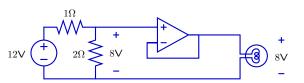


Last Time: Buffering with Op-Amps

Buffers can be used to simplify modular design.



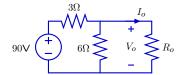
This op-amp circuit produces an output voltage equal to its input voltage (8V) while having no effect on the left part of the circuit.

There are also other useful ways to deal with element interactions. Today: **abstractions** to characterize circuit interactions

Systematic Changes

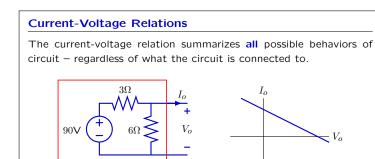
Altering an element changes voltages and currents systematically.

Example: consider changes in V_o and I_o when R_o is changed.

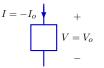


			$ \begin{array}{c} I_{o} \\ + \\ V_{o} \\ R_{o} \end{array} $	
How many	of the blue n	umbers are	e wrong?	
	R. [Q]	V_o [V]	τ. [Δ]	
	0		30	
		0	00	
	2	30	15	
	2		15 12	
	-			

Lecture 9



It allows us to think about circuit as a single element: a **one-port**.





A "one-port" is a circuit that is regarded as a single, generalized component.

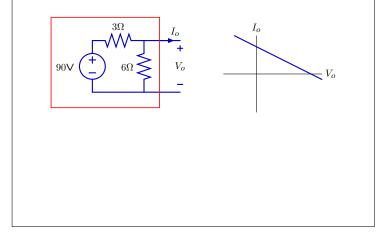


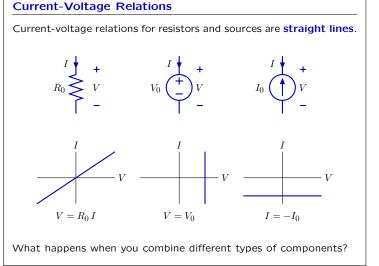
As with other components, a one-port has two terminals:

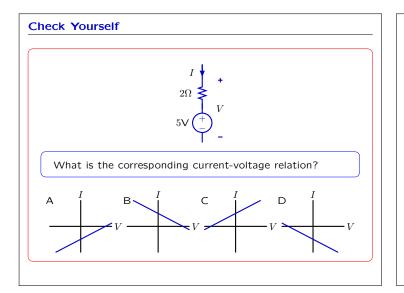
- current I enters "+" terminal and exits "-" terminal and
- produces voltage V across the terminals.



Under what conditions is the current-voltage relation a straight line?



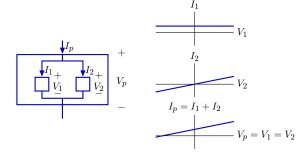




Parallel One-Ports

If the i-v curves for two one-ports are both straight lines, then the i-v curve for the parallel combination is a straight line.

Graphical "proof":



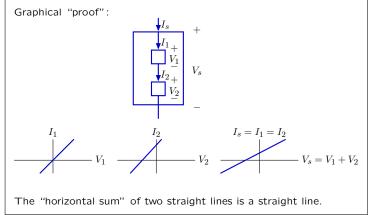
The "sum" of two straight lines is a straight line.

6.01: Introduction to EECS I

Lecture 9



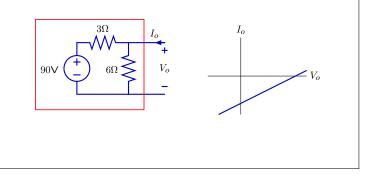
If the i-v curves for two one-ports are both straight lines, then the i-v curve for the series combination is a straight line.



Current-Voltage Relations

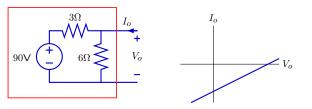
More generally, any combination of one-ports with straight i-v curves will produce a one-port with a straight i-v curve.

Example: if a one-port contains only resistors and sources, then the current-voltage relation will be a straight line.



