# 9.913 Pattern Recognition for Vision 

Class XIII, Motion and Gesture Yuri Ivanov

- Movement - Activity - Action
- View-based representation
- Sequence comparison
- Hidden Markov Models
- Hierarchical representations

From Tracking to Classification


How do we describe that?
How do we classify that?
Figure by MIT OCW.

From Tracking to Classification


Figure by MIT OCW.
How do we describe that?
How do we classify that?

- We might want to ask:
- Is <it> doing something meaningful?
- What exactly?
- How does it do it?
- How fast - e.g. conducting
- How accurately - e.g. dance instruction
- What style?
- That leads us to a sequence analysis


## Motion Taxonomy

- Movement
- Primitive motion
- Self-evidential, is "what it looks like"
- Activity
- Requires explicit sequence model

Images removed due to copyright considerations. Please see: Bobick, A.
"Movement, Activity, and Action: The Role of Knowledge in Perception of Motion." Phyl Trans of Royal Statistical Society 352 (1997).

- Action
- Requires contextual information
- Requires relational information
- And many other things...

Basic Problem


## Motion Energy Image

## First idea -implicit representation of time



Sum the differences over the last $\tau$ frames:


$$
E_{\tau}(x, y, t)=\bigcup_{i=0}^{\tau-1} D(x, y, t-i)
$$

- WHERE motion happened

Photographs and figures from: Bobick, A., and J. Davis. "The Representation and Recognition of Action Using Temporal Templates." IEEE Transactions on Pattern Analysis and Machine Intelligence 23, no. 3 (2002). Courtesy of IEEE, A. Bobick, and J. Davis. Copyright 2002 IEEE. Used with Permission.

## Motion History Image

## Step two: include temporal information



$$
H_{\tau}(x, y, t)= \begin{cases}\tau & \text { if } D(x, y, t)=1 \\ \max \left(0, H_{\tau}(x, y, t-1)-1\right) & \text { otherwise }\end{cases}
$$

- HOW motion happened

Aside - you can compute a similar measure recursively:

$$
H_{\tau}(x, y, t)=H_{\tau}(x, y, t-1)+\alpha\left(D(x, y, t)-H_{\tau}(x, y, t-1)\right)
$$



Photographs and figures from: Bobick, A., and J. Davis. "The Representation and Recognition of Action Using Temporal Templates." IEEE Transactions on Pattern Analysis and Machine Intelligence 23, no. 3 (2002). Courtesy of IEEE, A. Bobick, and J. Davis. Copyright 2002 IEEE. Used with Permission.

## Illustration



OpenCV - Intel Open source Computer Vision Library

## Classification

Feature vector:
$x=[7 \mathrm{Hu}$ moments for MEI +7 Hu moments for MHI]


RTS invariant shape descriptors (see the end of notes)

With the usual Gaussian assumption on distribution of $x$ :

$$
\mu_{\omega}=E\left[x_{\omega}\right] ; \quad \Sigma_{\omega}=E\left[\left(x_{\omega}-\mu_{\omega}\right)^{2}\right]
$$

Then the class, $\omega$ :

$$
\omega=\operatorname{argmin}\left[\left(x-\mu_{\omega}\right)^{T} \Sigma_{\omega}^{-1}\left(x-\mu_{\omega}\right)\right]
$$

## Multi-View Recognition

## The model is replicated for a discrete number of views:

$$
\begin{aligned}
& \text { For } \theta=\left\{0^{\circ} \ldots 90^{\circ}\right\} \\
& V\left(\omega_{i}\right)=\min _{\theta}\left[\left(x-\mu_{\omega_{i}}^{\theta}\right)^{T} \sum_{\omega_{i}}^{-1, \theta}\left(x-\mu_{\omega_{i}}^{\theta}\right)\right] \text { Closest member of each class } \\
& \boldsymbol{\omega}=\operatorname{argmin}\left[V\left(\omega_{i}\right)\right] \quad \text { Nearest class }
\end{aligned}
$$

Photographs and figures from: Bobick, A., and J. Davis. "The Representation and Recognition of Action Using Temporal
Templates." IEEE Transactions on Pattern Analysis and Machine Intelligence 23, no. 3 (2002). Courtesy of IEEE,
A. Bobick, and J. Davis. Copyright 2002 IEEE. Used with Permission.

## Example Application

## KidsRoom

- Interactive story
- Autonomous system
- Narration is controlled
- Input from cameras and mike
- Visual events:

Image removed due to copyright considerations. See:

- position
- motion energy
- motion direction
- gross body motion


## Motion Energy



## Movement Classification

## "Flap"



Last game sequence

## Temporal Alignment

Another idea - temporal alignment


If sequences are aligned to a common time axis, then we can treat them as vectors

## Temporal Alignment

Find re-indexing sequences $i_{x}$ and $i_{y}$ that align $X$ and $Y$ to a common time axis $k$ while minimizing dissimilarity.


