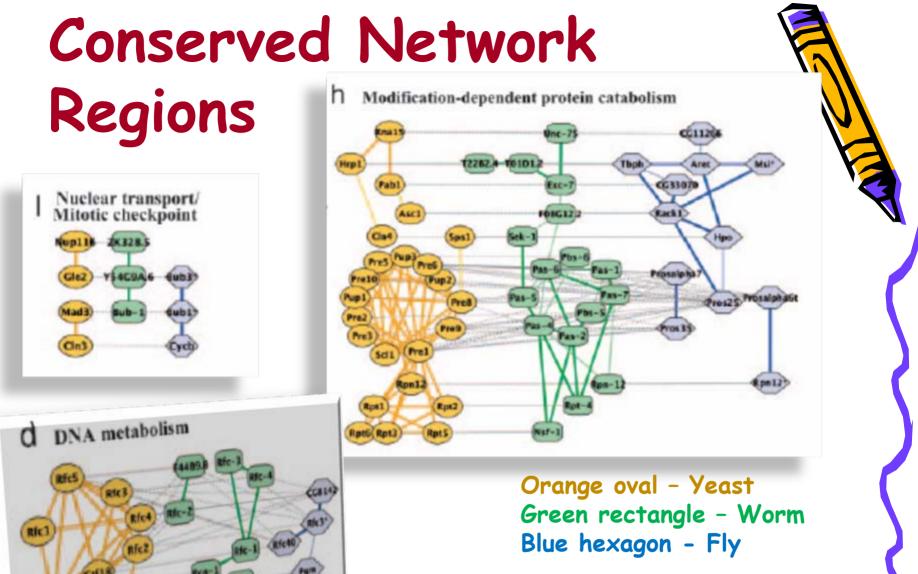
# **Experimental Results**

#### Protein sequences obtained from

- Saccharomyces Genome Database
- 4 WormBase
- \rm FlyBase
- Combined with the protein interaction data to generate a network alignment
  - 4 9,011 protein similarity groups
  - 49,688 conserved interactions for the three networks
- 183 protein clusters and 240 paths conserved at a significance level of P < 0.01</li>

