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<u>Criteria for Spontaneous Change</u>

The 2nd Law gave the Clausius inequality for spontaneous change

 $dS > dq/T_{surr.}$

The $1^{s^{\dagger}}$ law gave us dU = dq + dw

Putting the two together, assuming only pV work, gives us the following <u>general</u> criterion for spontaneous change:

** $dU + p_{ext}dV - T_{surr}dS < 0$ **

Equilibrium is when there is no possible change of state that would satisfy this inequality.

We can now use the general criterion above under <u>specific</u> conditions

• Consider first an isolated system (q=w=0, Δ V=0, Δ U=0)

Since dU=0 and dV=0, from the general criterion above, then

(dS)_{U,V} > 0

is the criterion for spontaneity for an *isolated* system

And equilibrium for an <u>isolated</u> system is then achieved when <u>entropy</u> <u>is maximized</u>. At maximum entropy, no spontaneous changes can occur.

Consider now <u>S and V constant</u>

 \Rightarrow (dU)_{S,V} < 0

is the criterion for spontaneity under <u>constant V and S</u>

At <u>constant S and V</u>, equilibrium is achieved when <u>energy is</u> <u>minimized</u>

• Consider now <u>S constant and p=p_{ext} constant</u>

$$\Rightarrow dU + pdV < 0 \Rightarrow d(U + pV) < 0$$

$$\downarrow$$
=H

So

$$\Rightarrow$$
 (dH)_{S,pext} < 0

is the criterion for spontaneity under <u>constant S and constant $p=p_{ext}$ </u>.

• Consider now <u>H constant and p=p_{ext} constant</u>

$$dU + pdV - T_{surr}dS < 0$$

but dU + pdV = dH, which is 0 (H is constant)

So
$$(dS)_{H,p=pext} > 0$$

is the criterion for spontaneity under <u>constant H and constant $p=p_{ext}$ </u>.

Now let's begin considering cases that are <u>experimentally</u> more controllable.

• Consider now <u>constant T=T_{surr} and constant V</u>

$$\Rightarrow$$
 dU - TdS < 0 \Rightarrow d(U - TS) < 0

Define A = U - TS, the Helmholtz Free Energy

- Then $(dA)_{V,T=Tsurr} < 0$
- is the criterion for spontaneity under constant $T=T_{surr}$ and constant V.

For constant V and constant $T=T_{surr}$, equilibrium is achieved when the Helmholtz free energy is minimized.

We now come to the most <u>important and applicable</u> constraint:
Consider now constant T=T_{surr} and constant p=p_{ext}.

$$(dU + pdV - TdS) < 0 \implies d(U + pV - TS) < 0$$

<u>Define</u> G = U + pV - TS, the Gibbs Free Energy

(can also be written as G = A + pV and G = H - TS)

Then
$$(dG)_{p=pext,T=Tsurr} < 0$$

is the criterion for spontaneity under <u>constant $T=T_{surr}$ and constant</u> <u> $p=p_{ext}$ </u>.

At constant $p=p_{ext}$ and constant $T=T_{surr}$, equilibrium is achieved when the <u>Gibbs free energy is minimized</u>.

Consider the process:

A(p,T) = B(p,T) (keeping p and T constant)

Under constant
$$p=p_{ext}$$
 and $T=T_{surr}$,
 $\Delta G < 0 \qquad A \rightarrow B$ is spontaneous
 $\Delta G = 0 \qquad A$ and B are in equilibrium
 $\Delta G > 0 \qquad$ then B $\rightarrow A$ is spontaneous