One solution - Dynamic Time Warp algorithm

$$
E=\frac{1}{M_{\phi}} \sum_{n=1}^{T}\left\{m(n)\left(s_{x}\left[i_{x}(n)\right]-s_{y}\left[i_{y}(n)\right]\right)^{2}\right\}
$$

Global normalization Local weighting

Example: Utterance Classification


## Example: Utterance Classification

Alternative - pair-wise alignment:

$$
\text { SVM: } f(x)=\sum_{i=1}^{N} \alpha_{i} y_{i} K\left(\mathbf{x}, \mathbf{x}_{i}\right)+b
$$

1. Compute the symmetric DTW between all pairs

$$
d_{i j}=\frac{D\left(s_{i}, s_{j}\right)+D\left(s_{j}, s_{i}\right)}{2}
$$

2. Compute an RBF Kernel

$$
K\left(s_{i}, s_{j}\right)=\exp \left(-\gamma d_{i j}\right)
$$

Danger: $K$ might not be a proper kernel matrix - need to regularize

## Example: Utterance Classification

Japanese Vowel Set (UCI Machine Learning Repository):

- Speaker identification task
- 9 speakers
- saying the same Japanese vowel
- features 12 cepstral coefficients
- each utterance - 7-30 samples
- 340 training examples
- 240 testing examples

|  | Accuracy |
| :--- | ---: |
| KNN | $94.60 \%$ |
| MCC | $94.10 \%$ |
| HMM | $96.20 \%$ |
| SVM | $98.20 \%$ |
| DynSVM | $98.20 \%$ |

Hidden Markov Model (HM\&M)

## Yet another idea:



## Hidden Markov Model (HM\&M)



## HMMs

## Another view - "Graphical Model":



Figure by MIT OCW.

## Components of an HMM

$$
\lambda=\{\pi, A, B\}
$$

1) $\pi$ - probability of starting from a particular state

$$
\begin{aligned}
& \pi_{i}=p\left(q_{l}=i\right) \\
& \sum_{i=1}^{N} \pi_{i}=1
\end{aligned}
$$

2) $A$ - probability of moving to a state, given the history

$$
\begin{aligned}
& a_{i j}=p\left(q_{t}=i \mid q_{t-1}=j\right)-\text { Markov assumption } \\
& \sum_{j=1}^{N} a_{i j}=1
\end{aligned}
$$

3) $B$ - probability of outputing a particular observation from a given state:

$$
\begin{aligned}
& b_{i}(o)=p\left(o_{t} \mid q_{t}=i\right) \\
& \int b_{i}(x) d x=1
\end{aligned}
$$

## HMM in Pictures



## HMM Example



## Three Tasks of HMM

1. Given a sequence of observations find a probability of it given the model, $p(O \mid \lambda)$
2. Given a sequence of observations recover a sequence of states, $P(q \mid O, \lambda)$
3. Given a sequence, estimate parameters of the model

## Problem I - Probability Calculation

Take I - brute force:

## Given: $\quad \mathbf{O}=\left(o_{1}, \ldots, o_{T}\right)$ <br> Calculate: $P(\mathbf{O} \mid \lambda)$

Marginalize:

$$
\begin{aligned}
P(\mathbf{O} \mid \lambda) & =\sum_{\forall \mathbf{q}} P(\mathbf{O}, \mathbf{q} \mid \lambda)=\sum_{\forall \mathbf{q}} P(\mathbf{O} \mid \mathbf{q}, \lambda) P(\mathbf{q} \mid \lambda) \\
P(\mathbf{O} \mid \mathbf{q}, \lambda) & =b_{q_{1}}\left(o_{1}\right) b_{q_{2}}\left(o_{2}\right) \ldots b_{q_{T}}\left(o_{3}\right) \quad P(\mathbf{q} \mid \lambda)=\pi_{q_{1}} a_{q_{1} q_{2}} a_{q_{2} q_{3}} \ldots a_{q_{T-1} q_{T}}
\end{aligned}
$$

$$
P(\mathbf{O} \mid \mathbf{q}, \lambda) P(\mathbf{q} \mid \lambda)=\pi_{q_{1}} b_{q_{1}}\left(o_{1}\right) a_{q_{1} q_{2}} b_{q_{2}}\left(o_{2}\right) a_{q_{2} q_{3}} b_{q_{3}}\left(o_{3}\right) \ldots a_{q_{T-1} q_{T}} b_{q_{T}}\left(o_{T}\right)
$$

$$
N \text { states, } T \text { transitions }=>|\mathbf{q}|=\mathrm{N}^{\mathrm{T}}
$$

$$
\mathrm{N}=5, \mathrm{~T}=100 \Rightarrow 2 T N^{T}=2 * 100 * 5^{100} \sim 10^{72} \text { computations }
$$

$$
65536 * 10^{72} \text { particles in the universe }
$$

## Try Again

$$
\begin{aligned}
& P(\mathbf{O} \mid \lambda)=\sum_{\forall \mathbf{q}} P(\mathbf{O}, \mathbf{q} \mid \lambda) \\
& =\sum_{\mathbf{q}=\mathbf{q}_{1}}^{\mathbf{q}_{10^{22}}} \pi_{q(1)} b_{q(1)}\left(o_{1}\right) a_{q(1) q(2)} b_{q(2)}\left(o_{2}\right) a_{q(2) q(3)} b_{q(3)}\left(o_{3}\right) \ldots a_{q(T-1) q(T)} b_{q(T)}\left(o_{T}\right) \\
& =\sum_{m} \sum_{l} \cdots \sum_{j} \sum_{i} \pi_{i} b_{i}\left(o_{1}\right) a_{i j} b_{j}\left(o_{2}\right) a_{j k} b_{k}\left(o_{3}\right) \ldots a_{l m} b_{m}\left(o_{T}\right) \\
& \approx 2 T N^{T}
\end{aligned}
$$