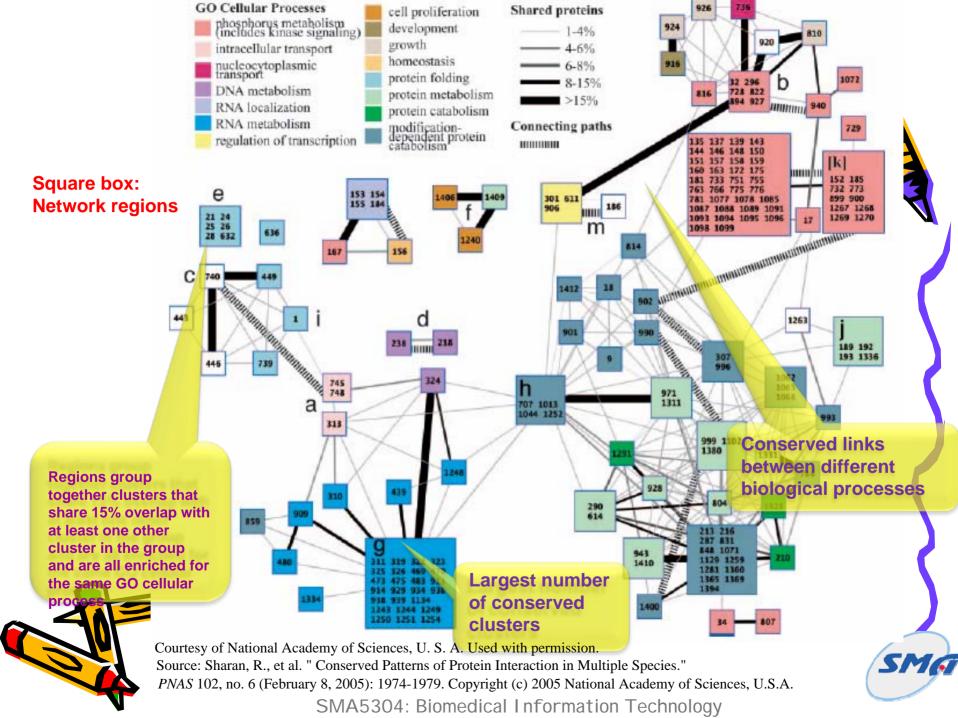


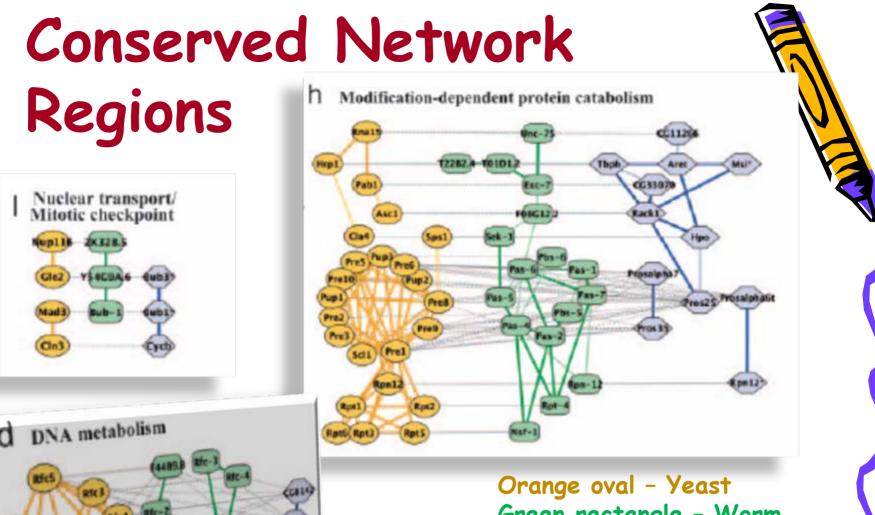




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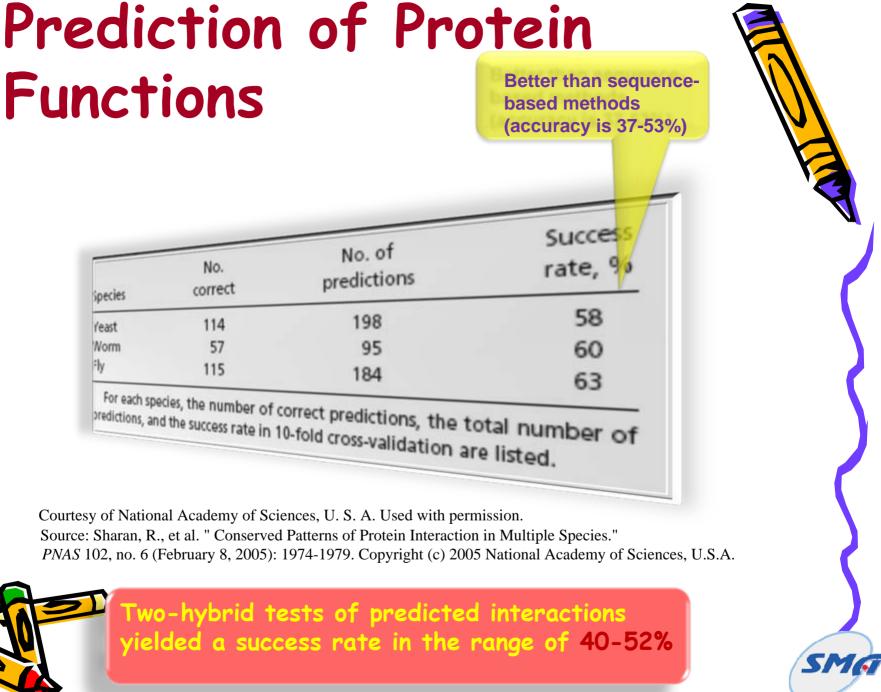




2ír

#### Green rectangle - Worm Blue hexagon - Fly

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#### Prediction of Proteins Interaction

	Sensitivity,	Specificity, %	Pvalue	Strategy
Species	%	77	1.1e-25	i I
Veat	50	82	1e-13 5.3e-5	i
Yeast	43	84	1.2e-6	i + ii
Worm	23	99	6e-4	i + ii i + ii
Fly	9	100	0.5	1+#
Yeast	10	100		
Worm	0.4			

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Prediction accuracy was highly significant

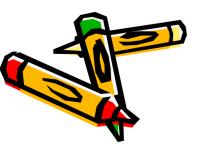
SMA CSB Program





#### Overview

- T. Shlomi, D. Segal, E. Ruppin, and R. Sharan. QPath: A Method for Querying Pathways in a Protein-Protein Interaction Network. *BMC Bioinformatics*, 7(199), 2006.
- B. Dost, T. Shlomi, N. Gupta et al. QNet: A Tool for Querying Protein Interaction Networks. In Proc. of ACM RECOMB, 2007.
- Y. Tian, R. C. McEachin, C. Santos et al. **SAGA: A subgraph** matching tool for biological graphs. *Bioinformatics*, 2006.