Linear Equations

If the current-voltage relation is a straight line, then the relation between element current and element voltage is a **linear equation**.

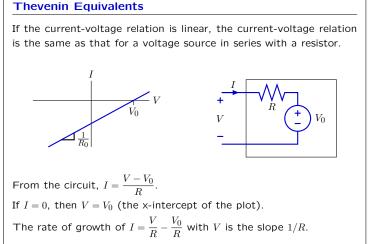


Linear equations have the form

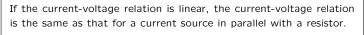
```
a_i V_i + b_i I_i + c_i = 0.
```

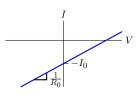
(i.e., there are no V_i^2 terms, no $\sqrt{I_i}$ terms, etc.)

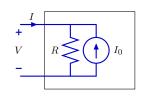
If all of the component equations are linear, then the i-v curve for the one-port will also be linear (since the solution to a system of linear components plus associated KVL and KCL equations is linear).



Norton Equivalents





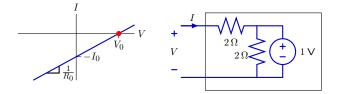


From the circuit, $V = (I + I_0)R$. If V = 0, then $I = -I_0$ (the negative of the y-intercept of the plot). The rate of growth of $I = -I_0 + V/R$ with V is the slope 1/R.

Open-Circuit Voltage and Short-Circuit Current

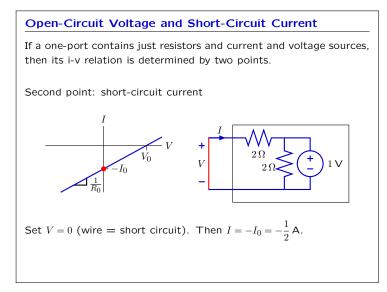
If a one-port contains just resistors and current and voltage sources, then its i-v relation is determined by two points.

First point: open-circuit voltage



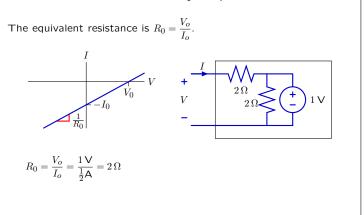
Set I = 0 in the circuit. Then $V = V_0 = 1$ V.

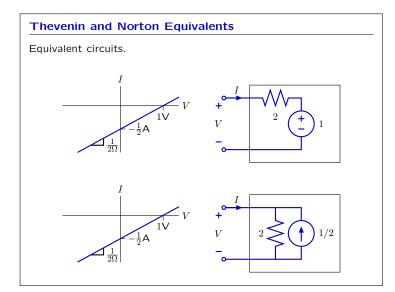
Lecture 9

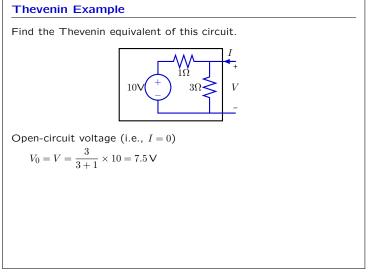


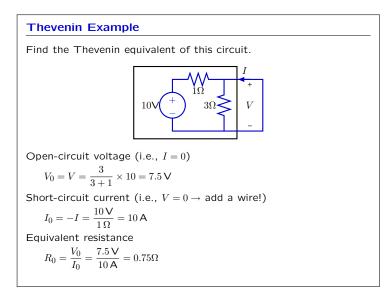
Open-Circuit Voltage and Short-Circuit Current

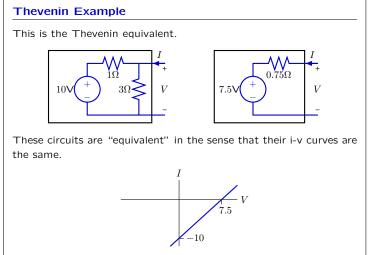
If a one-port contains just resistors and current and voltage sources, then its i-v relation is determined by two points.





