Pareto Efficient Income Taxation

Iván Werning

MIT

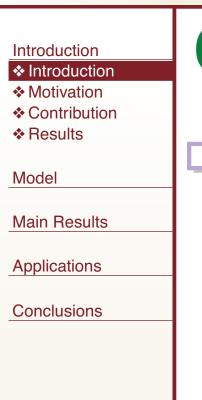
April 2007

NBER Public Economics meeting

Introduction

Introduction Introduction Motivation Contribution Results 	Q: Good shape for tax schedule ?
Model	
Main Results	
Applications	
Conclusions	

Introduction

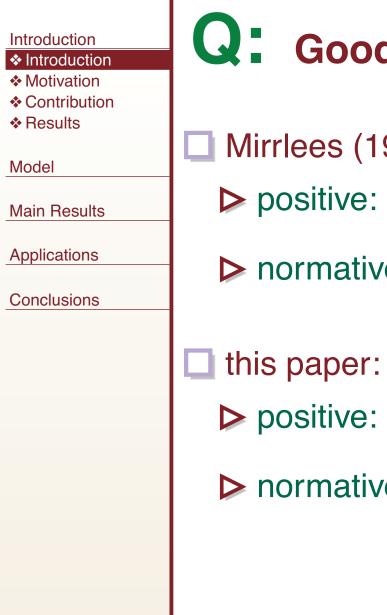


Q: Good shape for tax schedule **?**

Mirrlees (1971), Diamond (1998), Saez (2001)▶ positive: redistribution vs. efficiency

normative: Utilitarian social welfare function

Introduction



Q: Good shape for tax schedule **?**

Mirrlees (1971), Diamond (1998), Saez (2001)▶ positive: redistribution vs. efficiency

normative: Utilitarian social welfare function

this paper: Pareto efficient taxation
 positive: redistribution vs. efficiency

normative: Utilitarian social welfare function Pareto Efficiency

Old Motivation: "New New New..."

Introduction
Introduction
Motivation
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Results
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Model
Model Main Results

Conclusions

Why not Utilitarian? ($\sum_i U^i$)

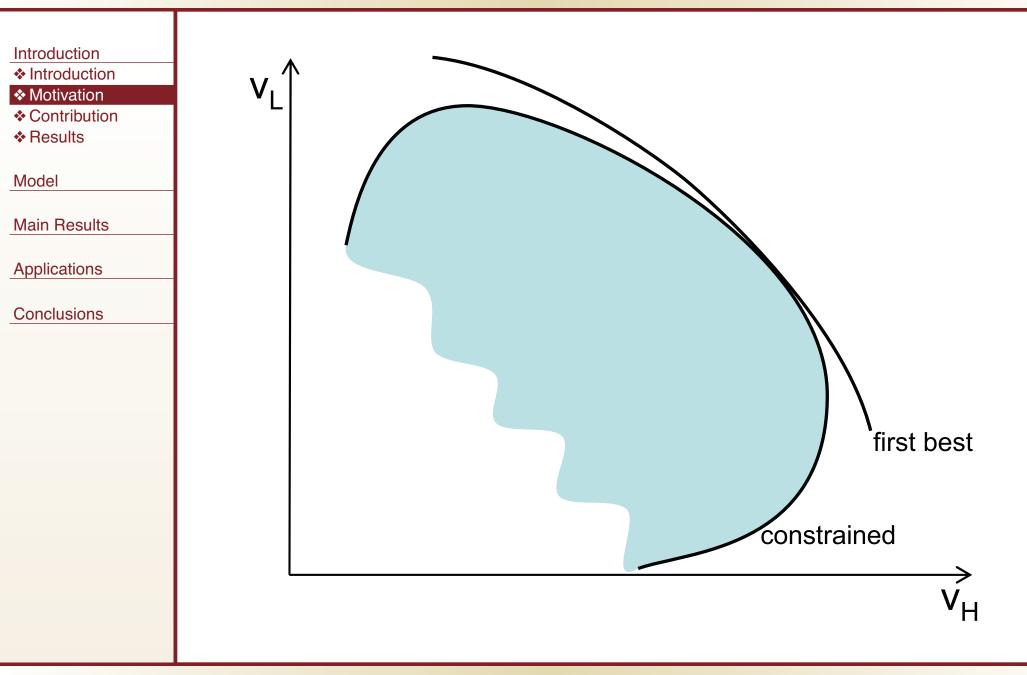
▷ practical: cardinality $U^i \to W(U^i)$ (or even $W^i(U^i)$) ... which Utilitarian?

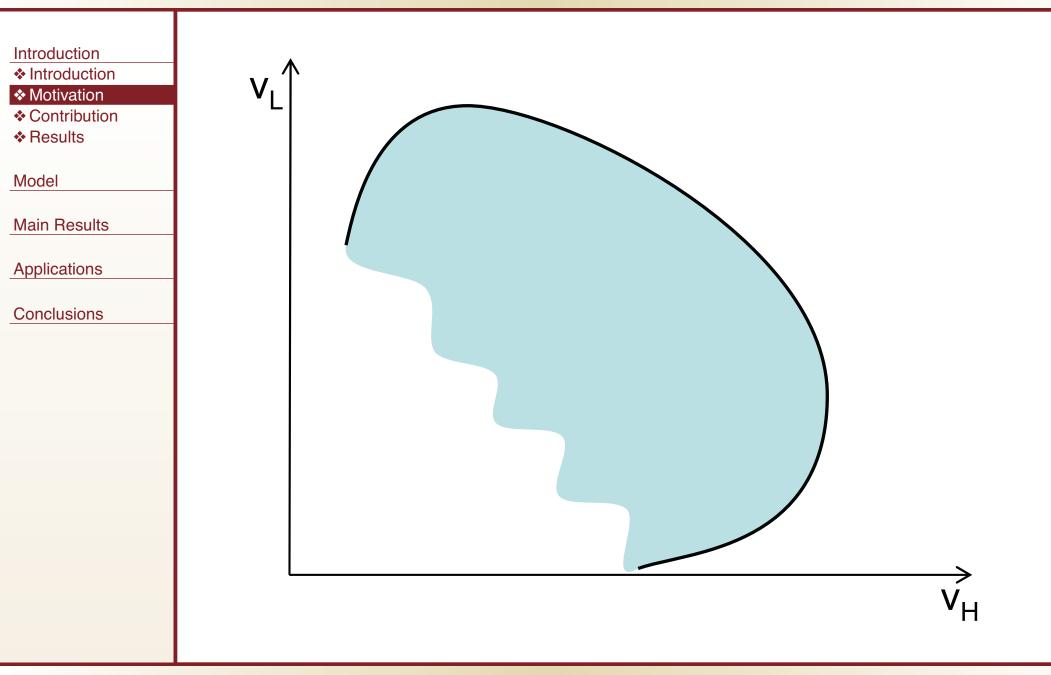
▷ conceptual: political process: social classes → Coasian bargain ...but $\max \sum U^i$?

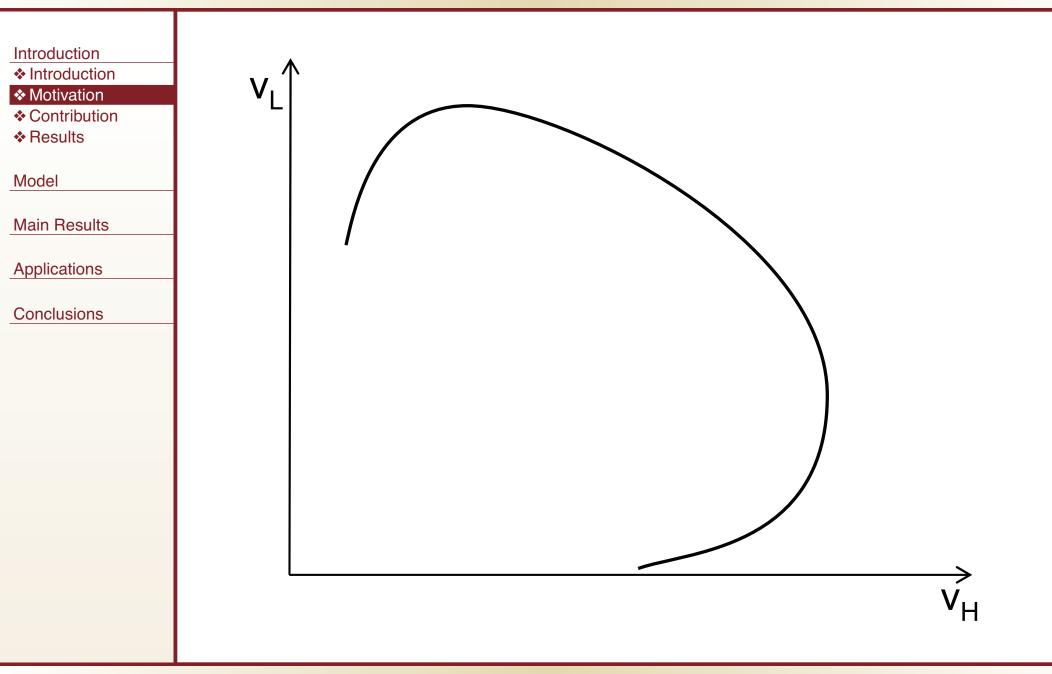
philosophical: other notions of fairness and social justice

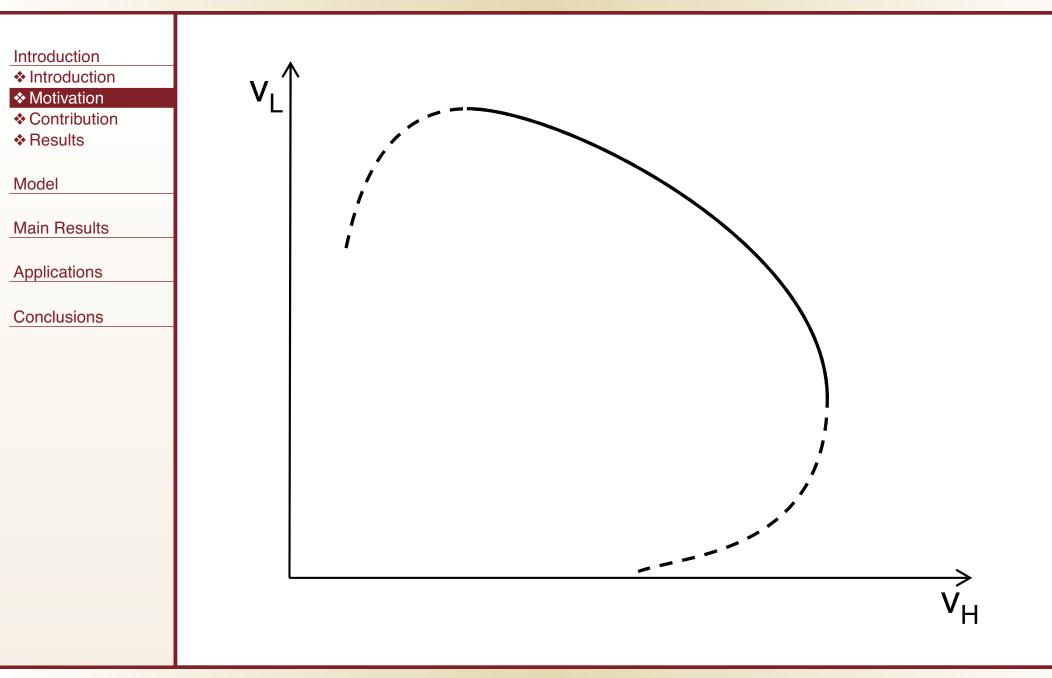
Old Motivation: "New New New..."

