## MITOCW | ocw-6.033-lec22

0:00:00 0:00:20 We started last time on protection. 0:00:23.852 You remember the model that we're considering? 0:00:28.951 We've got some client communicating over the Internet 0:00:34.844 with some server. And we said that there are 0:00:39.716 three main technical problems that we're going to look to 0:00:46.062 address. There is the problem of 0:00:49.575 authentication, the problem of authorization 0:00:54.447 and the problem of confidentiality. 0:01:00 0:01:05 Today what we're going to do is we're going to talk mostly about 0:01:09.221 this issue of authentication, but I want to just return to 0:01:13.041 some of the details that we were talking about at the end of 0:01:16.994 class last time so that you guys all get the important bits out 0:01:21.149 of our discussion of the RSA protocol. 0:01:23.628 Remember, last time we started talking about these are the main 0:01:27.783 requirements of a protection system. 0:01:31 And we drew a diagram that said that at the top level we want to 0:01:35.295 have an application that is protected. 0:01:37.818 Underneath that we're going to have a set of security 0:01:41.363 primitives. And then, underlying all of 0:01:43.954 this, we're going to have cryptography. 0:01:46.545 Cryptography is going to be sort of the essential technique 0:01:50.5 that we use to enable protection. 0:01:52.681 We talked briefly about several different types of cryptography. 0:01:58 Remember, we had our model where we have A is sending 0:02:02.5 through some box which takes the data and transforms it using 0:02:07.692 some cryptographic transform. And then that cryptographically 0:02:12.884 transformed data gets transmitted and then is reverse 0:02:17.384 transformed or untransformed at the other side and it comes out 0:02:22.75 to the receiver. What cryptography does is we 0:02:27.27 said that we want this open model where there is some key k1 0:02:32.054 here and some key k2 here that are used to decide how this 0:02:36.675 transform operator works and this untransform operator works 0:02:41.459 on the other side. We talked about a shared key 0:02:45.189 case where k1 is equal to k2. And the appendix A of the 0:02:49.567 chapter in the notes goes over a shared key protocol called DES 0:02:54.594 that is fairly commonly used. The basic idea behind shared 0:02:59.904 key cryptography is typically that both sides have this key 0:03:03.848 and we're going to transform the data by combining the message 0:03:07.996 stream that is coming from A together with the key in some 0:03:11.872 way, say, for example, by xoring the data in many 0:03:15.135 different ways or permuting the data around and then xoring it 0:03:19.283 with the key in some combination of ways. 0:03:22.003 That's sort of what the DES protocol does. 0:03:24.792 It's just multiple rounds, basically, of permuting and 0:03:28.395 xoring the data over and over again. 0:03:32 The idea is that if an attacker doesn't know the key, 0:03:36.197 it's very hard for them to reverse this process without 0:03:40.557 having the key, but if you know the key it's 0:03:44.028 relatively easy to reverse the process. 0:03:47.096 We also talked a little bit about public key cryptography 0:03:51.617 where k 1 is not equal to k 2 . In this case, $0: 03: 54.927$ we started talking about this protocol RSA which is an example 0:03:59.851 of a public key protocol. If you remember, 0:04:04.046 RSA has some set of rules for actually doing the 0:04:07.121 transformation of data. The basic idea is that we're 0:04:10.457 going to get a private key and a public key here, 0:04:13.598 which is going to consist of this prime number plus the 0:04:17.13 product of these two prime numbers and this private key k 0:04:20.794 which is going to consist of the other prime number and the 0:04:24.588 product of these two things. Now we have this way in which 0:04:28.317 we can transform the data. What this transform box does is 0:04:32.833 simply raise the message to the power of e modulo $n$ and we have 0:04:36.5 the reverse transform. This is just a specific 0:04:39.161 mathematical operation. The reason that this 0:04:41.704 mathematical operation works is that the intuition is that it is 0:04:45.43 relatively easy to take something to an exponent. 