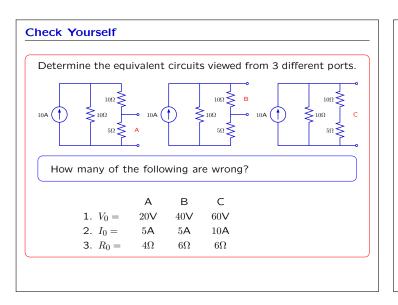






6.01: Introduction to EECS I

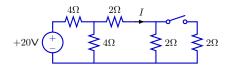
Lecture 9





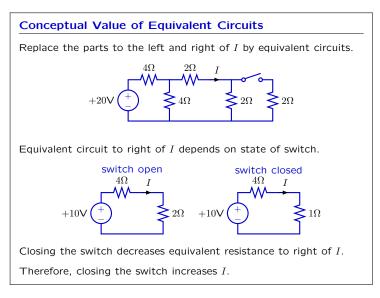
Equivalent circuits have conceptual value.

Example: Will closing the switch increase or decrease I?



We could just solve two circuits questions – one with switch open and one with switch closed – and compare currents.

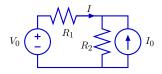
But this question can be answered without doing any calculations!



Superposition

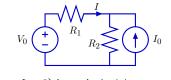
Superposition

If a circuit contains only linear parts (resistors, current and voltage sources), then any voltage (or current) can be computed as the sum of those that result when each source is turned on one-at-a-time.

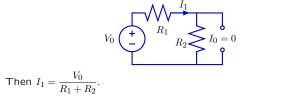


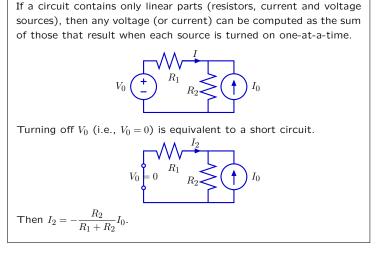
Superposition

If a circuit contains only linear parts (resistors, current and voltage sources), then any voltage (or current) can be computed as the sum of those that result when each source is turned on one-at-a-time.



Turning off ${\it I}_0$ (i.e., ${\it I}_0=0)$ is equivalent to an open circuit.





6.01: Introduction to EECS I

Lecture 9

Superposition

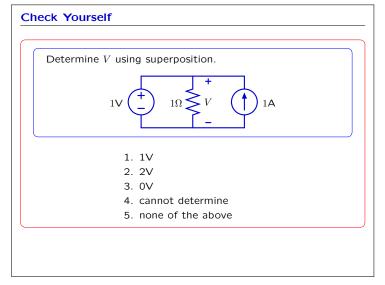
 $I = I_1 + I_2 =$

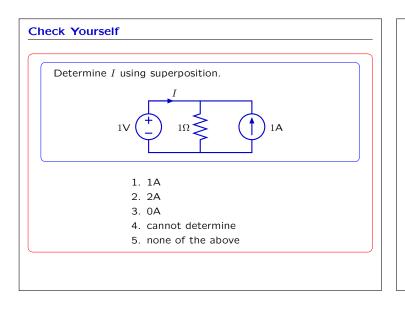
 $\overline{R_1 + R_2}$

If a circuit contains only linear parts (resistors, current and voltage sources), then any voltage (or current) can be computed as the sum of those that result when each source is turned on one-at-a-time. Combining: V_0 0 V_0 V_0 R_2

 I_0 .

 $R_1 + R_2$





Summary

Consequences of linearity.

If a one-port contains just linear elements (resistors, voltage sources, and current sources) then

- the current-voltage relation will be linear, and
- it can be represented by a Thevenin or Norton equivalent circuit.

Linear one-ports can be characterized by two points on their i-v curve (e.g., open-circuit voltage and short-circuit current).

Responses of multiple sources can be superposed to find electrical responses of linear circuits.

MIT OpenCourseWare http://ocw.mit.edu

6.01SC Introduction to Electrical Engineering and Computer Science Spring 2011

For information about citing these materials or our Terms of Use, visit: http://ocw.mit.edu/terms.