### 1.85 WATER AND WASTEWATER TREATMENT ENGINEERING HOMEWORK 5

Question 1 (4 points)
The water defined by the analysis given below is to be softened by excess-lime (and soda ash) treatment.
a. Sketch an meq/L bar graph (1 point).
b. Calculate the softening chemicals required (3 points).
c. Draw a bar graph for the softened water after recarbonation and filtration, assuming that $80 \%$ of the alkalinity is in the bicarbonate form (1 point).

| $\mathrm{CO}_{2}$ | $8.8 \mathrm{mg} / \mathrm{L}$ |
| :--- | :---: |
| $\mathrm{Ca}^{2+}$ | $40.0 \mathrm{mg} / \mathrm{L}$ |
| $\mathrm{Mg}^{2+}$ | $14.7 \mathrm{mg} / \mathrm{L}$ |
| $\mathrm{Na}^{+}$ | $13.7 \mathrm{mg} / \mathrm{L}$ |


| $\mathrm{ALK}\left(\mathrm{HCO}_{3}{ }^{-}\right)$ | $135 \mathrm{mg} / \mathrm{L}$ |
| :--- | :---: |
| $\mathrm{SO}_{4}{ }^{-}$ | $29.0 \mathrm{mg} / \mathrm{L}$ |
| $\mathrm{Cl}^{-}$ | $17.8 \mathrm{mg} / \mathrm{L}$ |

ANSWER - See solution to follow

## Solution for Homework 5, Problem 1

| Cations |  |  |  | Anions |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ion | MW | Charge | Conc | Equiv. | Ion | MW |  | Conc | Equiv. |
|  |  |  | $(\mathrm{mg} / \mathrm{L})$ | $(\mathrm{meq} / \mathrm{L})$ |  |  |  | $(\mathrm{mg} / \mathrm{L})$ | $(\mathrm{meq} / \mathrm{L})$ |


| $\mathrm{CO}_{2}$ | 44 | 2 | 8.8 | 0.40 |
| :--- | :--- | :--- | :--- | :--- |


| $\mathrm{Ca}^{2+}$ | 40 | 2 | 40 | 2.00 | $\mathrm{Alk}\left(\mathrm{HCO}_{3}{ }^{-}\right)$ | 50 | 1 | 135 | 2.70 |
| :--- | ---: | ---: | ---: | ---: | :--- | ---: | ---: | ---: | ---: |
| $\mathrm{Mg}^{2+}$ | 24.3 | 2 | 14.7 | 1.21 | $\mathrm{SO}_{{ }^{2-}}$ | 96 | 2 | 29 | 0.60 |
| $\mathrm{Na}^{+}$ | 23 | 1 | 13.7 | 0.60 | $\mathrm{Cl}^{-}$ | 35.5 | 1 | 17.8 | 0.50 |

Check charge balance:
Total cations: $3.81 \quad$ Total anions: 3.81
a. Sketch an meq/L bar graph


Note: scale is approximate but numbers are accurate to two digits.