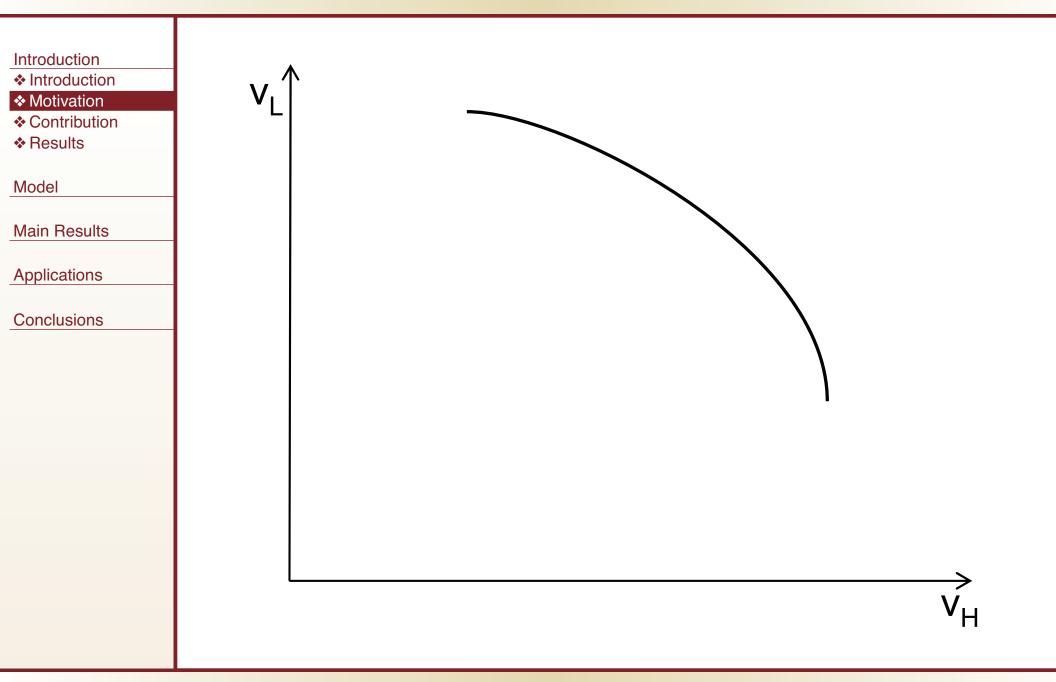
Introduction Introduction Motivation Contribution Results Model Main Results Applications Conclusions 	 Why not Utilitarian? (∑_i Uⁱ) ▶ practical: cardinality Uⁱ → W(Uⁱ) (or even Wⁱ(Uⁱ)) which Utilitarian? ▶ conceptual: political process: social classes → Coasian bargain but max ∑ Uⁱ ? ▶ philosophical: other notions of fairness and social justice
	Pareto efficiency

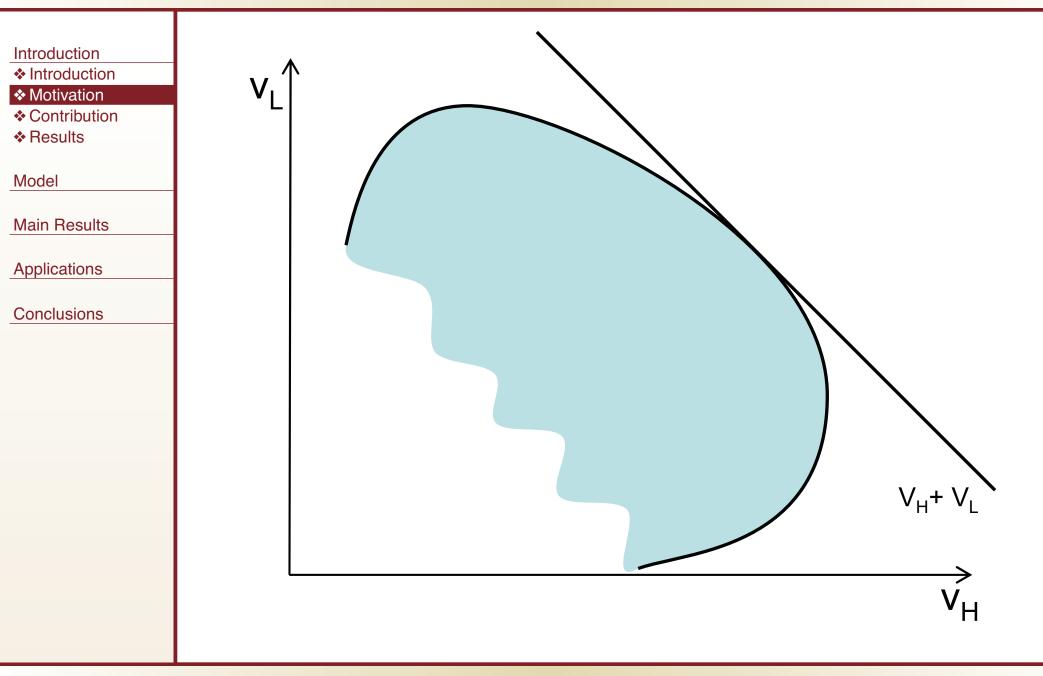


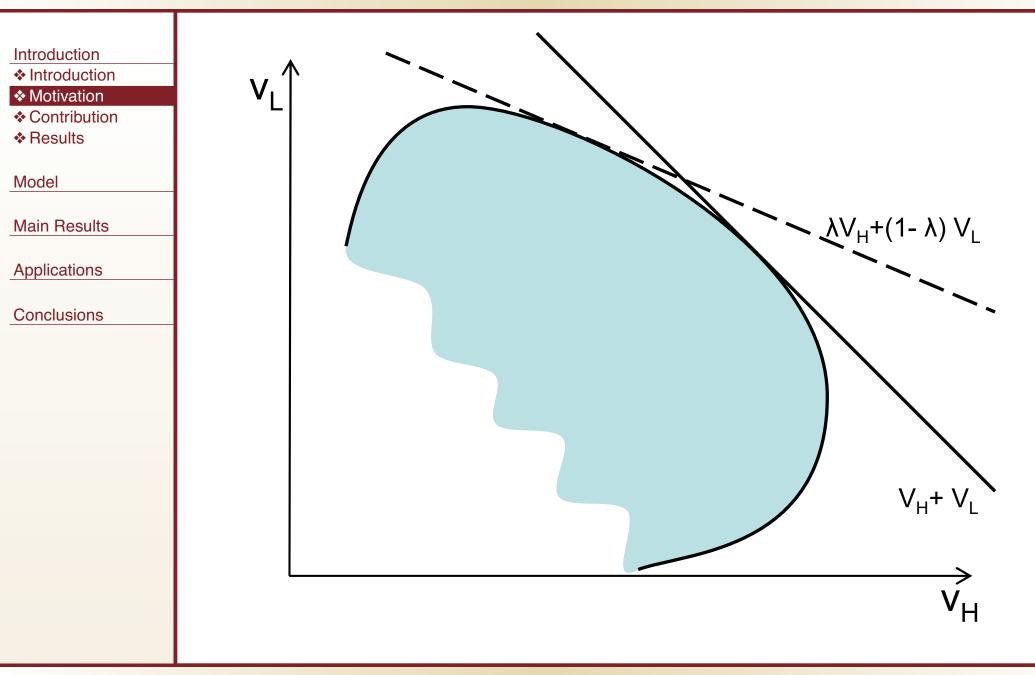












Contribution

Introduction Introduction Motivation Contribution Results	 invert Mirrlees model express in tractable way
Model	use it: some applications
Main Results	
Applications	
Conclusions	

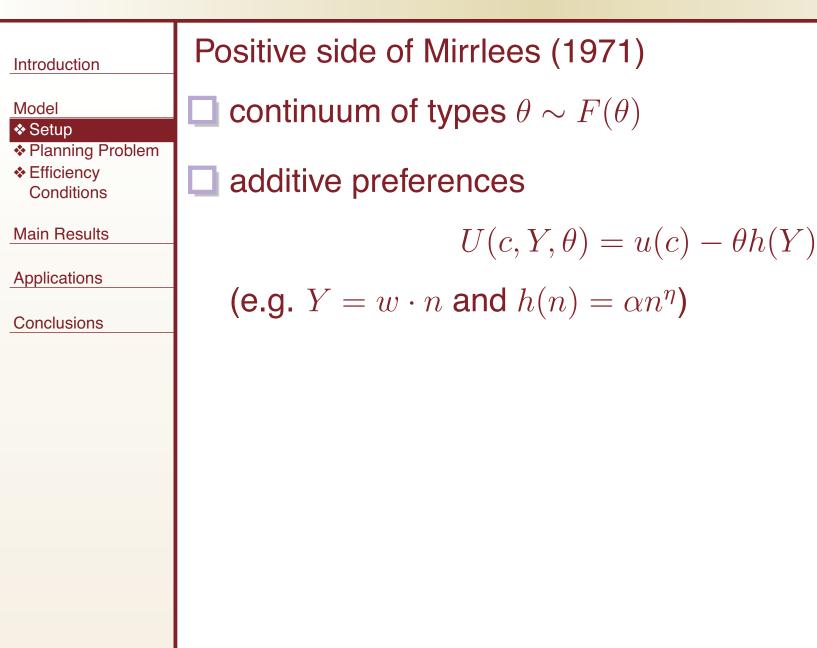
Results

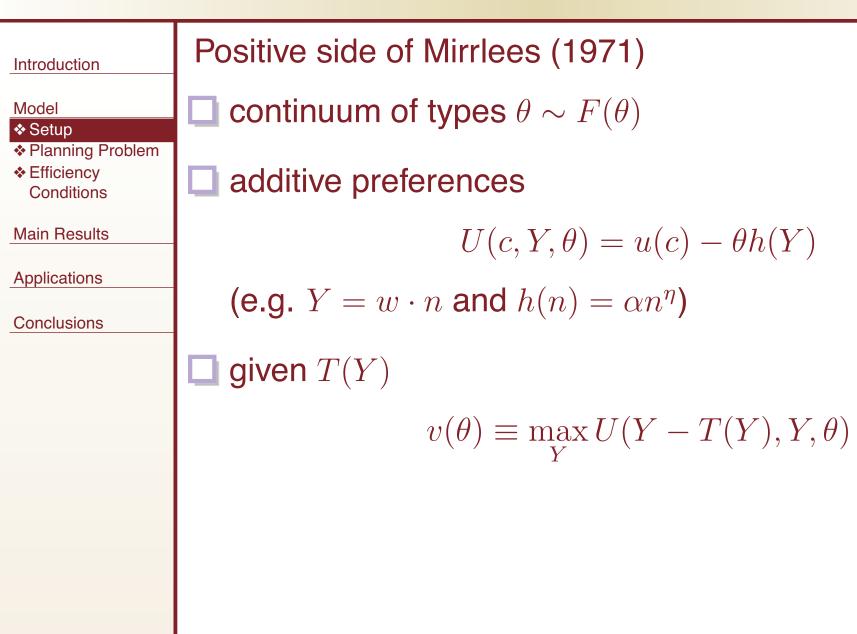
Introduction Introduction Motivation Contribution Results	 #0 restrictions generalize "zero-tax-at-the-top" #1 Any T(Y) ▷ efficient for many f(θ)
Model Main Results	logithmic inefficient for many $f(\theta)$ anything goes
Applications Conclusions	#2 Given $T_0(Y) \longrightarrow g(Y) \longrightarrow f(\theta)$ (Saez, 2001) \triangleright efficient set of $T(Y)$: large
	\blacktriangleright inefficient set of $T(Y)$: large
	#3 Simple test for efficiency of $T_0(Y)$