0:04:48.268 I can take a number and exponentiate it without doing 0:04:51.344 very much work. But in order for an attacker to 0:04:55.174 compromise this system, that is in order to discover, 0:04:58.821 for example, what the private key is, 0:05:01.347 in this case, what this value d is, 0:05:03.732 given just the public key which consists of e and $n, 0: 05: 07.309$ the attacker is going to be able to factor this number n, 0:05:11.237 which turns out to be very difficult to do. 0:05:14.183 Essentially, breaking this cryptographic 0:05:16.919 system comes down to be able to factor a very large number. 0:05:20.987 And that turns out to be, computationally, 0:05:23.863 very, very difficult to do. So that's sort of the intuition 0:05:27.931 behind the protection of this scheme. 0:05:32 The nice thing about RSA is it has, in most public key 0:05:35.54 cryptographic protocols is that they have this property that the 0:05:39.75 reverse is also true. So I can transform using 0:05:42.756 exponentiation with the public key or the private key and I can 0:05:46.898 reverse transform using the opposite. 0:05:49.303 If I transform with the public key, I can reverse transform 0:05:53.178 with the private key and vise versa. 0:05:55.517 So we are going to exploit this property a lot when we're 0:05:59.258 talking about this kind of cryptography. 0:06:03 Just to sort of point out that this is hard, 0:06:05.734 this is an estimate from the RSA Security Company about how 0:06:09.423 many compute years on modern computers it would take to 0:06:12.857 factor an RSA key of a given link. 0:06:14.956 So the bottom is the key link in bytes on the $x$-axis and then 0:06:18.771 the $y$-axis is the machine years to factor. 0:06:21.379 If the machine years to factor was 1,000 , that means it would 0:06:25.195 take 1,000 machines working together one year to do this or 0:06:28.883 one machine 1,000 years to do it. 0:06:32 So you see that the $y$-axis here is going up exponentially. 0:06:36.035 So to factor a 500 byte key is not that hard. 0:06:39.15 It takes maybe a few months of compute time to do it. 0:06:42.831 To factor a 2,000 byte key takes this a ridiculously long 0:06:46.796 time, ten to the 16th years it is going to take to factor this 0:06:51.115 thing. So there is just no way that, 0:06:53.592 at least modern computers, are ever going to be able to 0:06:57.415 actually perform this factoring using currently known algorithms 0:07:01.876 for factoring. It is, of course, 0:07:04.959 possible that somebody will develop a very fast factoring 0:07:08.118 algorithm or that there will be some fundamental breakthrough 0:07:11.503 like quantum computing that will make it possible to factor very 0:07:15.058 large numbers. But, at this point, 0:07:16.92 this is sort of the estimate of how long it would take to do 0:07:20.249 this. So, by using long keys, 0:07:21.828 you can be sort of guaranteed that somebody won't be able to 0:07:25.157 actually factor this number. So by using a factorina-based 0:07:28.373 attack on RSA that sort of won't be able to break it in this wav. 0:07:33 The laraest

RSA number that has been factored to date is some 0:07:36.866 500 odd byes, something like 520 bytes, 0:07:39.315 so RSA has challenges for the largest numbers that can be 0:07:42.923 factored. So we're sort of just barely on 0:07:45.501 this curve is where the largest numbers that have been factored 0:07:49.496 to date. And these are typically some 0:07:51.816 collection of machines on the Internet. 0:07:54.264 Somebody gets 1,000 machines on the Internet and they chew on 0:07:58.131 this problem. I think, in this case, 0:08:01.896 it took 1,000 machines three months to find a factor of this 0:08:06.982 500 byte key. This is the basic idea now. 0:08:10.431 What we're going to do is use these cryptography algorithms, 0:08:15.517 this math to build up a set of primitives that we can use to 0:08:20.603 actually accomplish our security goals that we want. 0:08:25 And I put these on the board briefly last time. 0:08:30 But I didn't talk at all about what the actual functionality 0:08:32.892 is. And we're going to spend a lot 0:08:34.509 of time talking about two of these primitives today, 0:08:37.009 and then we'll talk about a few more of them next time. 0:08:40 0:08:48 We have two sets of primitives in particular that we are 0:08:54.226 interested in. One set is called sign and 0:08:58.754 verify. And the other set is called 0:09:01.643 encrypt or decrypt. And we're going to use sign and 0:09:04.685 verify basically as a way to achieve authentications. 0:09:07.849 Remember, authentication is the process of verifying that a 0:09:11.379 message actually came from who it was supposed to come from. 0:09:14.969 And we're going to use encrypt and decrypt in order to provide 0:09:18.681 confidentiality to guaranty that somebody who we don't want to be 0:09:22.576 able to read a message, somebody who shouldn't be able 0:09:25.801 to read a message can, in fact, not read that message. 