## Problem I - Probability Calculation

Take II - forward procedure:
Define a "forward variable", $\alpha$

$$
\alpha_{t}(i)=P\left(o_{1} o_{2} \ldots o_{t}, q_{t}=i \mid \lambda\right) \quad \text { - probability of seeing the string up to } t
$$ and ending up in state $i$

1. Initialize

$$
\alpha_{1}(i)=\pi_{i} b_{i}\left(o_{1}\right)
$$

2. Induce

$$
\alpha_{t+1}(j)=\left[\sum_{i=1}^{N} \alpha_{t}(i) a_{i j}\right] b_{j}\left(o_{t+1}\right)
$$



## Define a "backward variable", $\beta$

$\beta_{t}(i)=P\left(o_{t+1} o_{t+2} \cdots o_{T} \mid q_{t}=i, \lambda\right) \quad$ - probability of seeing the rest of the string after $t$ and after visiting state $i$ at $t$

1. Initialize

$$
\beta_{T}(i)=1
$$

2. Induce

$$
\beta_{t}(i)=\sum_{j=1}^{N} a_{i j} b_{j}\left(o_{t+1}\right) \beta_{t+1}(j)
$$

3. Terminate


## Task II - Optimal State Sequence

"Optimality" - maximum probability of being in a state $i$ at time $t$.

$$
\text { Given: } \quad \mathbf{O}=\left(o_{1}, \ldots, o_{T}\right)
$$

Find: $\quad q_{t}=\operatorname{argmax} P\left(q_{t} \mid \mathbf{O}, \lambda\right)$
$q$
by Bayes rule

$$
P\left(q_{t}=i \mid \mathbf{O}\right)=\frac{P\left(\mathbf{O}, q_{t}=i\right)}{\sum_{i=1}^{N} P\left(\mathbf{O}, q_{t}=i\right)}
$$


$P\left(\mathbf{O}, q_{t}\right)=P\left(o_{1} \ldots o_{t}, o_{t+1} \ldots o_{T}, q_{t}\right)=P\left(o_{1} \ldots o_{t}, q_{t}\right) P\left(o_{t+1} \ldots o_{T} \mid o_{1} \ldots o_{t}, q_{t}\right)$

$$
=P\left(o_{1} \ldots o_{t}, q_{t}\right) P\left(o_{t+1} \ldots o_{T} \mid q_{t}\right)=\alpha_{t} \beta_{t}
$$

## State Posterior

So,

$$
P\left(q_{t}=i \mid \mathbf{O}\right)=\frac{P\left(\mathbf{O}, q_{t}=i\right)}{\sum_{j=1}^{N} P\left(\mathbf{O}, q_{t}=j\right)}=\frac{\alpha_{t}(i) \beta_{t}(i)}{\sum_{j=1}^{N} \alpha_{t}(j) \beta_{t}(j)}=\gamma_{t}(i)
$$

1. Forward pass - compute $\alpha$ matrix

$$
\begin{aligned}
\approx & N^{2} T \\
\approx & N^{2} T \\
& N T \\
\approx & N^{2} T
\end{aligned}
$$

2. Backward pass - compute $\beta$ matrix
3. Multiply element-by element
4. Normalize columns

What's the problem?
Inconsistent paths - some might not even be allowed

But not entirely useless! We will need it later.

## "Optimality" - single maximum probability path.

$$
\begin{array}{ll}
\text { Given: } & \mathbf{O}=\left(o_{1}, \ldots, o_{T}\right) \\
\text { Find: } & \underset{\mathbf{q}}{\operatorname{argmax}} P(\mathbf{q} \mid \mathbf{O}, \lambda)
\end{array}
$$

Define: $\quad \delta_{t}(i)=\max _{q_{1} q_{2} \ldots q_{t-1}} P\left(q_{1} \ldots q_{t-1}, q_{t}=i, o_{1} \ldots o_{t}\right)$ Max prob. path so far
By the optimality principle (Bellman, '57):

$$
\delta_{t+1}(j)=\left[\max _{i} \delta_{t}(i) a_{i j}\right] b_{j}\left(o_{t+1}\right)
$$

Just need to keep track of max probability states along the way

## Task II - Viterbi Algorithm (cont.)

1. Initialize

$$
\begin{aligned}
& \delta_{1}(i)=\pi_{i} b_{i}\left(o_{1}\right) \quad 1 \leq i \leq N \\
& \psi_{1}(i)=0 \quad \text { Housekeeping variable }
\end{aligned}
$$

2. Recurse

$$
\begin{array}{ll}
\delta_{t}(j)=\max _{1 \leq i \leq N}\left[\delta_{t-1}(i) a_{i j}\right] b_{j}\left(o_{t}\right) & 2 \leq t \leq T \\
& 1 \leq j \leq N \\
\psi_{t}(j)=\underset{1 \leq i \leq N}{\operatorname{argmax}}\left[\delta_{t-1}(i) a_{i j}\right] & 2 \leq t \leq T \\
& 1 \leq j \leq N
\end{array}
$$

3. Terminate

$$
\begin{aligned}
P^{*} & =\max _{1 \leq i \leq N} \delta_{T}(i) \\
q_{T}^{*} & =\underset{\sim}{\operatorname{argmax}} \delta_{T}(i)
\end{aligned}
$$