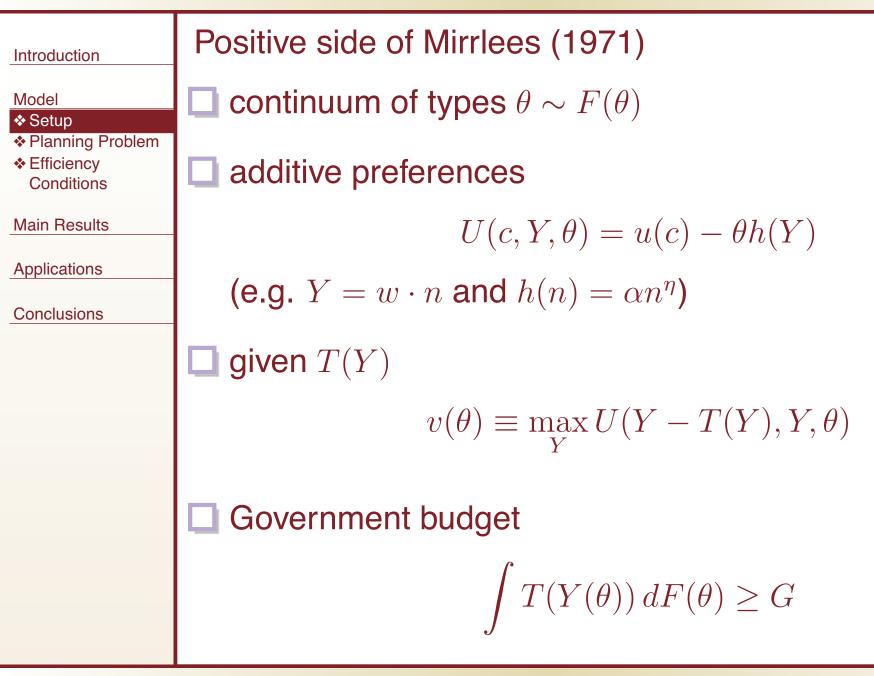
Results

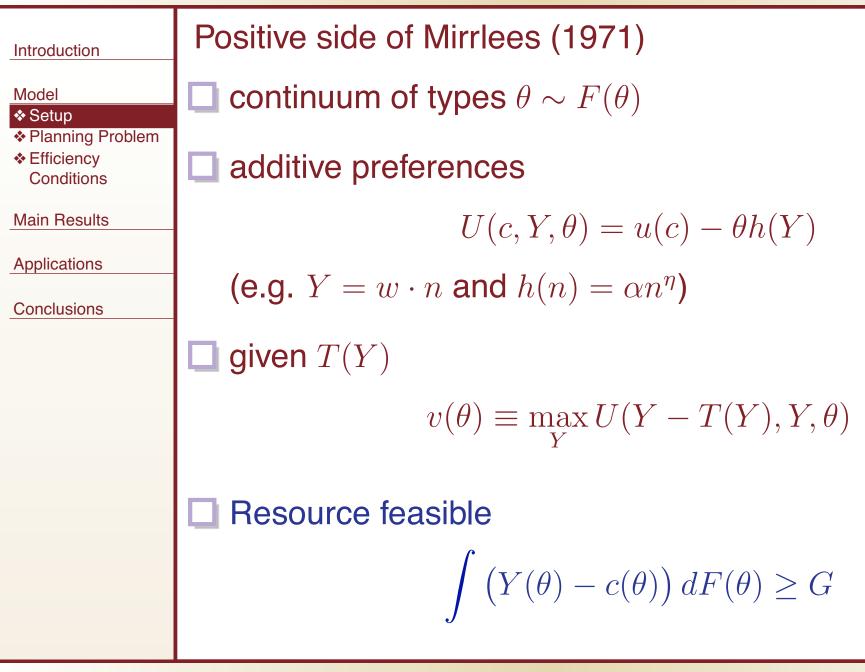
Introduction Introduction Motivation Contribution Results 	 #4 Simple formulas bound on top tax rate
Model	efficiency of a flat tax
Main Results	#5 Increasing progressivity
Applications	maintains Pareto efficiency
Conclusions	#6 observable heterogeneity not conditioning can be efficient

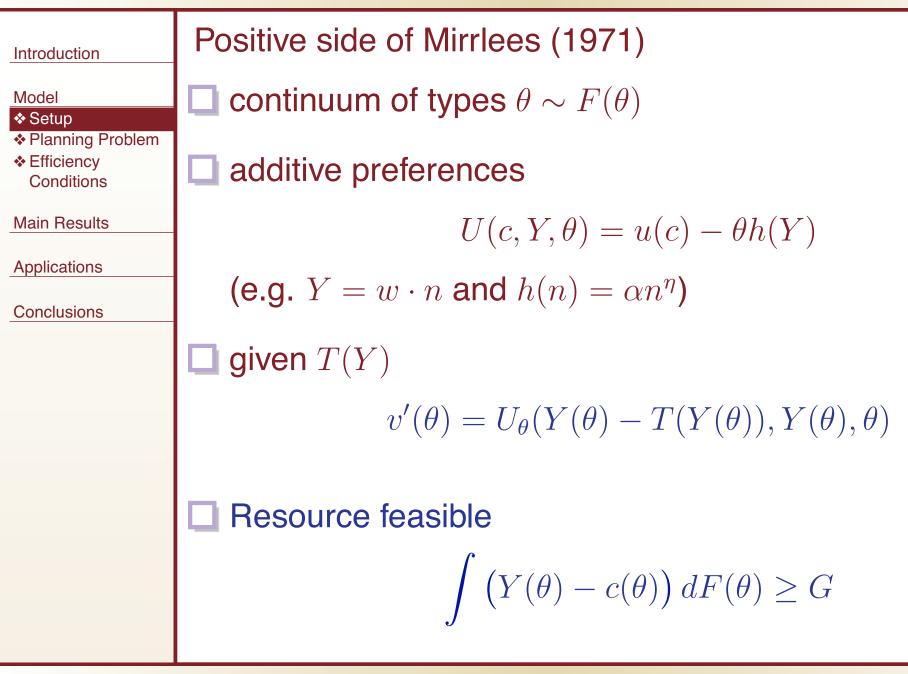
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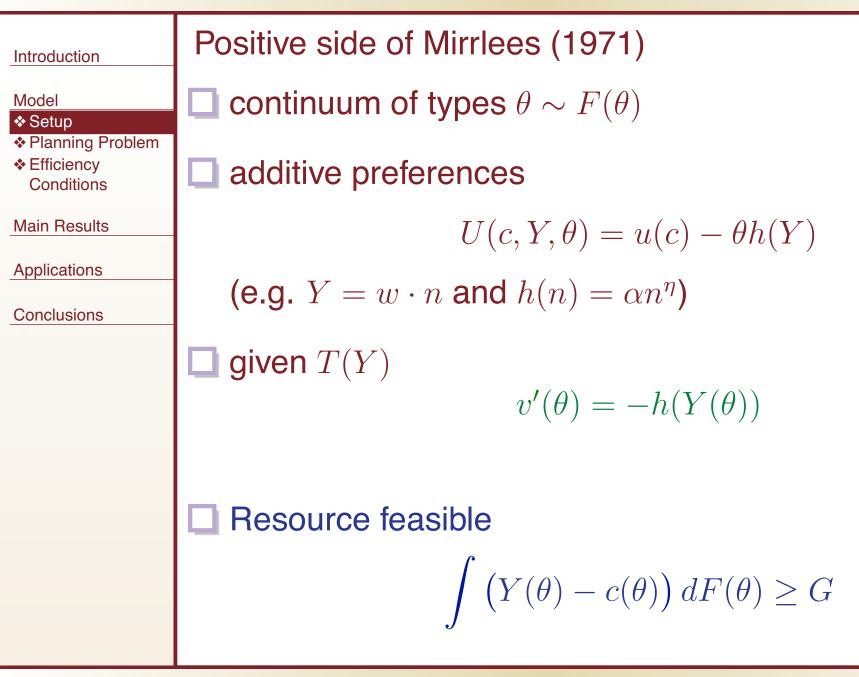


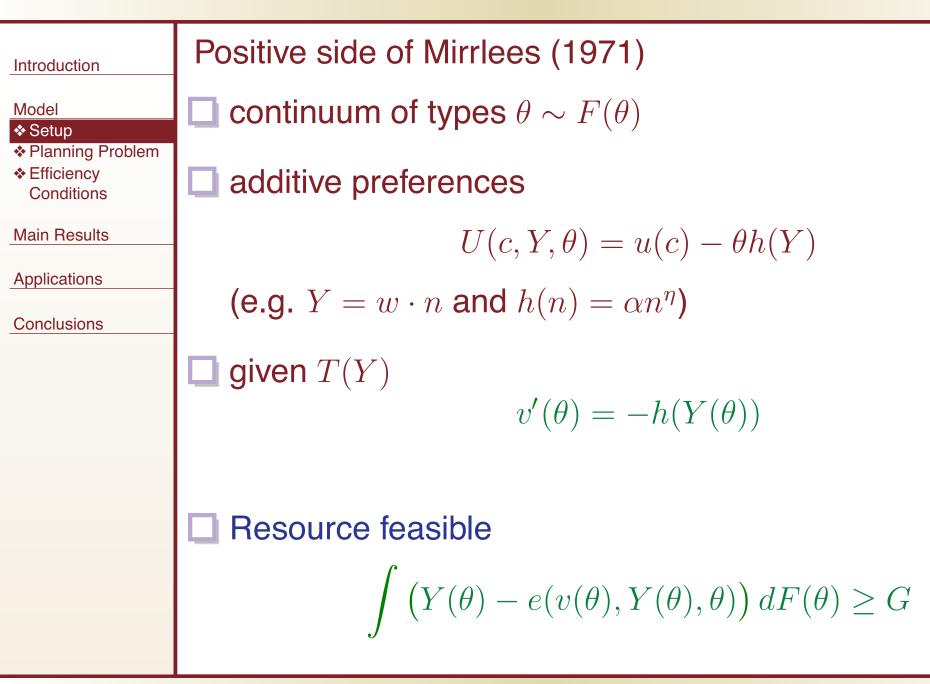












Introduction Model	Dual Pareto Problem
 Setup Planning Problem Efficiency Conditions 	maximize net resources
Main Results Applications Conclusions	subject to, $\tilde{v}(\theta) \geq v(\theta)$ incentives

Introduction Model	Dual Pareto Problem	
 Setup Planning Problem Efficiency Conditions 	$\max_{\tilde{Y},\tilde{v}} \int \left(\tilde{Y}(\theta) - e(\tilde{v}(\theta), \tilde{Y}(\theta), \theta) \right) dF(\theta)$	
Main Results	subject to,	
Applications	$\tilde{v}(\theta) \ge v(\theta)$	
Conclusions		
	incentives	

Introduction	D	ual Pare
Model		
Setup		
Planning Problem		
 Efficiency Conditions 		
Main Results		subject
Applications		
Conclusions		

$$\max_{\tilde{Y},\tilde{v}} \int \left(\tilde{Y}(\theta) - e(\tilde{v}(\theta), \tilde{Y}(\theta), \theta) \right) dF(\theta)$$

t to,

 $\tilde{v}(\theta) \ge v(\theta)$

$$\tilde{v}'(\theta) = -h(\tilde{Y}(\theta))$$

Introduction	D	ual Pareto Problem
Model		
 Setup Planning Problem 		
 Efficiency Conditions 		$\max_{\tilde{Y},\tilde{v}} \int \Big(\tilde{Y}$
Main Results		subject to,
Applications		
Conclusions		
		$ ilde{Y}$

$$\max_{\tilde{Y},\tilde{v}} \int \left(\tilde{Y}(\theta) - e(\tilde{v}(\theta), \tilde{Y}(\theta), \theta) \right) dF(\theta)$$

ect to,
$$\tilde{v}(\theta) \ge v(\theta)$$
$$\tilde{v}'(\theta) = -h(\tilde{Y}(\theta))$$
$$\tilde{Y}(\theta) \text{ nonincreasing}$$