| Hardness $=$ | $3.21 \mathrm{meq} / \mathrm{L}$ | $160 \mathrm{mg} / \mathrm{L}$ as $\mathrm{CaCO}_{3}$ |
| :--- | :--- | ---: |
| Strong bases $=$ | $3.81 \mathrm{meq} / \mathrm{L}$ | $190 \mathrm{mg} / \mathrm{L}$ as $\mathrm{CaCO}_{3}$ |
| Strong acids $=$ | $1.11 \mathrm{meq} / \mathrm{L}$ | $55 \mathrm{mg} / \mathrm{L}$ as $\mathrm{CaCO}_{3}$ |
| Alk = | $2.70 \mathrm{meq} / \mathrm{L}$ | $135 \mathrm{mg} / \mathrm{L}$ as $\mathrm{CaCO}_{3}$ |
| Carb hardness = | $2.70 \mathrm{meq} / \mathrm{L}$ | $135 \mathrm{mg} / \mathrm{L} \mathrm{as} \mathrm{CaCO}_{3}$ |
| Ca carb hardness = | $2.00 \mathrm{meq} / \mathrm{L}$ | $100 \mathrm{mg} / \mathrm{L} \mathrm{as} \mathrm{CaCO}_{3}$ |
| Mg carb hardness = | $0.71 \mathrm{meq} / \mathrm{L}$ | $36 \mathrm{mg} / \mathrm{L}$ as $\mathrm{CaCO}_{3}$ |
| Non-carb hardness = | $0.51 \mathrm{meq} / \mathrm{L}$ | $25 \mathrm{mg} / \mathrm{L}$ as $\mathrm{CaCO}_{3}$ |
| Mg NCH = | $0.51 \mathrm{meq} / \mathrm{L}$ | $25 \mathrm{mg} / \mathrm{L}$ as $\mathrm{CaCO}_{3}$ |

b. Calculate the softening chemicals required

Lime requirement:

| Component |  | $\mathrm{mg} / \mathrm{L}$ as $\mathrm{CaCO}_{3}$ | meq/L | Lime as $\mathrm{CaCO}_{3}$ |
| :---: | :---: | :---: | :---: | :---: |
| Lime for $\mathrm{CO}_{2}$ | $\mathrm{CO}_{2}$ | 20 | 0.40 | 20 |
| Lime for CaCH | $\mathrm{Ca}\left(\mathrm{HCO}_{3}\right)_{2}$ | 100 | 2.00 | 100 |
| Lime for Mg CH | $\mathrm{Mg}\left(\mathrm{HCO}_{3}\right)_{2}$ | 36 | 0.71 | 71 |
| Lime for non-carb hardness | NCH | 25 | 0.51 | 25 |
| Total lime needed | Total | 181 | 3.62 | 216 |
| Total lime as CaO |  |  | $\mathrm{mg} / \mathrm{L}$ as C |  |
| Plus excess lime |  | 35 | $\mathrm{mg} / \mathrm{L}$ as C |  |
| Total lime including excess |  | 156 | $\mathrm{mg} / \mathrm{L}$ as C |  |

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## Solution for Homework 5, Problem 1

Soda ash requirement:

| Component |  | $\mathrm{mg} / \mathrm{L}$ as <br> $\mathrm{CaCO}_{3}$ | $\mathrm{meq} / \mathrm{L}$ | Soda as <br> $\mathrm{CaCO}_{3}$ |
| :--- | :--- | ---: | ---: | ---: |
| Soda for non-carb hardness | NCH | 25 | 0.51 | 25 |
| Total soda ash needed | Total | 25 | 0.51 | 25 |
|  |  |  |  |  |
| Total soda ash as $\mathrm{Na}_{2} \mathrm{CO}_{3}$ |  | 27 | $\mathrm{mg} / \mathrm{L}$ as $\mathrm{Na}_{2} \mathrm{CO}_{3}$ |  |

c. Draw a bar graph for the softened water after recarbonation and filtration, assuming that $80 \%$ of the alkalinity is in the bicarbonate form


Question 2 (2 points)
A small community has used an unchlorinated ground-water supply containing approximately $0.3 \mathrm{mg} / \mathrm{L}$ of iron and manganese for several years without any apparent iron and manganese problems. A health official suggested that the town install chlorination equipment to disinfect the water and provide a chlorine residual in the distribution system. After initiating chlorination, consumers complained about water staining washed clothes and bathroom fixtures. Explain what is occurring due to chlorination.
ANSWER: Chlorine is a strong oxidizer and is oxidizing the iron and the manganese. The oxidized iron and manganese is relatively insoluble and forms precipitates. These precipitates cause the stains on fixtures and laundry. Apparently, before chlorination, the iron and manganese remained dissolved or as fine colloids and passed through the system without causing problems.