#### QPath

#### Goal

Querying linear pathways within a given network

#### QPath

Searches for matching pathways composed of distinct proteins that are similar to the query proteins in their sequence and interaction patterns





# Path Query Problem

#### Input

- ▲ a target network, represented as an undirected weighted graph G(V,E) with a weight function on the edges w : E×E→R
- 4 a path query  $Q = (q_1, ..., q_k)$ .
- Additionally, a scoring function H : Q×V is given.



# Path Query Problem

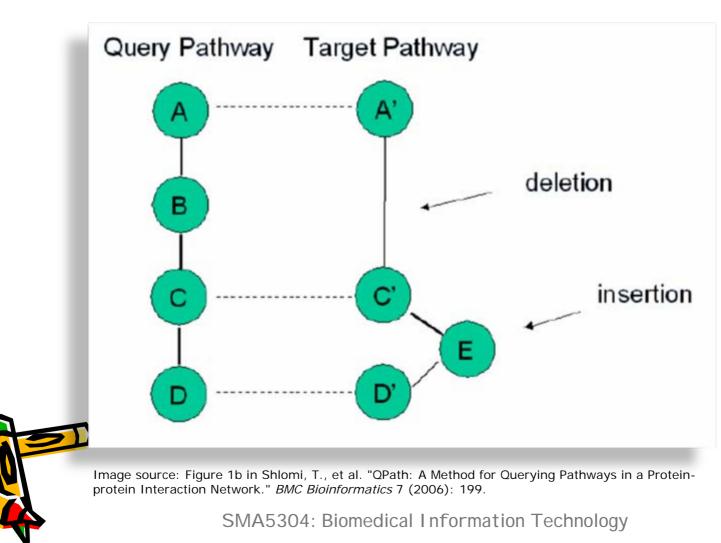
#### Output

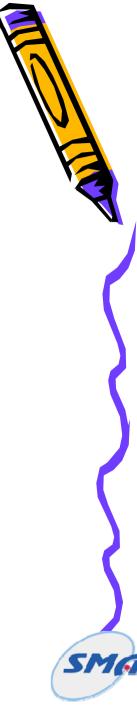
- A set of best matching pathways P = (p<sub>1</sub>,...,p<sub>k</sub>) in G, where a good match is measured in two respects
- Each node in the matched pathway and its corresponding node in the query are similar with respect to the given scoring function H.
- The reliability of edges in the matched pathway is high





# Example of Alignment





# Evaluation of Pathway Queries

• Queried the yeast network with the yeast filamentous growth MAPK cascade.





Image source: Figure 6 (supplemental material) in Shlomi, T., et al. "QPath: A Method for Querying Pathways in a Protein-protein Interaction Network." *BMC Bioinformatics* 7 (2006): 199.

# **Evaluation of QPath**

- Modified QPath algorithm is used to search the network for pathways that have high interaction scores
  - Limited to pathways consisting of 6 proteins
    Allow for (up to 3) insertions and deletions.
- Identified a set of 271 non-redundant pathways whose scores exceeded those of 99% of randomly chosen pathways