4. Backtrack

$$
q_{t}^{*}=\psi_{t+1}\left(q_{t+1}^{*}\right) \quad t=(T-1), \ldots, 1
$$



- Similar to the forward procedure
- Typically, you'll do it in log space for speed and underflows:
- replace all parameters with their logarithms
- replace all multiplications with additions


## Task III - Parameter Estimation

## Baum-Welch algorithm (EM for HMMs)

$$
\begin{array}{ll}
\text { Given: } & \mathbf{O}=\left(o_{1}, \ldots, o_{T}\right) \\
\text { Find: } & \pi, A, B
\end{array}
$$

First, introduce another greek letter:

$$
\xi_{t}(i, j)=P\left(q_{t}=i, q_{t+1}=j \mid \mathbf{O}\right)=\frac{P\left(q_{t}=i, q_{t+1}=j, \mathbf{O}\right)}{P(\mathbf{O})}
$$



$$
=\frac{\alpha_{t}(i) a_{i j} b_{j}\left(o_{t+1}\right) \beta_{t}(j)}{P(\mathbf{O})}
$$

## Transition Probability



This leads to:

$$
\bar{a}_{i j}=\frac{E[\#(i \rightarrow j)]}{E[\#(i \rightarrow .)]}=\frac{\sum_{i=1}^{T-1} \xi_{t}(i, j)}{\sum_{t=1}^{T-1} \gamma_{t}(i)}
$$

The rest is easy

## Priors and Outputs

## Prior distribution:

$$
\bar{\pi}_{i}=E[\#(i, t=1)]=\gamma_{1}(i)
$$

Output distribution (discrete):

$$
\bar{b}_{i}(k)=\frac{E\left[\#\left(i, v_{k}\right)\right]}{E[\#(i)]}=\frac{\sum_{t=1}^{\substack{o_{t}=v_{k}}} \gamma_{t}(i)-\begin{array}{l}
\text { Sum probabilities of } \\
\text { being in state } i \text { while } \\
\text { seeing symbol } v_{k}
\end{array}}{\sum_{t=1}^{T} \gamma_{t}(i)} \quad \begin{aligned}
& \text { Normalize }
\end{aligned}
$$



Figure by MIT OCW.

## Continuous Output Case

Output distribution (continuous, Gaussian):

$$
\begin{aligned}
& \bar{b}_{i}(o)=N\left(\mu_{i}, \Sigma_{i}\right) \\
& \bar{\mu}_{i}=\frac{\sum_{t=1}^{T} \gamma_{t}(i) \cdot o_{t}}{\sum_{t=1}^{T} \gamma_{t}(i)} \begin{array}{l}
\text { Observation at time } t \text { weighted } \\
\text { by the probability of being in the } \\
\text { state at that time }
\end{array} \\
& \bar{\Sigma}_{i}=\frac{\sum_{t=1}^{T} \gamma_{t}(i) \cdot\left(o_{t}-\mu_{i}\right)\left(o_{t}-\mu_{i}\right)^{T}}{\sum_{t=1}^{T} \gamma_{t}(i)}
\end{aligned}
$$



Input


Initial state


Output distributions

Transition matrix



How HMM sees it

## Gesture Recognition -Trajectory Model

Modeling a tracked hand trajectory.


## HMM Classifier

Nothing unusual:


Bank of HMMs

## Applications - American Sign Language

## Task: Recognition of sentences of American Sign Language

## 40 word lexicon:

- Single camera
- No special markings on hands
- Real-time

| part of speech | vocabulary <br> pronoun <br> verb <br> l, you, he, we, <br> you(pl), they |
| :--- | :--- |
| noun | want, like, lose, <br> dontwant, <br> dontlike, love, <br> pack, hit, loan |
| box, car, book, <br> table, paper, <br> pants, bicycle, <br> bottle, can, <br> wristwatch, <br> umbrella, coat, <br> pencil, shoes, <br> food, magazine, <br> fish, mouse, pill, <br> bowl |  |
| adjective | red, brown, <br> black, gray, <br> yellow |

Table from: Starner, T., and et. al. "Real-Time American Sign Language Recognition Using Desk and Wearable Computer Based Video." IEEE Transactions on Pattern Analysis and Machine Intelligence (1998). Courtesy of IEEE. Copyright 1998 IEEE. Used with Permission.

## ASL - Features and Model

"Word" model - a 4-state L-R HMM with a single skip transition:


Features
(from skin model):

$$
o=\left[\left(x, y, d x, d y, \operatorname{area}, \theta, \lambda_{\max }, \lambda_{\max } / \lambda_{\min }\right)_{r g k t},(\ldots)_{l f f}\right]^{T}
$$

System 1: Second person


## System 2: First person



Photo marked with black box due to copyright consideration.
Nose could be used for initializing the skin model

## ASL - In Action



Courtesy of Thad Starner. Used with permission.