Question 3 (2 points)
A wastewater containing phenol at a concentration of $0.4 \mathrm{mg} / \mathrm{L}$ is to be treated by granular activated carbon. Batch tests have been performed in the laboratory to determine the relative adsorption of phenol by GAC. Testing entails adding a mass of carbon to $\mathrm{V}=1$ liter of the $0.4 \mathrm{mg} / \mathrm{L}$-solution, allowing the solution to reach equilibrium over 6 days, and then measuring the resulting equilibrium concentration of phenol. Results are shown in the table below. Develop a Freundlich isotherm to fit these data.

| Mass of carbon, <br> $M(\mathrm{gm})$ | Initial conc., <br> $\mathrm{C}_{0}(\mathrm{mg} / \mathrm{L})$ | Equilibrium conc <br> $\mathrm{C}_{\mathrm{e}}(\mathrm{mg} / \mathrm{L})$ |
| :---: | :---: | :---: |
| 0.52 | 0.400 | 0.322 |
| 2.32 | 0.400 | 0.117 |
| 3.46 | 0.400 | 0.051 |
| 3.84 | 0.400 | 0.039 |
| 4.50 | 0.400 | 0.023 |
| 5.40 | 0.400 | 0.012 |
| 6.67 | 0.400 | 0.0061 |
| 7.60 | 0.400 | 0.0042 |
| 8.82 | 0.400 | 0.0023 |

Answer: From spreadsheet calculation:

Data tabulation:

| Mass of carbon, M | Initial conc. $\mathrm{C}_{0}$ | $\begin{gathered} \text { Equil. conc } \\ C_{A} \end{gathered}$ | $\mathrm{C}_{0}-\mathrm{C}_{\mathrm{A}}$ | V * $\left(\mathrm{C}_{0}-\mathrm{C}_{\mathrm{A}}\right)$ | $\mathrm{q}_{\mathrm{A}}=\mathrm{V}\left(\mathrm{C}_{0}-\mathrm{C}_{\mathrm{A}}\right) / \mathrm{M}$ | $\log \mathrm{C}_{\mathrm{A}}$ | $\log \mathrm{q}_{\mathrm{A}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (g) | (mg/L) | (mg/L) | (mg/L) | (mg) | ( $\mathrm{mg} / \mathrm{g}$ ) |  |  |
| 0.52 | 0.4 | 0.322 | 0.078 | 0.078 | 0.150 | -0.492 | -0.824 |
| 2.32 | 0.4 | 0.117 | 0.283 | 0.283 | 0.122 | -0.932 | -0.914 |
| 3.46 | 0.4 | 0.051 | 0.349 | 0.349 | 0.101 | -1.292 | -0.996 |
| 3.84 | 0.4 | 0.039 | 0.361 | 0.361 | 0.094 | -1.409 | -1.027 |
| 4.5 | 0.4 | 0.023 | 0.377 | 0.377 | 0.084 | -1.638 | -1.077 |
| 5.4 | 0.4 | 0.012 | 0.388 | 0.388 | 0.072 | -1.921 | -1.144 |
| 6.67 | 0.4 | 0.0061 | 0.3939 | 0.3939 | 0.059 | -2.215 | -1.229 |
| 7.6 | 0.4 | 0.0042 | 0.3958 | 0.3958 | 0.052 | -2.377 | -1.283 |
| 8.82 | 0.4 | 0.0023 | 0.3977 | 0.3977 | 0.045 | -2.638 | -1.346 |
| Mass of adsorbent |  | Liquid phase concentration | Change in conc. in water | Mass adsorbed to carbon | Solid phase concentration |  |  |

Data are plotted below and fall more or less on a straight line. Determine approximate slope from first and last points on line: (Note that linear regression would be more accurate.)