Introduction

Lagrangian

Model

Setup

Planning Problem

Efficiency Conditions

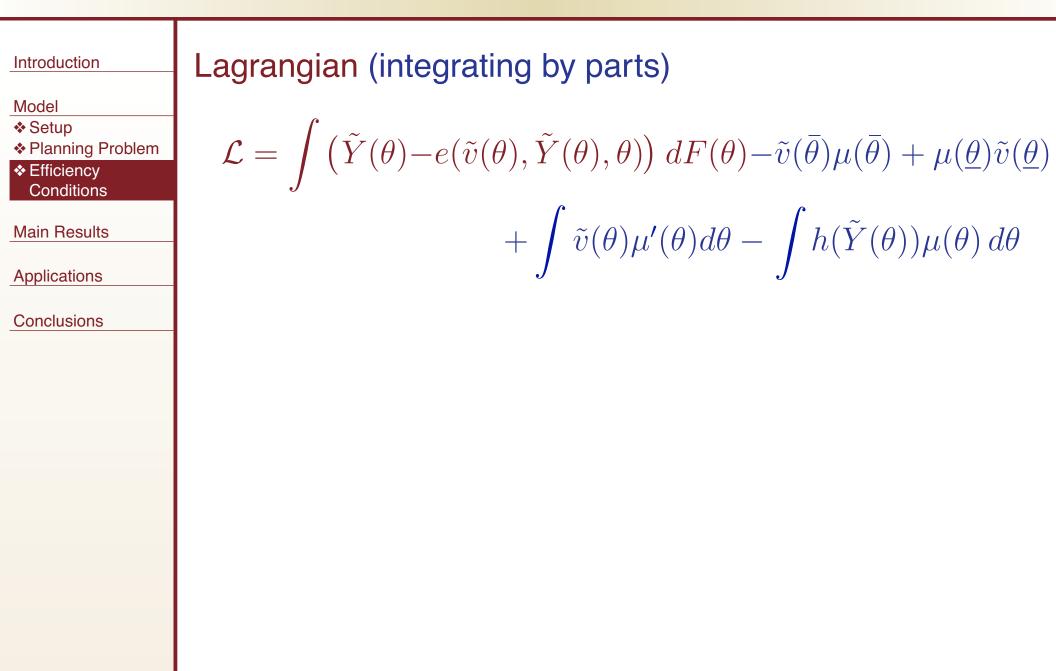
Main Results

Applications

Conclusions

 $\mathcal{L} = \int \left(\tilde{Y}(\theta) - e(\tilde{v}(\theta), \tilde{Y}(\theta), \theta) \right) dF(\theta)$

$$-\int \left(\tilde{v}'(\theta) + h(\tilde{Y}(\theta))\right) \mu(\theta) \, d\theta$$



Introduction

Model

Setup

Planning Problem

Efficiency
 Conditions

Main Results

Applications

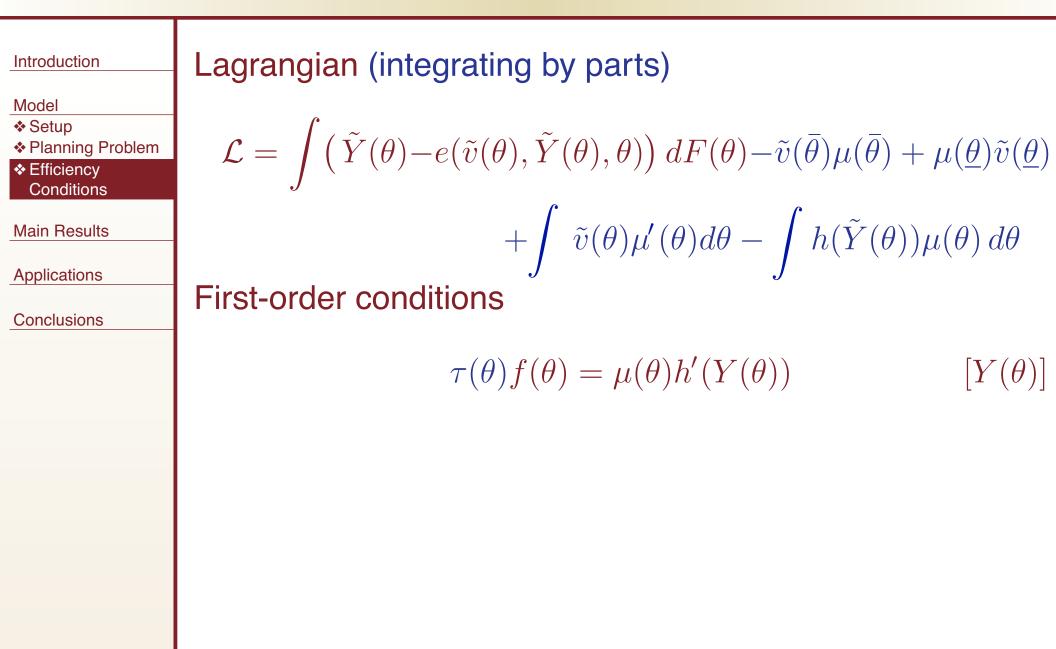
Conclusions

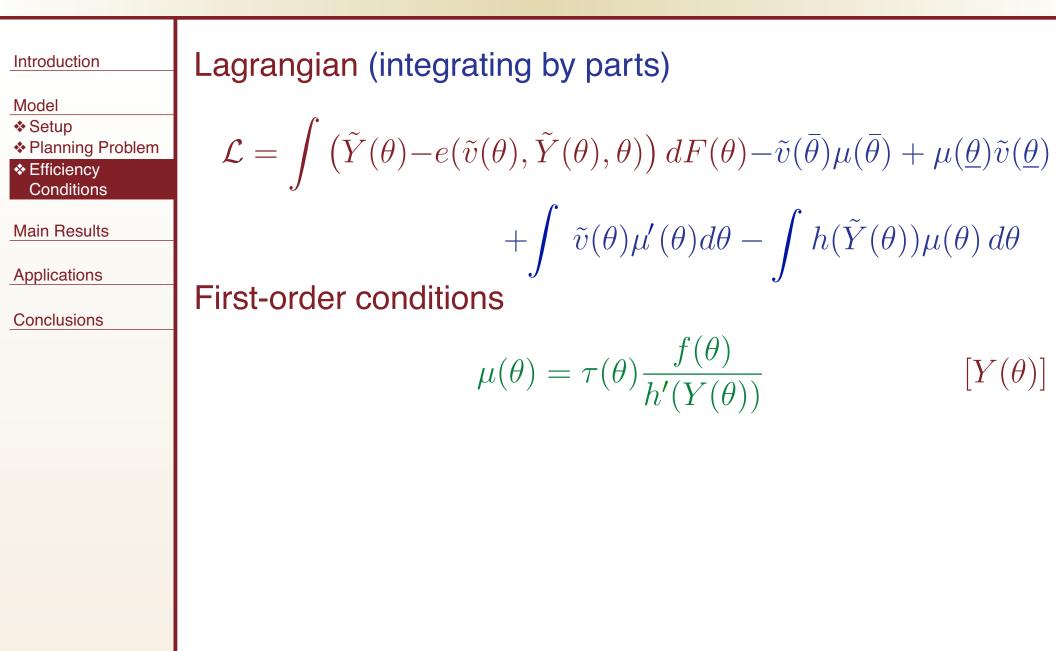
Lagrangian (integrating by parts)

$$\mathcal{L} = \int \left(\tilde{Y}(\theta) - e(\tilde{v}(\theta), \tilde{Y}(\theta), \theta) \right) dF(\theta) - \tilde{v}(\bar{\theta})\mu(\bar{\theta}) + \mu(\underline{\theta})\tilde{v}(\underline{\theta}) + \int \tilde{v}(\theta)\mu'(\theta)d\theta - \int h(\tilde{Y}(\theta))\mu(\theta)d\theta$$

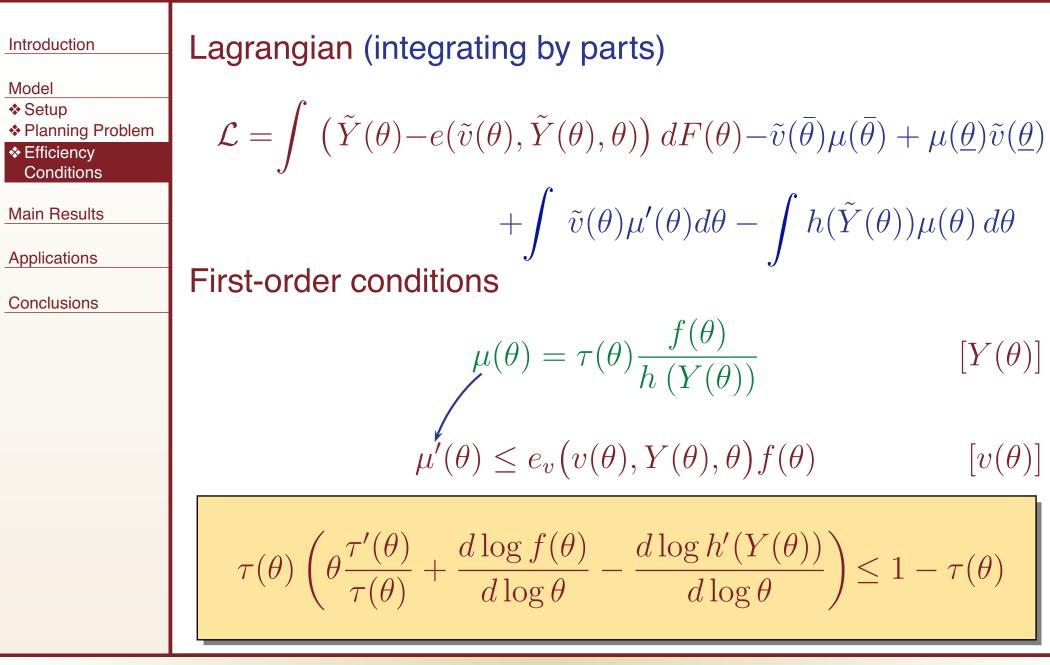
First-order conditions

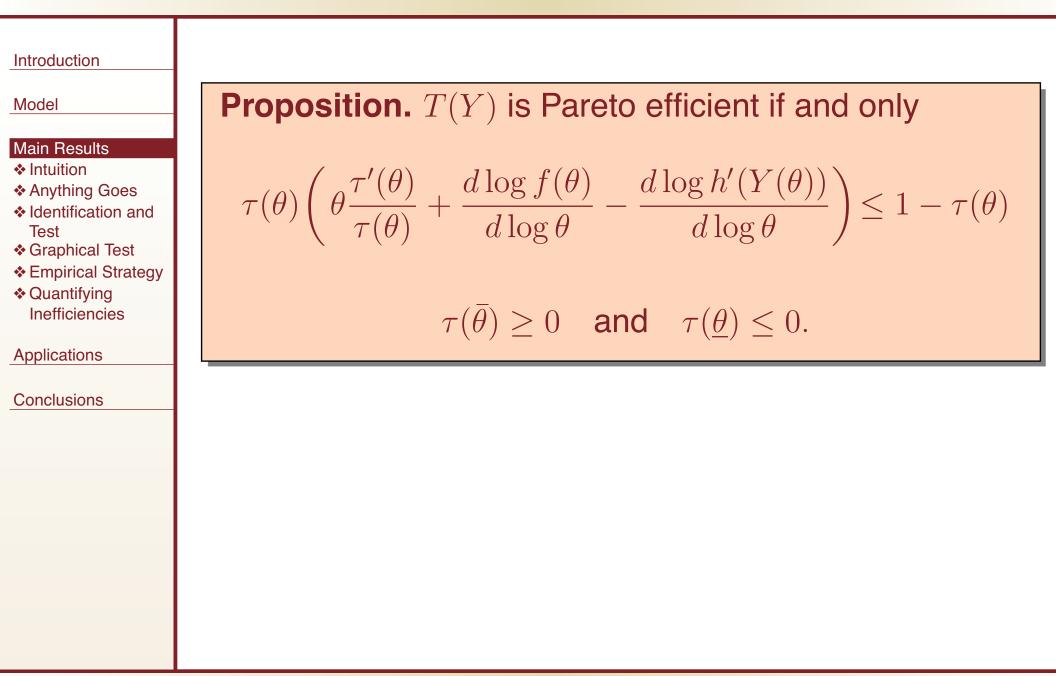
$$(1 - e_Y(v(\theta), Y(\theta), \theta)) f(\theta) = \mu(\theta) h'(Y(\theta))$$
 [Y(\theta)]