## Applications - American Sign Language

## 500 sentences ( 400 training, 100 testing)

System 1:

| experiment | training set | test set | \% words recognizedcorrectly |
| :---: | :---: | :---: | :---: |
| all features | 94.10\% | 91.90\% |  |
| relative features | 89.60\% | 87.20\% | Word accuracy,$D+S+I$ |
| all features \& | 81.0\% (87\%) | 74.5\% (83\%) |  |
| unrestricted | ( $\mathrm{D}=31, \mathrm{~S}=287$, | ( $\mathrm{D}=3, \mathrm{~S}=76$, |  |
| grammar | $\mathrm{I}=137, \mathrm{~N}=2390$ ) | $\mathrm{I}=41, \mathrm{~N}=470$ ) |  |

System 2:

| grammar | training set | test set |
| :---: | :---: | :---: |
| part-of-speech | $99.30 \%$ | $97.80 \%$ |
| 5-word sentence | $98.2 \%(98.4 \%)$ |  |
|  | $(\mathrm{D}=5, \mathrm{~S}=36$, |  |
|  | $\mathrm{I}=5 \mathrm{~N}=2500)$ | $97.80 \%$ |
| unrestricted | $96.4 \%(97.8 \%)$ | $96.8 \%(98.0 \%)$ |
|  | $(\mathrm{D}=24, \mathrm{~S}=32$, | $(\mathrm{D}=4, \mathrm{~S}=6, \mathrm{I}=6$, |
|  | $\mathrm{I}=35, \mathrm{~N}=2500)$ | $\mathrm{N}=500)$ |

## Beyond HMM

## Where can we go if HMM is not sufficient?

## Ideas:

- Hierarchical HMM
- More complex models - SCFG

Explicit representation of structure


Capable of generating only a regular language

More expressive, may include memory, but harder to deal with

Figures from: Ivanov, Y., and A. Bobick. "Recognition of Visual Activities and Interactions." IEEE Transactions of Pattern Analysis and Machine Intelligence (2000). Courtesy of IEEE. Copyright 2000 IEEE. Used with Permission.

## Structured Gesture

a)



Problem:
2 directions $=2$ models WHY???

Solution - split the model in two:

- Components (trajectories)
- Structure (events)


## Heterogeneous Representation

- Many high-level activities are sequences of primitives
- Pitching, cooking, dancing, stealing a car from a parking lot
- Components
- Signal level model
- Variability in performance
- Hidden state representation (HMM, etc.)
- Structure
- Event-level model
- Uncertainty in component detections
- State is NOT hidden (SRG, SCFG, etc)
- Right tool for the right task!


## Two-tier Recognition Architecture



## Application: Conducting Music



## Application: Conducting Music

Jean Sibelius, Second Symphony, Opus 43, D Major


Grammar:

| $G_{c}:$ |  |  |  |
| :--- | :--- | :--- | :--- |
| PIECE | $\rightarrow$ | BAR PIECE | $[0.5]$ |
|  |  | BAR | $[0.5]$ |
| BAR | $\rightarrow$ | TWO | $[0.5]$ |
|  |  | THREE | $[0.5]$ |
| THREE | $\rightarrow$ | down3 right3 up3 | $[1.0]$ |
| TWO | $\rightarrow$ | down2 up2 | $[1.0]$ |


|  | Correct |
| :--- | :---: |
| Individual | $\sim 70 \%$ |
| Component | $\sim 85 \%$ |
| Bar | $\sim 95 \%$ |

## Component Detection



## Temporal Consistency

## Grammar:

$$
A \rightarrow a b \mid a b A
$$

Input


## Temporal Consistency

## Grammar:

$A \rightarrow a b \mid a b A$

Input $\qquad$


Figures from: Ivanov, Y., and A. Bobick. "Recognition of Visual Activities and Interactions." IEEE Transactions of Pattern Analysis and Machine Intelligence (2000). Courtesy of IEEE. Copyright 2000 IEEE. Used with Permission.

## Temporal Consistency

## Grammar:

$A \rightarrow a b \mid a b A$
Input


Terminals have temporal extent!


Figures from: Ivanov, Y., and A. Bobick. "Recognition of Visual Activities and Interactions." IEEE Transactions of Pattern Analysis and Machine Intelligence (2000). Courtesy of IEEE. Copyright 2000 IEEE. Used with Permission.

## Temporal Consistency

## Grammar:

$A \rightarrow a b \mid a b A$
Input

Inconsistent parse

## Consistent parse

$\qquad$


Figures from: Ivanov, Y., and A. Bobick. "Recognition of Visual Activities and Interactions." IEEE Transactions of Pattern Analysis and Machine Intelligence (2000). Courtesy of IEEE. Copyright 2000 IEEE. Used with Permission.

## Parsing

The idea is that the top level parse will filter out mistakes in low level detections


Detection adecb

## Stochastic Context-Free Grammar

Example Grammar:


## Event Parsing



For the production $X$, events $a, b$ and $c$ should be consistent

## Application: Musical Conducting



Courtesy of Teresa Marrin-Nakra. Used with permission.

```
Segmentation:
BAR:
    2/4 start/end sample: [0 66]
    Conducted as two quarter beat pattern.
BAR:
    2/4 start/end sample: [66 131]
    Conducted as two quarter beat pattern.
BAR:
    3/4 start/end sample: [131 194]
    Conducted as three quarter beat pattern.
BAR:
    2/4 start/end sample: [194 246]
    Conducted as two quarter beat pattern.
Viterbi probability = 0.00423416
```

|  | Correct |
| :--- | :---: |
| Individual | $\sim 70 \%$ |
| Component | $\sim 85 \%$ |
| Bar | $\sim 95 \%$ |

From Tracking to Classification


How do we describe that?
How do we classify that?
Figure by MIT OCW.