Slope $=1 / n=\left[\left(\log q_{A, \max }\right)-\log \left(\mathrm{q}_{\mathrm{A}, \text { min }}\right)\right] /\left[\log \left(\mathrm{C}_{\mathrm{A}, \max }\right)-\log \left(\mathrm{C}_{\mathrm{A}, \min }\right)\right]$
$1 / n=$
0.243

Next determine $K_{F}=q_{A} / C_{A} / n$ for each data point and find average $K_{F}$ value:

| Mass of carbon, <br> $M$ | Equil. conc <br> $\mathrm{C}_{\mathrm{A}}$ | $\mathrm{q}_{\mathrm{A}}$ <br> $=\mathrm{V}\left(\mathrm{C}_{0}-\mathrm{C}_{\mathrm{A}}\right) / \mathrm{M}$ | $\mathrm{K}_{\mathrm{F}}=\mathrm{q}_{\mathrm{A}} / \mathrm{C}_{\mathrm{A}}{ }^{1 / \mathrm{n}}$ |
| :---: | :---: | ---: | ---: |
| $(\mathrm{g})$ | $(\mathrm{mg} / \mathrm{L})$ | $(\mathrm{mg} / \mathrm{g})$ |  |
| 0.52 | 0.322 | 0.150 | 0.198 |
| 2.32 | 0.117 | 0.122 | 0.206 |
| 3.46 | 0.051 | 0.101 | 0.208 |
| 3.84 | 0.039 | 0.094 | 0.207 |
| 4.5 | 0.023 | 0.084 | 0.210 |
| 5.4 | 0.012 | 0.072 | 0.211 |
| 6.67 | 0.0061 | 0.059 | 0.204 |
| 7.6 | 0.0042 | 0.052 | 0.197 |
| 8.82 | 0.0023 | 0.045 | 0.198 |
|  | Average $=$ |  |  |

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Data plot:
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Question 4 (2 points)
An ion exchange resin is used to remove nitrate from a water supply with the ionic concentrations shown below. The total resin capacity is 1.5 equivalents per liter of resin.

| Cations | meq/L |
| :--- | ---: |
| $\mathrm{Ca}^{2+}$ | 1.4 |
| $\mathrm{Mg}^{2+}$ | 0.8 |
| $\mathrm{Na}^{+}$ | 2.6 |


| Anions | meq/L |
| :--- | ---: |
| $\mathrm{SO}_{4}{ }^{2-}$ | 0.0 |
| $\mathrm{Cl}^{-}$ | 3.0 |
| $\mathrm{NO}_{3}{ }^{-}$ | 1.8 |

d. Do the anions and cations balance? (1 point).
e. What volume of water can be treated with each liter of resin? (2 points)
f. Qualitatively, how would your answer differ if the concentrations of $\mathrm{Cl}^{-}$and $\mathrm{SO}_{4}^{-}$ were reversed? (1 point).

## Answer:

a. $\quad$ cations $=4.8 \mathrm{meq} / \mathrm{L}$ Eanions $=4.8 \mathrm{meq} / \mathrm{L} \quad$ Charges balance!.
b. Each liter of resin can remove 1.5 equivalents. Only chloride is present in quantity and nitrate is well above chloride in ion exchanger preference series shown in lecture, therefore can ignore exchange of ions other than nitrate:

Concentration of nitrate $=1.8 \times 10^{-3} \mathrm{eq} / \mathrm{L}$
Volume treated $=1.5 \mathrm{eq} / 1.8 \times 10^{-3} \mathrm{eq} / \mathrm{L}=833$ liters
C. Since $\mathrm{SO}_{4}$ is above $\mathrm{NO}_{3}$ in the preference series, if $\mathrm{SO}_{4}$ were present rather than $\mathrm{Cl}, \mathrm{SO}_{4}$ would be adsorbed instead of $\mathrm{NO}_{3}$. There were would be far less, if any, $\mathrm{NO}_{3}$ adsorption. Another resin or much greater amount of resin would be needed.


[^0]:    * Note Mg carbonate hardness requires double lime dose