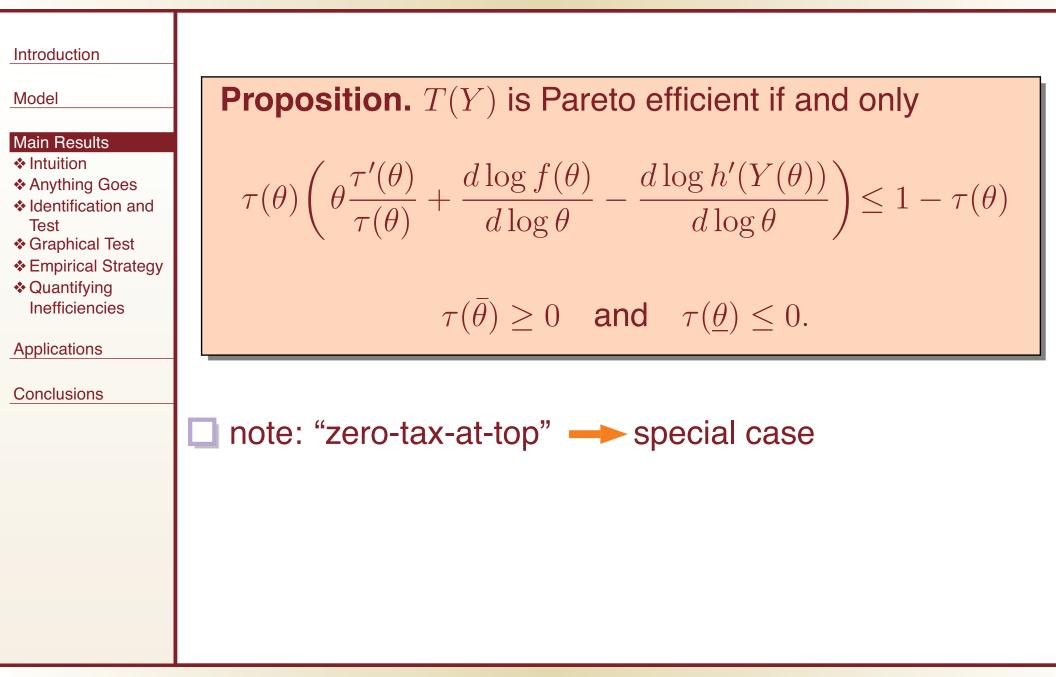




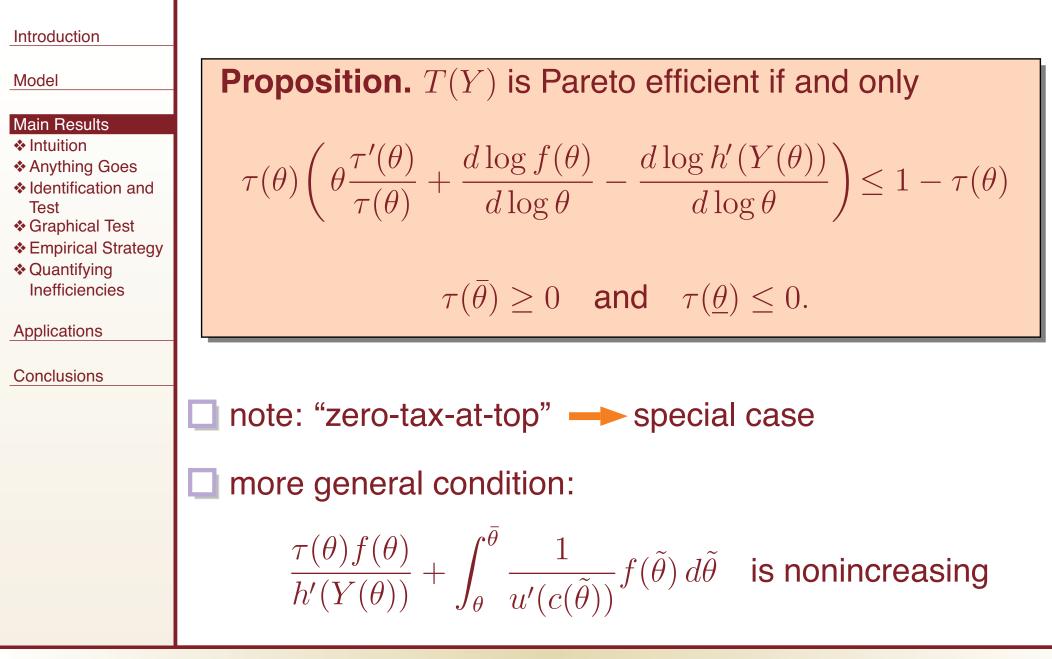
	Lagrangian (integrating by parts)
Model Setup Planning Problem Efficiency Conditions	$\mathcal{L} = \int \left(\tilde{Y}(\theta) - e(\tilde{v}(\theta), \tilde{Y}(\theta), \theta) \right) dF(\theta) - \tilde{v}(\bar{\theta})\mu(\bar{\theta}) + \mu(\underline{\theta})\tilde{v}(\underline{\theta}) + \mu(\underline{\theta})\tilde$
Main Results Applications	$+\int \tilde{v}(\theta)\mu'(\theta)d\theta - \int h(\tilde{Y}(\theta))\mu(\theta)d\theta$ First order conditions
Conclusions	First-order conditions $f(\rho)$
	$\mu(\theta) = \tau(\theta) \frac{f(\theta)}{h'(Y(\theta))} \qquad [Y(\theta)]$
	$\mu'(\theta) \le e_v(v(\theta), Y(\theta), \theta) f(\theta) \qquad [v(\theta)$