- Outdoor environment - occlusions and lighting changes
- Static cameras
- Real-time performance
- Labeling activities and person-vehicle interactions in a parking lot
- Handling simultaneous events


## Monitoring System



Photos and figures from: Stauffer, Chris, and Eric Grimson, "Learning Patterns of Activity Using Real-Time Tracking." IEEE Transactions on Pattern Recognition and Machine Intelligence (TPAMI 22, no. 8 (2000): 747-757. Courtesy of IEEE, Chris Stauffer, and Eric Grimson.
Copyright 2000 IEEE. Used with Permission.

- Tracker (Stauffer, Grimson)
- assigns identity to the moving objects
- collects the trajectory data into partial tracks
- Event Generator
- maps partial tracks onto a set of events
- Parser
- labels sequences of events according to a grammar
- enforces spatial and temporal constraints


## Tracker

- Adaptive to slow lighting changes:
- Each pixel is modeled by a mixture

$$
P\left(X_{t}\right)=\sum_{i=1}^{K} w_{i, t} * \eta\left(X_{t}, \mu_{i, t}, \Sigma_{i, t}\right)
$$

- Foreground regions are found by connected components algorithm
- Object dynamics is modeled in 2D by a set of Kalman filters
- Details - (Stauffer, Grimson CVPR 99)


## Tracker



Camera view



An object

Photos and figures from: Stauffer, Chris, and Eric Grimson, "Learning Patterns of Activity Using Real-Time Tracking." IEEE Transactions on PatternRecognition and Machine Intelligence (TPAMI) 22, no. 8 (2000): 747-757. Courtesy of IEEE, Chris Stauffer, and Eric Grimson. Copyright 2000 IEEE. Used with Permission.

## Event Generator



Photos and figures from: Stauffer, Chris, and Eric Grimson, "Learning Patterns of Activity Using Real-Time Tracking." IEEE Transactions on Pattern Recognition and Machine Intelligence (TPAMI) 22, no. 8 (2000): 747-757. Courtesy of IEEE, Chris Stauffer, and Eric Grimson. Copyright 2000 IEEE. Used with permission.
Map tracks onto events: car-enter, person-enter, car-found, person-found, car-lost, person-lost, stopped

- Events along with class likelihoods are posted at the endpoints of each track (car-appear [0.5], car-disappear [1.0])
- Action label is assigned to each event in accordance with the environment map (car-enter [0.5], car-exit [1.0])
- Each event is complemented if the label probability is < 1
(car-enter [0.5], person-enter [0.5], car-exit [1.0])


## Parking Lot Grammar (Partial)

| $G_{p}$ : |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| TRACK | $\rightarrow$ |  | CAR-TRACK | [0.5] |
|  |  | I | PERSON-TRACK | [0.5] |
| CAR-TRACK | $\rightarrow$ |  | CAR-THROUGH | [0.25] |
|  |  | I | CAR-PICKUP | [0.25] |
|  |  | I | CAR-0UT | [0.25] |
|  |  | I | CAR-DROP | [0.25] |
| CAR-PICKUP | $\rightarrow$ |  | ENTER-CAR-B CAR-STOP PERSON-LOST B-CAR-EXIT | [1.0] |
| ENTER-CAR-B | $\rightarrow$ |  | CAR-ENTER | [0.5] |
|  |  | 1 | CAR-ENTER CAR-HIDDEN | [0.5] |
| CAR-HIDDEN | $\rightarrow$ |  | CAR-LOST CAR-FOUND | [0.5] |
|  |  | 1 | CAR-LOST CAR-FOUND CAR-HIDDEN | [0.5] |
| B-CAR-EXIT | $\rightarrow$ |  | CAR-EXIT | [0.5] |
|  |  | 1 | CAR-HIDDEN CAR-EXIT | [0.5] |
| CAR-EXIT | $\rightarrow$ |  | car-exit | [0.7] |
|  |  | 1 | SKIP car-exit | [0.3] |
| CAR-LOST | $\rightarrow$ |  | car-lost | [0.7] |
|  |  | 1 | SKIP car-lost | [0.3] |
| CAR-STOP | $\rightarrow$ |  | car-stop | [0.7] |
|  |  | 1 | SKIP car-stop | [0.3] |
| PERSON-LOST | $\rightarrow$ |  | person-lost | [0.7] |
|  |  | 1 | SKIP person-lost | [0.3] |

Photos and figures from: Stauffer, Chris, and Eric Grimson, "Learning Patterns of Activity Using Real-Time Tracking." IEEE Transactions on Pattern Recognition and Machine Intelligence (TPAMI) 22, no. 8 (2000): 747-757. Courtesy of IEEE, Chris Stauffer, and Eric Grimson. Copyright 2000 IEEE. Used with Permission.

