# ASSET PRICE APPROACH TO INCIDENCE 

### 14.471-Fall 2012

Many taxes are levied on durable assets (houses, physical capital such as buildings and equipment, patents, natural resource stocks)

These are traded assets with prices - changes in current and future taxes can affect these prices.

Key component of incidence: price changes for existing asset owners. How much do prices change? By the change in the present discounted value of future tax payments associated with that asset.

Best illustrations are in markets with long-lived assets: corporate capital, land, housing are examples. Focus on owner-occupied homes following Poterba QJE 1984.

Equilibrium condition in durable asset market:
Value of asset services per unit: $\mathrm{R}(\mathrm{H})$

## $\mathrm{R}^{\prime}(\mathrm{H})<0$ reflects diminishing value of housing capital

$\mathrm{R}(\mathrm{H})$ must equal the investor cost of holding the asset for one period. This cost includes the depreciation of the asset (exponential at rate $\delta$ per period) and the opportunity cost of funds. We denote this as $(1-\tau)$ r: the after-tax interest rate. There might also be a risk premium, but assume not for now.

The investor cost also includes any capital gain or loss to holding the asset. A capital gain reduces the investor cost of holding the asset; a capital loss increases it.
$q_{H, t}=$ asset price at the start of period t

$$
q_{H, t+1}-q_{H, t}=\text { capital gain or loss during period } \mathrm{t}
$$

## Equilibrium Condition:

$$
\text { (1) } R\left(H_{t}\right)=q_{H, t}(r(1-\tau)+\delta)-\left(q_{H, t+1}-q_{H, t}\right)
$$

Consider a tax on each house that takes the form of a required payment $T_{t}$ in period $t$. Because houses are longlived assets, even taxes that will not be levied until future years can depress prices today. In each period when the tax is levied, the equilibrium condition becomes
(2) $R\left(H_{t}\right)-T_{t}=q_{H, t}(1+r(1-\tau)+\delta)-q_{H, t+1}$.

Note that $q_{H, t+1}$ is not generally know at time period t . Assume perfect foresight; one could also embed this analysis in a stochastic model of price determination.

To find the $q_{H}$ from (2), solve forward by rewriting (2) as:

$$
\begin{equation*}
q_{H, t}=\frac{R\left(H_{t}\right)-T_{t}+q_{H, t+1}}{1+r(1-\tau)+\delta} \tag{3}
\end{equation*}
$$

Solving recursively by substituting for $q_{H, t+1}$ yields, after multiple substitutions,
(4) $\quad q_{H, t}=\sum_{i=0}^{S} \frac{R\left(H_{t+i}\right)-T_{t+i}}{(1+r(1-\tau)+\delta)^{j+1}}+\frac{q_{H, t+S}}{(1+r(1-\tau)+\delta)^{S+1}}$.

We impose a transversality condition to rule out an "exploding" asset price:

$$
\begin{equation*}
\lim _{S \rightarrow \infty} \frac{q_{H, t+S}}{(1+r(1-\tau)+\delta)^{S+1}}=0 . \tag{5}
\end{equation*}
$$

With this condition we can see how a stream of tax liabilities $\left\{\mathrm{T}_{\mathrm{t}}\right\}$ will affect the price of houses:

$$
\begin{equation*}
q_{H, t}=\sum_{i=0}^{\infty} \frac{R\left(H_{t+i}\right)}{(1+r(1-\tau)+\delta)^{i+1}}-\sum_{i=0}^{\infty} \frac{T_{t+i}}{(1+r(1-\tau)+\delta)^{i+1}} . \tag{6}
\end{equation*}
$$

The second term is the present discounted value of current and future tax payments.

If the stock of housing is fixed, so $H_{t+i}=H_{t}$ for all $i$, then from (6) we can determine $d q_{t, t} / d T_{t+i}$. When the housing stock is endogenous, however, changes in future tax policies will also affect current and future investment, hence $\left\{H_{t}\right\}$. In general the effect of changing $\left\{H_{t}\right\}$ will offset the effect of taxes on house prices. When taxes rise, thereby depressing prices, housing construction will
decline. That will raise the rental value of a unit of housing services, thereby helping to raise prices.

Need to model supply function for new construction:
(7) $\quad I_{t}=\psi\left(q_{H, t}\right)$
where $I_{t}$ denotes gross construction of new housing. The net change in the housing stock is given by
(8) $\quad H_{t+1}-H_{t}=\psi\left(q_{H, t}\right)-\delta H_{t}$.

The corresponding equation for the evolution of house prices from (2) is
(9) $\quad q_{H, t+1}-q_{H, \mathrm{t}}=(r(1-\tau)+\delta) q_{H, t}-R\left(H_{t}\right)+T_{t}$.

Equations (8) and (9) define a two-equation system of difference equations in two variables: $\left(q_{H}, H\right)$. To analyze
how the value of $q_{H, t}$ responds to a shock to $\left\{\mathrm{T}_{t}\right\}$, we analyze the stability properties of this system of difference equations using phase diagram methods.
The figure below shows the loci on which $q_{H}$ and $H$ are respectively constant. The steady state is defined by:
(10) $\psi\left(q_{H}\right)=\delta H$ and $(r(1-\tau)+\delta) q_{H}=R(H)-T$.

When the system is out of equilibrium, for example when a tax shock moves the $\left(d q_{H} / d t\right)$ curve, there is a unique stable path that leads to the equilibrium point; conditional on a value of $H$, there is only one value of $q_{H}$ that will result in the system evolving back to the equilibrium.


One can link this diagram to the basic partial equilibrium incidence diagram we have used before. Note that even when the $d H / d t=0$ locus is horizontal, so there is a fixed long-run supply price of housing, a leftward shift in the $d q_{H} / d t=0$ locus induced for example by a new tax on housing would create a transitory decline in house prices that would burden existing house owners.