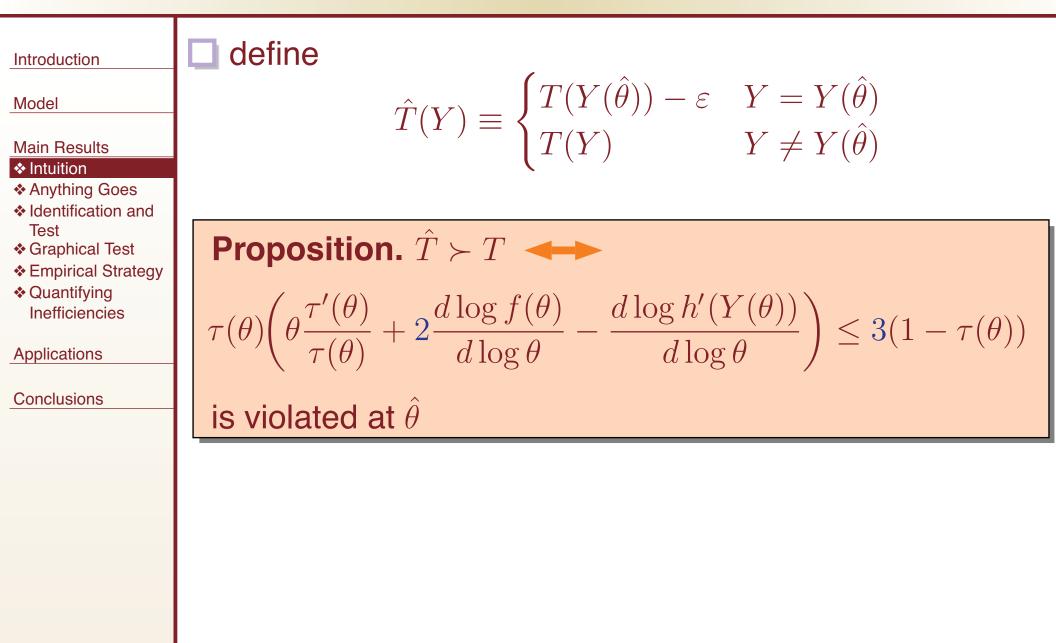


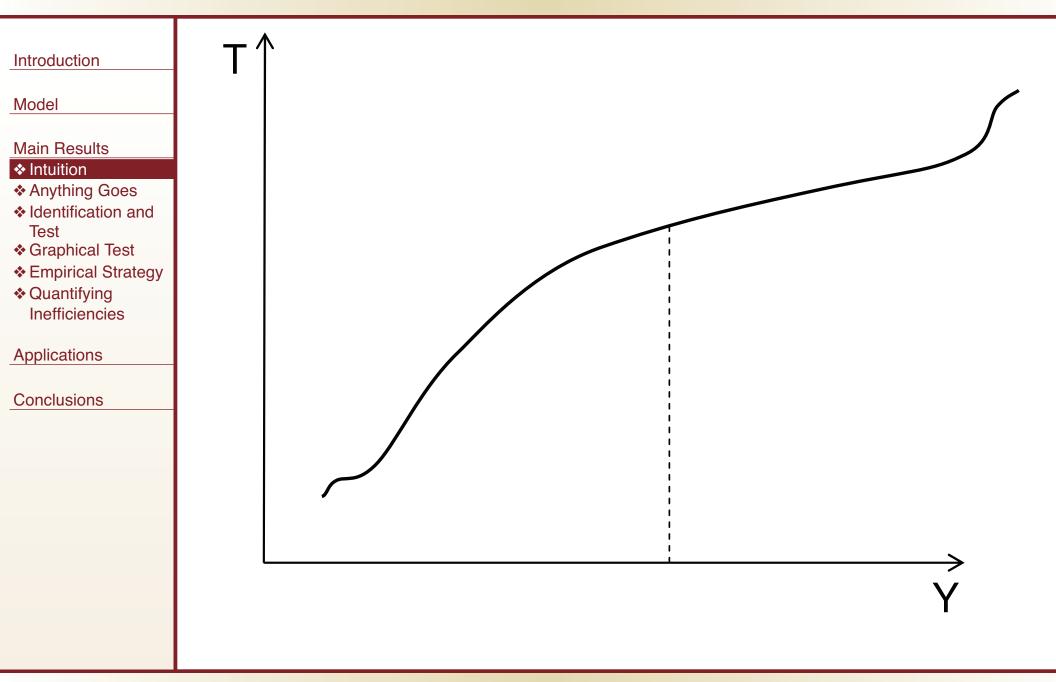


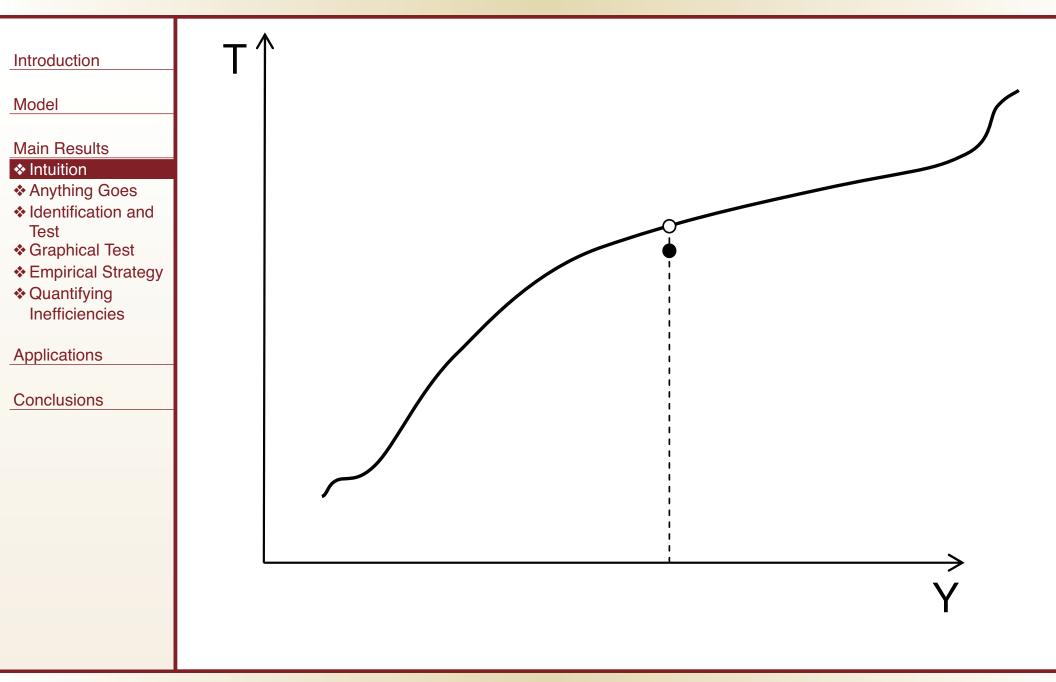
Efficiency Conditions

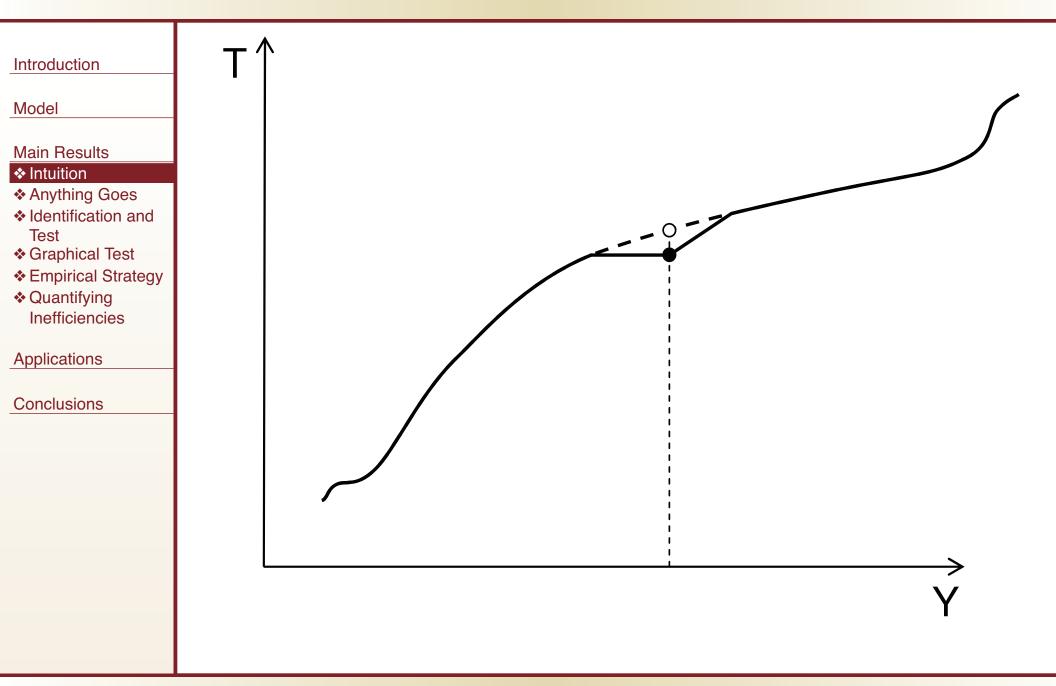


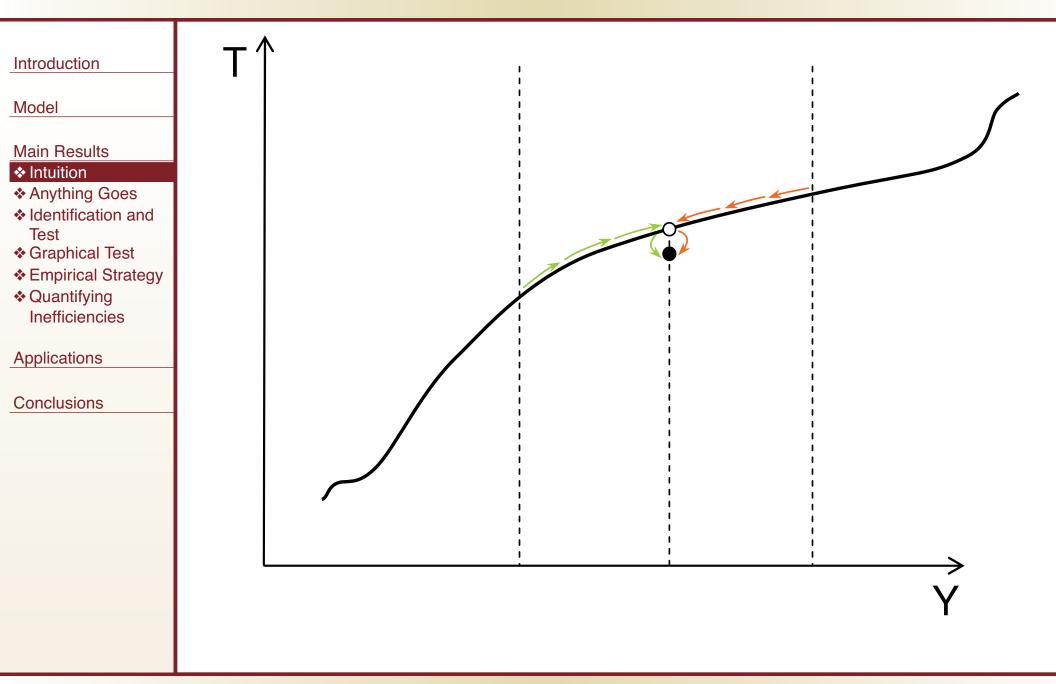
Intuition

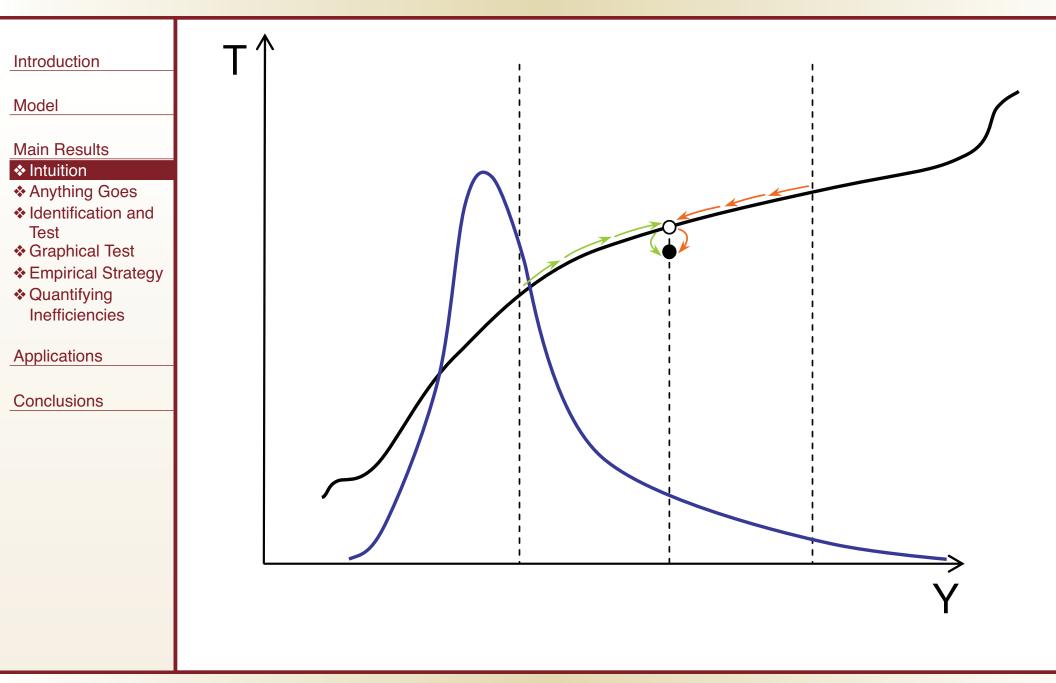


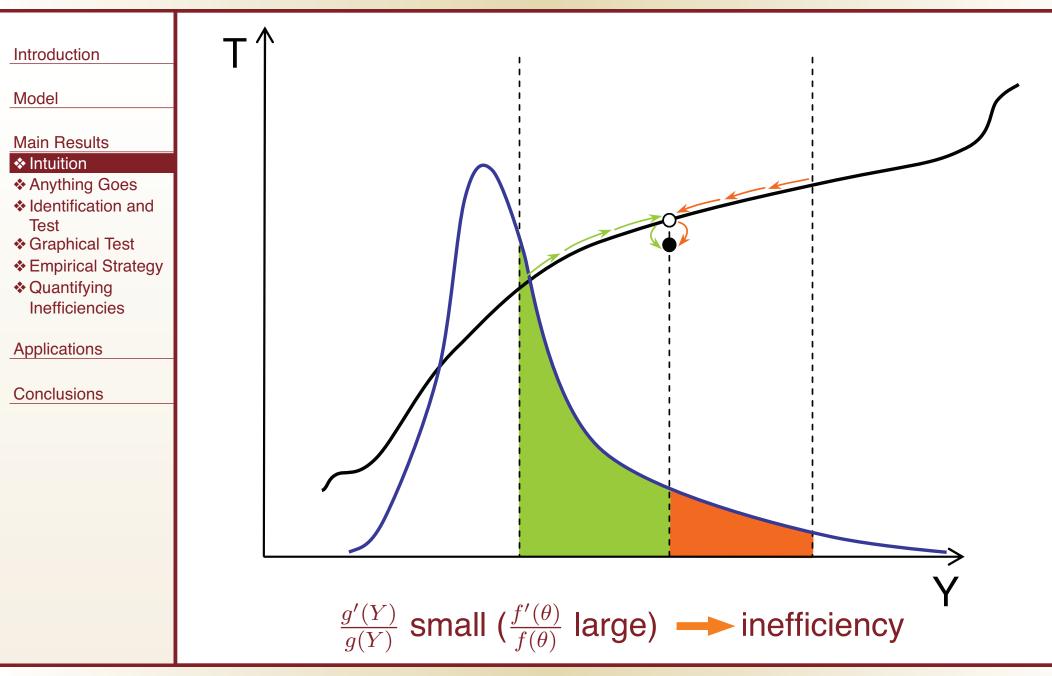








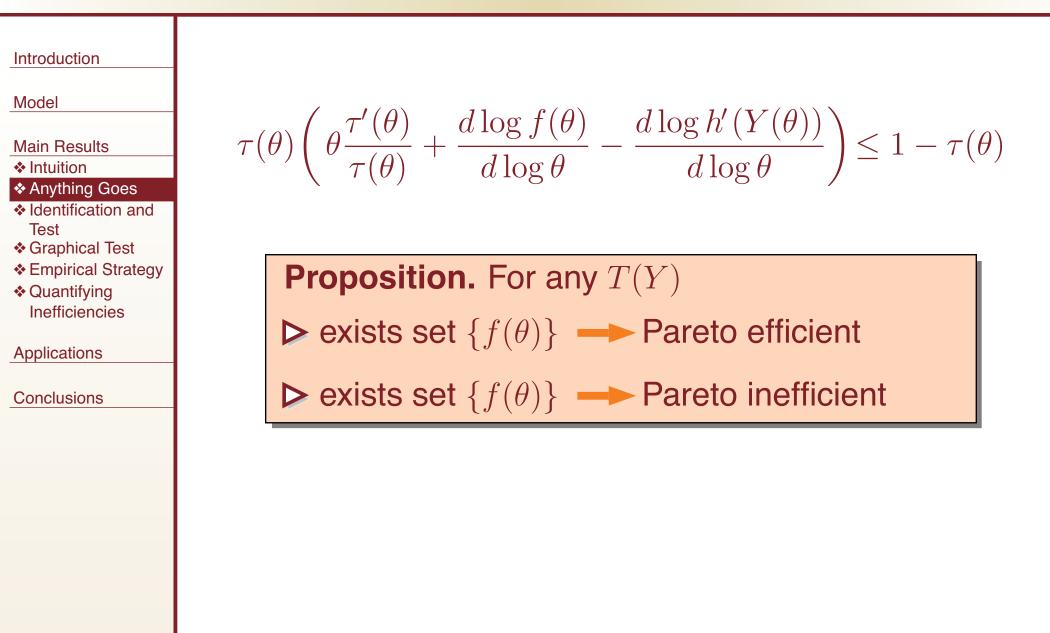




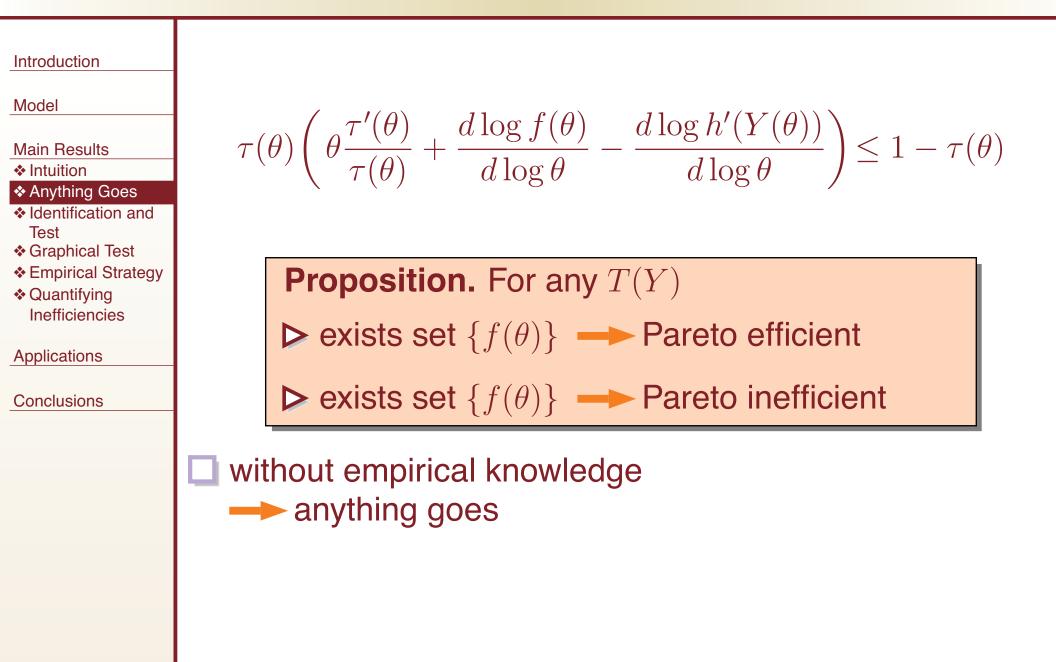
Laffer

Introduction	Iower taxes — increase revenue
Model	Pareto improvements
Main Results Intuition Anything Goes 	
 Identification and Test Graphical Test Empirical Strategy 	Proposition. $T_1(Y) \succ T_0(Y) \longrightarrow T_1(Y) \leq T_0(Y)$
 Quantifying Inefficiencies 	
Applications	
Conclusions	