## Consistency

- Temporal
- Events should happen in particular order
- Temporally close events are more likely to be related
- Tracks overlapping in time are definitely not related to the same object
- Spatial
- Spatially close events are more likely to be related
- Other
- Objects don't change identity within a track


## Spatio-Temporal Consistency



$$
\mathbf{r}=(x, y), \quad d \mathbf{r}=(d x, d y)
$$

Predict new position:

$$
\mathbf{r}_{p}=\mathbf{r}_{1}+d \mathbf{r}_{1}\left(t_{2}-t_{1}\right)
$$

Penalize:

$$
\begin{aligned}
& \text { Penalize: } f\left(\mathbf{r}_{p}, \mathbf{r}_{2}\right)=\left\{\begin{array}{l}
0, \quad \text { if }\left(t_{2}-t_{1}\right)<0 \\
\exp \left(\frac{\left(\mathbf{r}_{2}-\mathbf{r}_{p}\right)^{T}\left(\mathbf{r}_{2}-\mathbf{r}_{p}\right)}{\theta \square}\right)
\end{array}\right.
\end{aligned}
$$

## Input Data



## Event Generator

| $\begin{aligned} & 11 \\ & \stackrel{1}{0} \\ & 0^{\prime} \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | Event | UID | Avg. Size | Class | P | x | y | t | frame | $\square$ <br> $\frac{\square}{2}$ <br> $\frac{1}{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ENTER | 724 | 0.122553 | 0 | 0.5 | 0.450094 | 0.938069 | 917907137.8 | 1906 |  |
|  | ENTER | 665 | 0.046437 | 1 | 0.5 | 0.6107 | 0.94674 | 917907122.5 | 1799 |  |
|  | PERSON-LEAVE | 665 | 0.045869 | 1 | 0.997846 | 0.648089 | 0.98855 | 917907142.7 | 1938 |  |
|  | STOPPED | 724 |  | 0 | 0.995784 | 0.348569 | 0.345513 | 917907146.5 | 1964 |  |
|  | ENTER | 780 | 0.034293 | 1 | 0.5 | 0.74188 | 0.980292 | 917907151.3 | 1998 |  |
|  | ENTER | 790 | 0.069093 | 0 | 0.5 | 0.814565 | 0.032611 | 917907153.4 | 2012 |  |
|  | FOUND | 787 | 0.033573 | 1 | 0.5 | 0.297585 | 0.357887 | 917907153.1 | 2010 |  |
|  | CAR-LEAVE | 790 | 0.061263 | 0 | 0.997285 | 0.975971 | 0.211984 | 917907155.3 | 2025 |  |
|  | PERSON-LEAVE | 780 | 0.038616 | 1 | 0.999923 | 0.974494 | 0.865237 | 917907158.6 | 2047 |  |
|  | PERSON-LEAVE | 787 | 0.032045 | 1 | 0.999997 | 0.296519 | 0.183704 | 917907158.7 | 2048 |  |
|  | ENTER | 813 | 0.034776 | 1 | 0.5 | 0.012821 | 0.348379 | 917907160.9 | 2063 |  |
|  | ENTER | 816 | 0.093513 | 0 | 0.5 | 0.960425 | 0.793899 | 917907161.9 | 2070 |  |
|  | CAR-LEAVE | 724 | 0.097374 | 0 | 0.993211 | 0.972272 | 0.693728 | 917907165.2 | 2091 |  |
|  | CAR-LEAVE | 816 | 0.089424 | 0 | 0.99023 | 0.693699 | 0.990798 | 917907165.2 | 2091 |  |

## Interleaved events in the input stream

Figures from Ivanov, Yuri, Chris Stauffer, Aaron Bobick, W. E. L. Grimson. "Video Surveillance of Interactions." IEEE Workshop on Visual Surveillance (ICCV 2001) (1999). Courtesy of IEEE, Yuri Ivanov, Chris Stauffer, Aaron Bobick, and W. E. L. Grimson. Copyright 1999 IEEE. Used with Permission.

## Parse 1: Person-Pass-Through

Action label
Component labels
Object track


Figures from Ivanov, Yuri, Chris Stauffer, Aaron Bobick, W. E. L. Grimson. "Video Surveillance of Interactions." IEEE Workshop on Visual Surveillance (ICCV 2001) (1999). Courtesy of IEEE, Yuri Ivanov, Chris Stauffer, Aaron Bobick, and W. E. L. Grimson. Copyright 1999 IEEE. Used with Permission.

## Parse 2: Drive-In

## Action label

## Component labels

## Object tracks



Figures from Ivanov, Yuri, Chris Stauffer, Aaron Bobick, W. E. L. Grimson. "Video Surveillance of Interactions." IEEE Workshop on Visual Surveillance (ICCV 2001) (1999). Courtesy of IEEE, Yuri Ivanov, Chris Stauffer, Aaron Bobick, and W. E. L. Grimson.
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## Parse 3: Drop-off

Action label
Component labels

## Object track



## Temporal extent

Figures from Ivanov, Yuri, Chris Stauffer, Aaron Bobick, W. E. L. Grimson. "Video Surveillance of Interactions." IEEE Workshop on Visual Surveillance (ICCV 2001) (1999). Courtesy of IEEE, Yuri Ivanov, Chris Stauffer, Aaron Bobick, and W. E. L. Grimson. Copyright 1999 IEEE. Used with Permission.

## Parse 4: Car-Pass-Through

## Action label

## Component labels

## Object track



## Temporal extent

Figures from Ivanov, Yuri, Chris Stauffer, Aaron Bobick, W. E. L. Grimson. "Video Surveillance of Interactions." IEEE Workshop on Visual Surveillance (ICCV 2001) (1999). Courtesy of IEEE, Yuri Ivanov, Chris Stauffer, Aaron Bobick, and W. E. L. Grimson. Copyright 1999 IEEE. Used with Permission.