To illustrate how this framework can be used to evaluate changes to housing tax policy, consider a plausible measure of the user cost of owner-occupied housing in the current tax law:
(11) $\mathrm{c}=\left[1-\tau_{\mathrm{y}}\right]^{*}\left(\lambda \mathrm{r}_{\mathrm{M}}+(1-\lambda) \mathrm{r}_{\mathrm{Alt}}+\beta\right)+\mathrm{m}+\left(1-\tau_{\text {ded }}\right) * \tau_{\text {prop }}-\pi_{\mathrm{e}}$
where $\tau_{\mathrm{y}}$ is the marginal income tax rate for mortgage interest and property tax deductions as well as investment income, $r_{M}$ is the mortgage interest rate, $\lambda$ is the loan-tovalue ratio on the house (fraction of house financed with mortgage), $\mathrm{r}_{\text {Alt }}$ is the return on the alternative assets that the household might invest in if not using equity for a house, $\beta$ denotes the pre-tax housing risk premium, m is the combined cost of depreciation and maintenance, $\tau_{\text {prop }}$ is the property tax rate, and $\pi_{\mathrm{e}}$ is the expected rate of nominal house price appreciation. Plausible parameter values for 2012 might be: $\tau_{\mathrm{y}}=.25, \mathrm{r}_{\mathrm{M}}=\mathrm{r}_{\text {Alt }}=.04, \lambda=$ $0.75, \beta=\mathrm{m}=.02, \tau_{\text {prop }}=.015, \pi_{\mathrm{e}}=.02$. This implies $\mathrm{c}=$ 0.05625 .

What if we eliminate the federal income tax deduction for the property tax? Now $c^{\prime}=0.06$. This is an increase of 6.7 percent; with fixed H and a price elasticity of demand of -1 , house prices would drop by 6.7 percent. Calibrated rational expectations model suggests -3.7 percent.

Empirical work to be done in asset price models:
(i) estimate elasticity of demand for the durable asset (this is calibrating $\mathrm{R}(\mathrm{H})$ );
(ii) estimate supply curve $\psi\left(\mathrm{q}_{\mathrm{H}}\right)$
(iii) estimate how other endogenous variables (loan-tovalue ratio, level of property taxes) might respond to changes in federal tax rules.

Estimates of User Costs of Owner-Occupied Housing in 2003 (from Poterba \& Sinai, Natl Tax Jnl 2011; average $=0.059$ )

| Age of Head | $<40 \mathrm{~K}$ | $40-75 \mathrm{~K}$ | $75-125 \mathrm{~K}$ | $125-$ | $250+$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $25-34$ | 0.065 | 0.060 | 0.053 | 0.048 | 0.045 |
| $35-49$ | 0.065 | 0.059 | 0.054 | 0.049 | 0.046 |
| $50-64$ | 0.066 | 0.059 | 0.055 | 0.050 | 0.046 |
| $65+$ | 0.070 | 0.059 | 0.056 | 0.053 | 0.049 |
| All | 0.068 | 0.059 | 0.054 | 0.050 | 0.046 |

## Applications of Asset Price Incidence Analysis:

Proposition 13 in California: Property Tax Reform (K. Rosen, JPE 1982)

| Community | Property Tax Rate <br> FY1978 | Property Tax Rate <br> FY1979 |
| :--- | :--- | :--- |
| Berkeley | 13.75 | 5.04 |
| Pleasanton | 12.83 | 5.60 |
| Novato | 10.62 | 4.81 |
| Menlo Park | 8.64 | 4.09 |
| Atherton | 8.81 | 4.14 |

$\Delta$ House Price $=7.28 *$ Tax Saving + Home Attributes $\beta$ (2.45)

## Impact of Corporate Tax Reform

(D. Cutler AER 1988)

Tax Reform Act of 1986 (TRA86) Generates Differential Benefits for Different Firms

Event Study Methodology: Return on Security i at time t :

$$
\mathrm{R}_{\mathrm{it}}=\alpha_{\mathrm{i}}+\beta_{\mathrm{i}} * \mathrm{R}_{\mathrm{M}, \mathrm{t}}+\varepsilon_{\mathrm{it}} \text { (CAPM - could do multi-factor) }
$$

ADD: Variable capturing news of policy change. Let $\mathrm{I}_{\mathrm{t}}$ denote indicator variable for days on which the
probability of tax reform rises. Let \%Equip denote share of firm's capital stock that is equipment. Prediction: firms with more equipment (ITC was eliminated) should experience higher returns $b / c$ their competition will have to pay more for equipment.

Estimate:

$$
\mathrm{R}_{\mathrm{it}}=\alpha_{\mathrm{i}}+\beta_{\mathrm{i}} * \mathrm{R}_{\mathrm{M}, \mathrm{t}}+\lambda \text { EQUIP }^{2}{ }_{\mathrm{i}} * \mathrm{I}_{\mathrm{t}}+\varepsilon_{\mathrm{it}}
$$

$\lambda$ measures change in value -- but calibration requires an estimate of change in PROBABILITY of law passage over all $I_{t}$.

|  | $\lambda$ without industry <br> effects | $\lambda$ with industry <br> effects |
| :--- | :--- | :--- |
| One Day Window | 0.018 | 0.000 |
|  | $(0.012)$ | $(.015)$ |
| 10-Day Window | 0.083 | 0.035 |
|  | $(0.025)$ | $(0.031)$ |
| 30-Day Window | 0.064 | 0.024 |
|  | $(0.043)$ | $(0.051)$ |

Predicted effect from simulation models: 0.07 . Why are coefficients so much smaller?

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