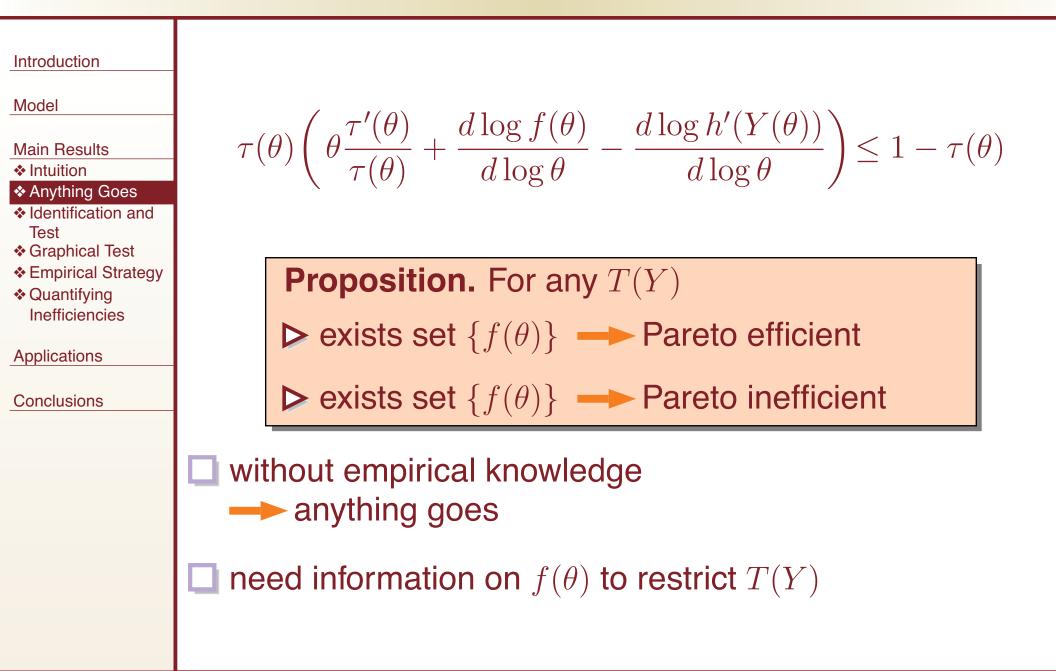
Anything Goes



Anything Goes



Anything Goes



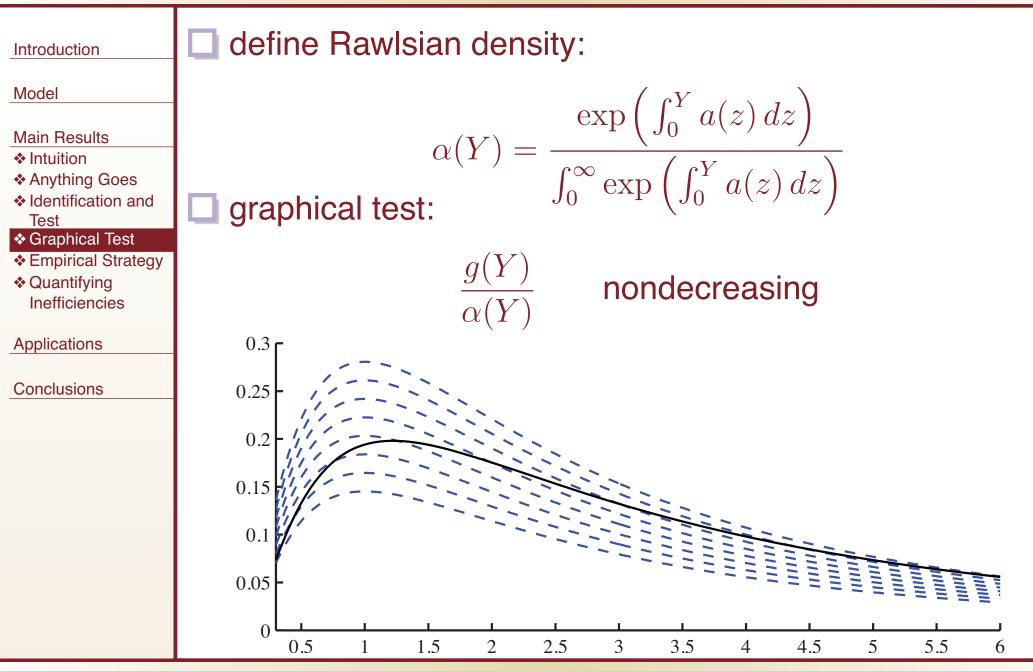
Identification and Test

Introduction	\Box observe $g(Y)$ identify (Saez, 2001)
Model Main Results Intuition Anything Goes Identification and Test Graphical Test Comprised Strategy Quantifying	$\theta(Y) = (1 - T'(Y)) \frac{u'(Y - T(Y))}{h'(Y)}$ $ f(\theta(Y)) = \frac{g(Y)}{\theta'(Y)}$
Inefficiencies Applications Conclusions	

Identification and Test

Introduction Model Main Results * Intuition * Anything Goes * Identification and Test * Graphical Test * Graphical Test * Empirical Strategy * Quantifying Inefficiencies Applications Conclusions	 observe g(Y) identify (Saez, 2001) θ(Y) = (1 − T'(Y)) $\frac{u'(Y − T(Y))}{h(Y)}$ → f(θ(Y)) = $\frac{g(Y)}{\theta'(Y)}$ efficiency test $\frac{d \log g(Y)}{d \log Y} \ge a(Y)$
	$d\log Y$ – ()
	for tax schedule in place

Graphical Test



Introduction

Model

- Main Results
- Intuition
- Anything Goes
- Identification and Test
- Graphical Test
- Empirical Strategy
- Quantifying Inefficiencies

Applications

Conclusions

needed

- **1.** current tax function T(Y)
- **2.** distribution of income g(Y)
- **3.** utility function $U(c, Y, \theta)$

Introduction

Model

Main Results

Intuition

- Anything Goes
- Identification and Test
- Graphical Test
- Empirical Strategy
- Quantifying Inefficiencies

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Applications
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Conclusions

needed

- **1.** current tax function T(Y)
- **2.** distribution of income g(Y)
- **3.** utility function $U(c, Y, \theta)$

in principle: #1 and #2 ---- easy #3 usual deal

Introduction	🔲 needed
Model	1. current tax function $T(Y)$
Main Results Intuition Anything Goes Identification and 	2. distribution of income $g(Y)$ 3. utility function $U(c, Y, \theta)$
Test Graphical Test Empirical Strategy Quantifying Inefficiencies	in principle: #1 and #2 easy #3 usual deal
Applications	Diamond (1998) and Saez (2001)
Conclusions	

Introduction	needed
Model	1. current tax function $T(Y)$
Main Results	2. distribution of income $g(Y)$
 Intuition Anything Goes 	3. utility function $U(c, Y, \theta)$
 Identification and Test 	
 Graphical Test Empirical Strategy 	\Box in principle: #1 and #2 \longrightarrow easy
 Quantifying Inefficiencies 	#3 usual deal
Applications	Diamond (1998) and Saez (2001)
Conclusions	
	some challenges
	1. econometric: need to estimate $g'(Y)$ and $g(Y)$
	2. conceptual: static model
	\longrightarrow lifetime $T(Y)$ and $g(Y)$ (Fullerton and Rogers)

Т

Output Density

Introduction Model	□ IRS's SOI Public Use Files for Individual tax returns ▶ lifetime $g(Y)$?
Main Results Intuition Anything Goes Identification and Test Graphical Test Empirical Strategy 	▶ lifetime $T(Y)$ schedule? ↓ $Y^i = \frac{1}{n} \sum Y_t^i$
 Quantifying Inefficiencies Applications 	Smooth density estimate assumed $T(Y) = .30 \times Y$
Conclusions	

Introduction

Model

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Main Results
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Intuition

- Anything Goes
- Identification and Test
- Graphical Test
- Empirical Strategy
- Quantifying Inefficiencies

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Applications
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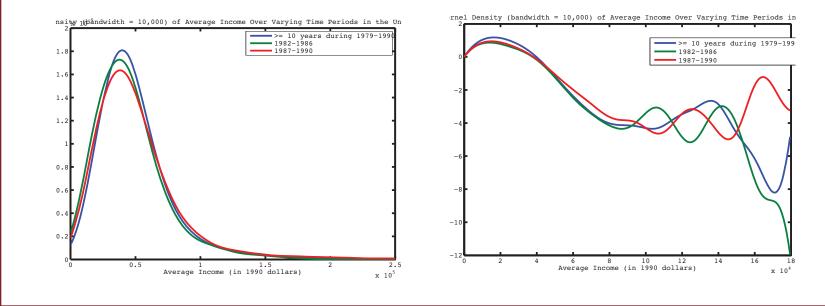
Conclusions

IRS's SOI Public Use Files for Individual tax returns lifetime g(Y)?

 \triangleright lifetime T(Y) schedule?

 $\square Y^i = \frac{1}{n} \sum Y_t^i$

smooth density estimate assumed $T(Y) = .30 \times Y$



2:

Implied

elasticity¹⁹

Pareto Efficient Income Taxati Pigure 1: Density of income Figure $\frac{Yg'(Y)}{Yg'(Y)}$

Output Density

Introduction Model	□ IRS's SOI Public Use Files for Individual tax returns ▶ lifetime $g(Y)$?
Main Results	lifetime $T(Y)$ schedule?
 Anything Goes Identification and Test Graphical Test Empirical Strategy 	$\square Y^i = \frac{1}{n} \sum Y_t^i$
 Quantifying Inefficiencies 	smooth density estimate
Applications	assumed $T(Y) = .30 \times Y$
Conclusions	Relight Test against 1987–1990 Average Income Data (sigma = 0, eta = 2, T = .3 $\int_{0}^{0} \int_{0}^{0} \int_{0$

Quantifying Inefficiencies

☐ □ efficiency test → qualitative

] quantitative...