- Real-time system
- First of a kind end-to end system
- Extended robust parsing algorithm
- Events are staged in real environment with other cars and people
- ~10-15 events per minute
- Staged events $-100 \%$ detected
- Accidental events - $\sim 80 \%$ detected
- Outdoor environment - occlusions and lighting changes
- Static cameras
- Real-time performance
- Labeling activities and person-vehicle interactions in a parking lot
- Handling simultaneous events


## Appendix: Hu Moments

## Image Moments

The two-dimensional $(p+q)$ th order moments of a density distribution function $\rho(x, y)$ (e.g., image intensity) are defined in terms of Riemann integrals as:

$$
\begin{equation*}
m_{p q}=\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} x^{p} y^{\rho} \rho(x, y) d x d y \tag{1}
\end{equation*}
$$

for $p, q=0,1,2, \cdots$.
The central moments $\mu_{p q}$ are defined as:

$$
\begin{equation*}
\mu_{p q}=\int_{-\infty}^{\infty} \int_{-\infty}^{\infty}(x-\bar{x})^{p}(y-\bar{y})^{q} \rho(x, y) d(x-\bar{x}) d(y-\bar{y}) \tag{2}
\end{equation*}
$$

where

$$
\begin{aligned}
& \bar{x}=m_{10} / m_{00}, \\
& \bar{y}=m_{01} / m_{01} .
\end{aligned}
$$

It is well-known that under the translation of coordinates, the central moments do not change, and are therefore invariants under translation. It is quite easy to express the central moments $\mu_{p q}$ in terms of the ordinary moments $m_{\rho q}$. For the first four orders, we have

$$
\begin{aligned}
& \mu_{00}=m_{00} \equiv \mu \\
& \mu_{10}=0 \\
& \mu_{01}=0 \\
& \mu_{20}=m_{20}-\mu \bar{x}^{2} \\
& \mu_{11}=m_{11}-\mu \bar{x} \bar{y} \\
& \mu_{02}=m_{02}-\mu \bar{y}^{2} \\
& \mu_{00}=m_{30}-3 m_{20} \bar{x}+2 \mu \bar{x}^{3} \\
& \mu_{21}=m_{21}-m_{20} \bar{y}-2 m_{11} \bar{x}+2 \mu \bar{x}^{2} \bar{y} \\
& \mu_{12}=m_{12}-m_{02} \bar{x}-2 m_{11} \bar{y}+2 \mu \bar{x} \bar{y}^{2} \\
& \mu_{03}=m_{03}-3 m_{02} \bar{y}+2 \mu \bar{y}^{3} .
\end{aligned}
$$

To achieve invariance with respect to orientation and scale, we first normalize for scale defining $\eta_{p q}$ :

$$
\eta_{p q}=\frac{\mu_{p q}}{\left(\mu_{\infty}\right)^{\gamma}},
$$

where $\gamma=(p+q) / 2+1$ and $p+q \geq 2$. The first seven orientation invariant Hu moments are defined as:

$$
\begin{aligned}
\nu_{1}= & \eta_{20}+\eta_{02} \\
\nu_{2}= & \left(\eta_{20}-\eta_{02}\right)^{2}+4 \eta_{11}^{2} \\
\nu_{3}= & \left(\eta_{00}-3 \eta_{12}\right)^{2}+\left(3 \eta_{21}-\eta_{03}\right)^{2} \\
\nu_{4}= & \left(\eta_{00}+\eta_{12}\right)^{2}+\left(\eta_{21}+\eta_{03}\right)^{2} \\
\nu_{5}= & \left(\eta_{00}-3 \eta_{12}\right)\left(\eta_{30}+\eta_{12}\right)\left[\left(\eta_{00}+\eta_{12}\right)^{2}-3\left(\eta_{21}+\eta_{03}\right)^{2}\right] \\
& +\left(3 \eta_{21}-\eta_{03}\right)\left(\eta_{21}+\eta_{03}\right) \\
& \cdot\left[3\left(\eta_{00}+\eta_{12}\right)^{2}-\left(\eta_{21}+\eta_{03}\right)^{2}\right] \\
\nu_{6}= & \left(\eta_{00}-\eta_{02}\right)\left[\left(\eta_{00}+\eta_{12}\right)^{2}-\left(\eta_{21}+\eta_{03}\right)^{2}\right] \\
& +4 \eta_{11}\left(\eta_{00}+\eta_{12}\right)\left(\eta_{21}+\eta_{03}\right) \\
\nu_{7}= & \left(3 \eta_{21}-\eta_{03}\right)\left(\eta_{30}+\eta_{12}\right)\left[\left(\eta_{00}+\eta_{12}\right)^{2}-3\left(\eta_{21}+\eta_{03}\right)^{2}\right] \\
& -\left(\eta_{00}-3 \eta_{12}\right)\left(\eta_{21}+\eta_{03}\right)\left[3\left(\eta_{50}+\eta_{12}\right)^{2}-\left(\eta_{21}+\eta_{03}\right)^{2}\right]
\end{aligned}
$$

These moments can be used for pattern identification independent of position, size, and orientation.

Full appendix from: Bobick, A., and J. Davis. "The Representation and Recognition of Action Using Temporal Templates." IEEE Transactions on Pattern Analysis and Machine Intelligence 23, no. 3 (2002). Courtesy of IEEE. Copyright 2002 IEEE. Used with Permission.