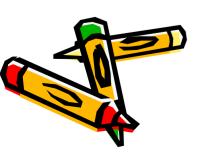
# Quality Assessment of the Pathways

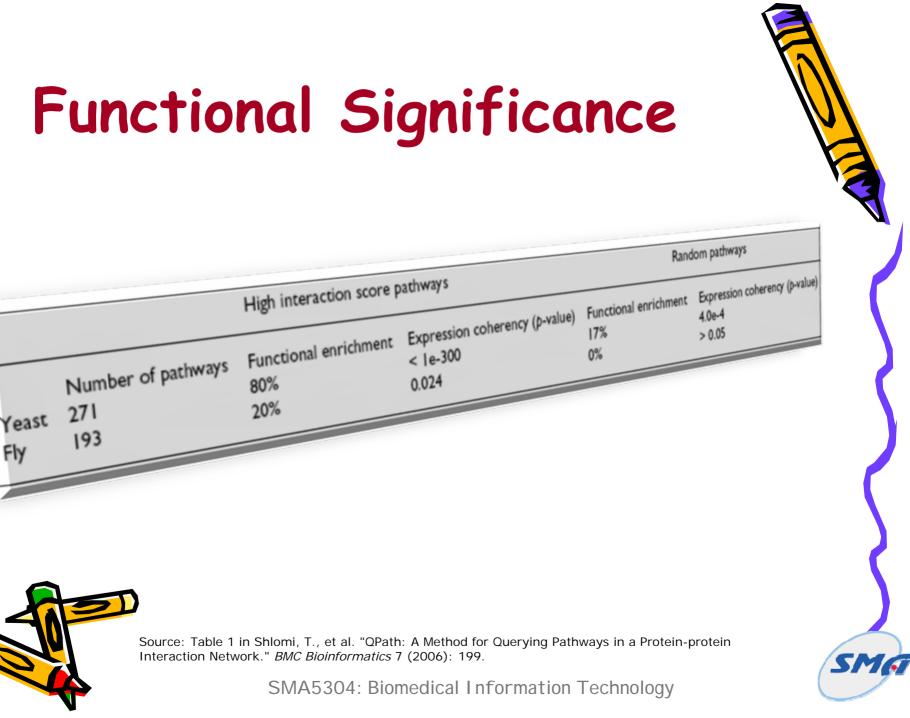
#### Functional enrichment

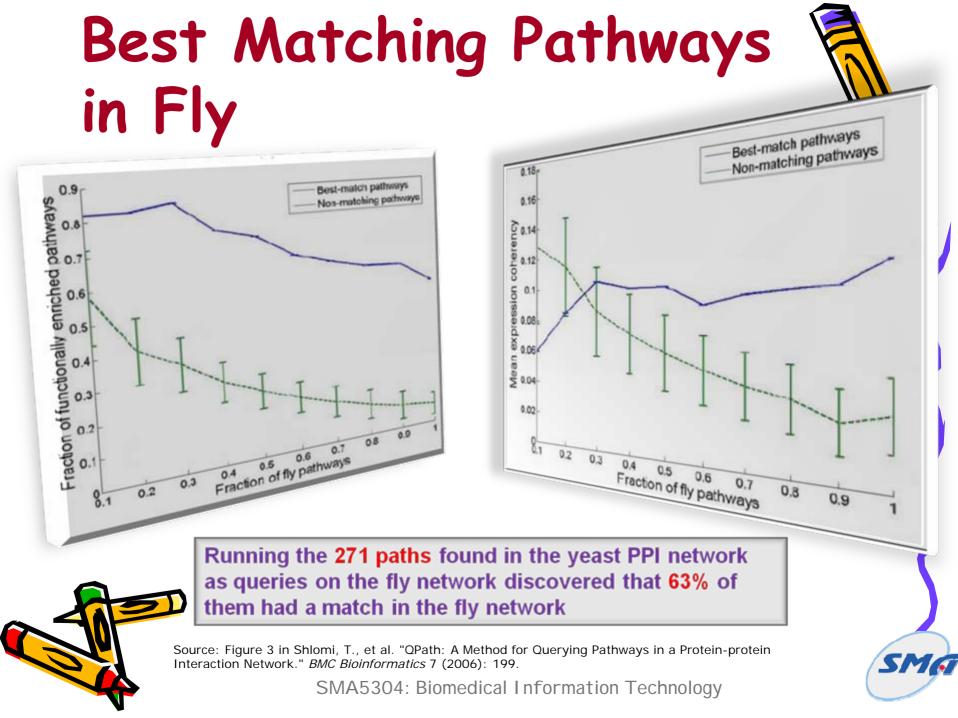
Representing the tendency of the pathway's proteins to have coherent GO functions

#### Expression coherency

measuring the similarity in expression profiles of the pathway's coding genes across different experimental conditions







#### Is the Insertion and Deletion Flexibility Really Required?

Most conserved paths between the yeast and the fly required more than one insertion and deletion

Source: Figure 2 in Shlomi, T., et al. "QPath: A Method for Querying Pathways in a Protein-protein Interaction Network." *BMC Bioinformatics* 7 (2006): 199.

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Insertions

# Is the Insertion and Deletion Flexibility Really Required?

Functionally enriched paths are strongly depended on Ins/Del



Source: Figure 2 in Shlomi, T., et al. "QPath: A Method for Querying Pathways in a Protein-protein Interaction Network." *BMC Bioinformatics* 7 (2006): 199. SMA5304: Biomedical Information Technology

Insertions

### Functional Conservation

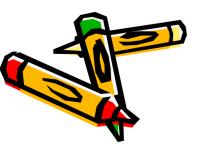
For 64% of the conserved paths, the matched paths in the fly network conserved one or more functions of the yeast query pathways

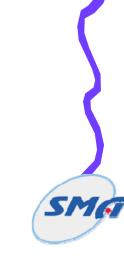




#### Conclusions

- Very young field!
- Advanced computational methodology
  - Scaling multiple network alignment
- Association of network features with diseases





#### **References Used**

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