Introduction

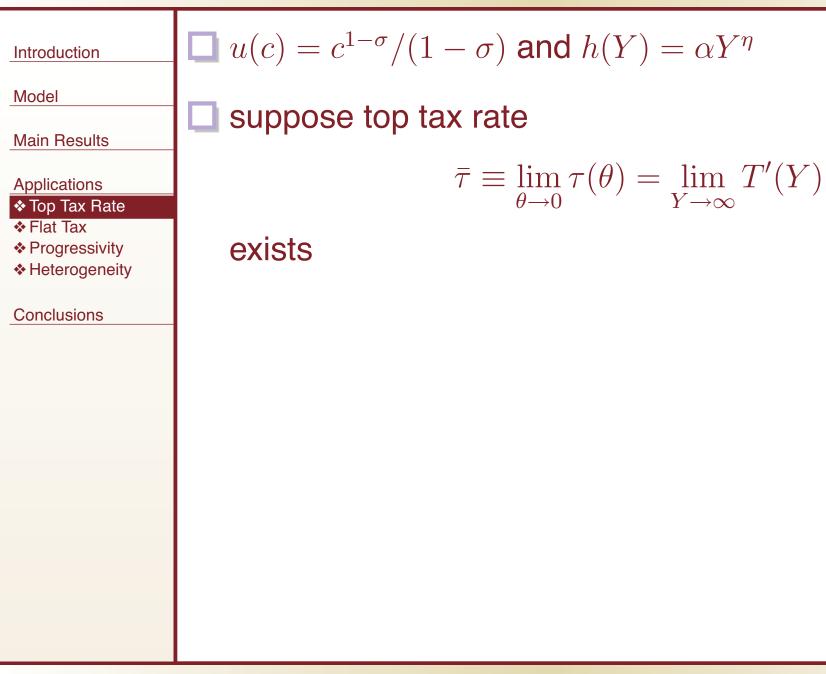
Main Results

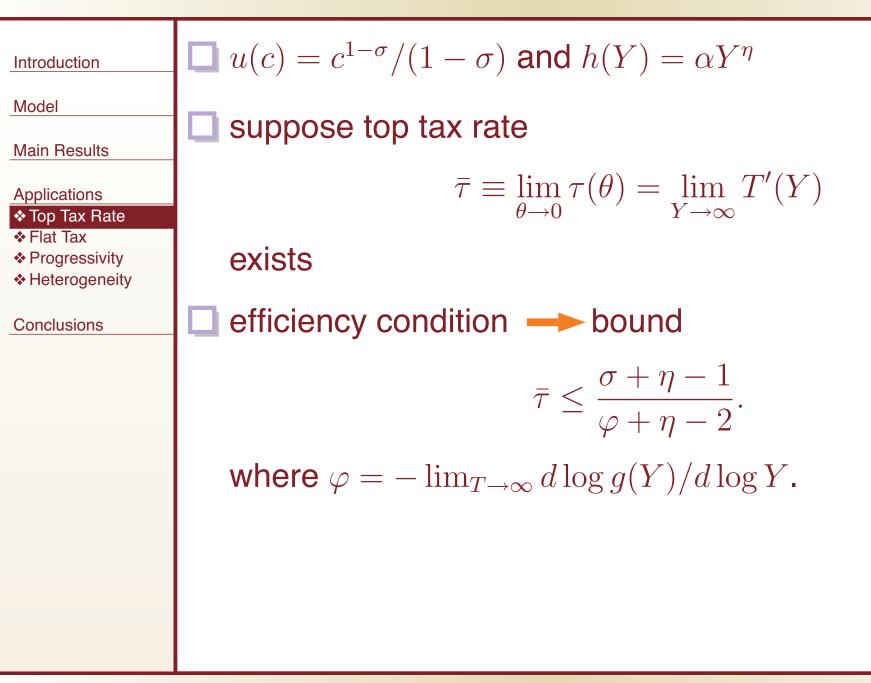
Model

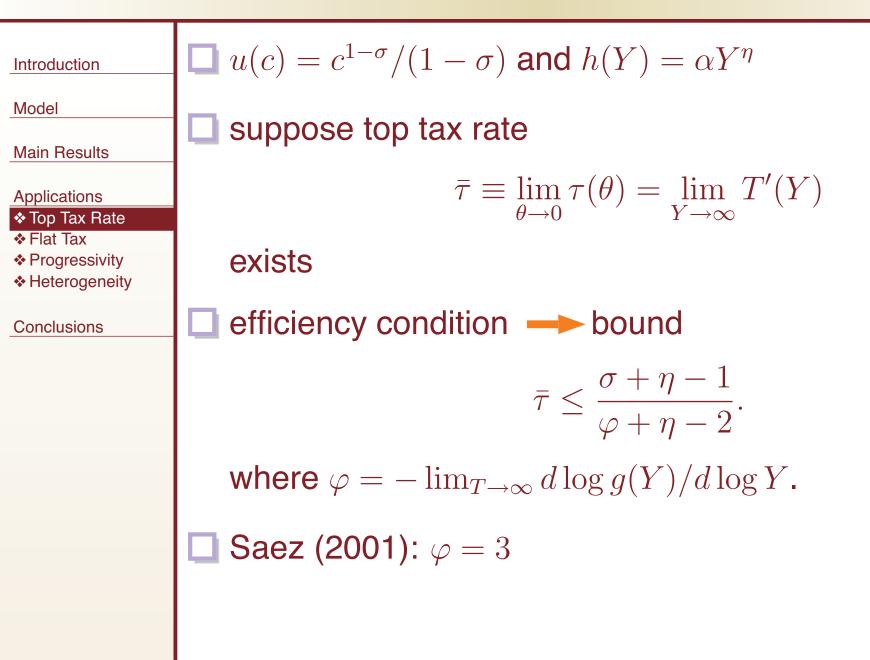
$$\Delta \equiv \int \left(\tilde{Y}^*(\theta) - \tilde{c}^*(\theta) \ dF(\theta) - \int \left(Y(\theta) - c(\theta) \ dF(\theta) \right) \right) dF(\theta)$$

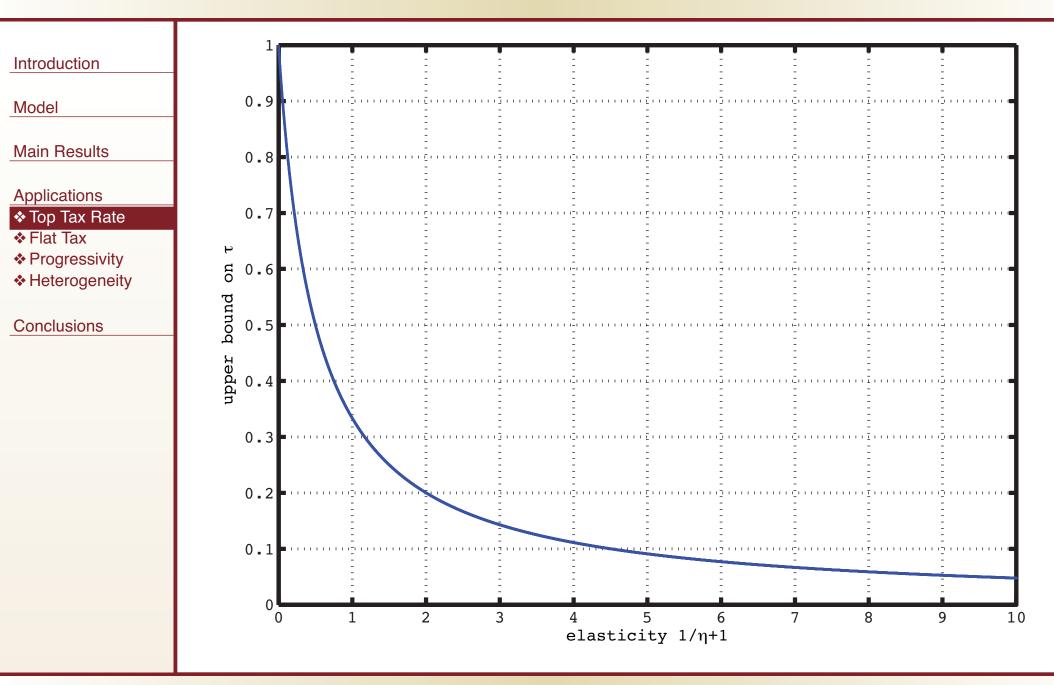
does not count welfare improvements

 $\tilde{v}(\theta) > v(\theta)$

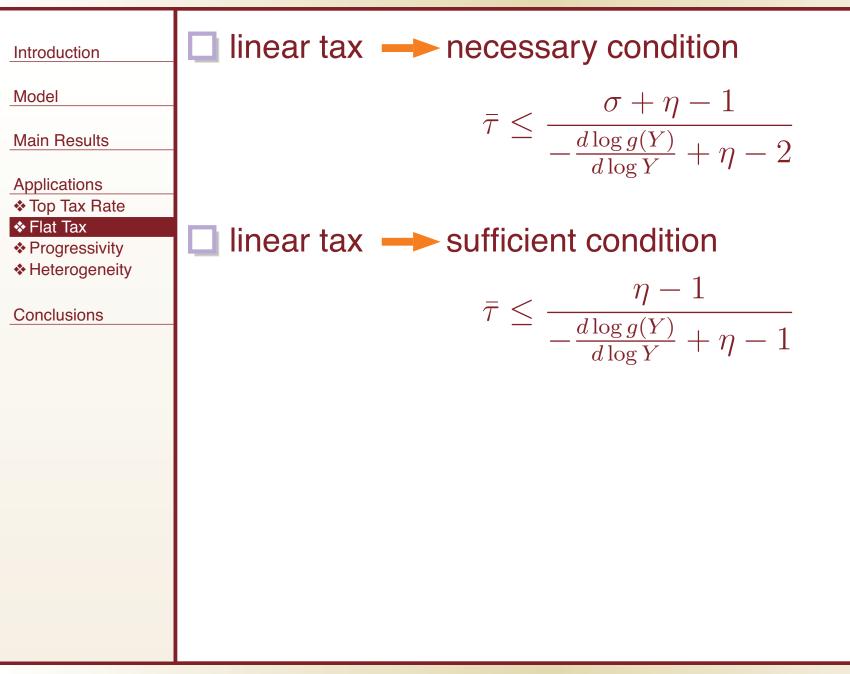








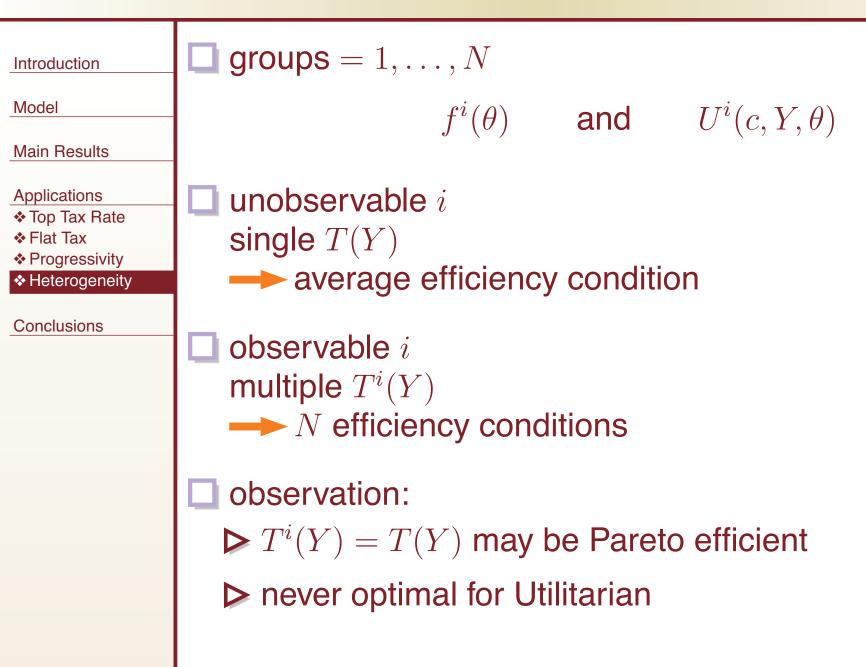
Flat Tax



Progressivity

Introduction	Quasi-linear $u(c) = c$
Model	result: can always increase progressivity
Main Results Applications	
 Top Tax Rate Flat Tax Progressivity 	
 Heterogeneity Conclusions 	

Heterogeneity



Conclusions

Introduction	Pareto efficiency
Model Main Results	generalizes zero-tax-at-the-top result
Applications	Pareto inefficient Laffer effects
Conclusions Conclusions	flat taxes may be optimal
	more progressivity always efficient

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