0:09:30 Let me just illustrate a simple example. 0:09:35.282 Suppose we're using a public key system, we can say suppose 0:09:43.139 we use something like RSA to encode a message $m$ with some 0:09:50.725 key, say we're sending a message from $A$ to $B$, we use it to encode 0:09:59.394 some key, say, kA private. 0:10:04 What this notation means is that whoever has A's private key 0:10:09.344 encodes that message or transforms that message using a 0:10:14.236 cryptographic protocol using, say, for example, 0:10:18.404 kA private. What this says is Alice, 0:10:21.574 perhaps as A, runs her RSA algorithm on the 0:10:25.379 message and generates some encoded thing. 0:10:30 This is an encryption. We're going to use this 0:10:34.368 encoding with the private key to sign a message. 0:10:38.932 When Alice encodes this with her private key what that means 0:10:44.66 is that somebody who has Alice's public key can decode this, 0:10:50.388 because we said if you encode with the private key somebody 0:10:56.019 with the public key can decode. For example, 0:11:00.675 if she sends this to Bob, Bob is going to be able to $0: 11: 03.545$ decode this. At first that seems like, $0: 11: 05.628$ well, what good does that do us? 0:11:07.373 Bob can read this message. But the thing is if Bob can 0:11:10.356 decode this, what he knows, with very high certainty is $0: 11: 13.395$ that the person who encoded this message had access to A's $0: 11: 16.604$ private key. If he is willing to trust that, $0: 11: 19.024$ in fact, the only person who has access to A's private key is 0:11:22.401 A herself, then he can be reasonably confident that this 0:11:25.497 message came from A. You guys all sort of see how 0:11:28.198 that works. What we say is that Alice signs 0:11:33.069 this message. And, by signing this message, 0:11:37.227 she is able to sort of give Bob some confidence that this 0:11:42.772 message, in fact, came from her. 0:11:45.841 We can also do the opposite thing where, say, $0: 11: 50.198$ for example, Alice is sending a message to 0:11:54.257 Bob. She can take $m$ and sign it with 0:11:57.722 kB public. Sorry, she can encrypt it with 0:12:01.99 kB public. She is going to use the RSA 0:12:04.444 algorithm. She is going to encrypt this 0:12:06.965 message. And, when she encrypts this $0: 12: 09.287$ message, she is going to basically use the RSA algorithm 0:12:12.936 using kB public. And what is going to happen is $0: 12: 15.987$ now she is going to be reasonably assured that this $0: 12: 19.304$ message is going to be able to only be read by Bob because only 0:12:23.417 Bob presumably has his own private key. 0:12:27 What I've shown here makes this look very simple. 0:12:29.884 I sort of said it as though we're simply taking this message 0:12:33.43 and running the basic RSA algorithm, as I showed it, 0:12:36.495 on the message in order to do sign and in order to encrypt. 0:12:39.981 It turns out that actually getting sign and encrypt to work 0:12:43.467 property requires some fairly sophisticated sort of reasoning 0:12:47.073 about the RSA algorithm. For example, $0: 12: 49.237$ when you're encrypting something, if the message is $0: 12: 52.242$ very small, it turns out that if you encrypt a small message 0:12:55.787 simply using the RSA algorithm as I presented it that it's 0:12:59.213 relatively easy to break the RSA algorithm. 0:13:03 The RSA algorithm becomes vulnerable with very small 0:13:05.684 messages. That means the encryption 0:13:07.473 process actually needs to pad out the message to some longer 0:13:10.578 link. It needs to put unused bytes at 0:13:12.473 the end of every message in order for it to be secure. 0:13:15.263 These sign and encrypt algorithms themselves sort of 0:13:17.947 have to do some additional work on top of the basic RSA 0:13:20.789 algorithm in order to be secure. And that additional work is 0:13:23.894 sort of beyond the scope of this class. 0:13:25.894 It requires a certain degree of mathematical sophistication that 0:13:29.21 we are not going to rely on here. 0:13:32 You can go take an extra class about cryptography and learn 0:13:36.441 about how these sign and encrypt algorithms actually work, 0:13:40.806 but the basic idea is that you can sort of grasp it by just 0:13:45.247 seeing RSA. These things are hard to build. 0:13:49 0:13:54 Now that we have sort of quickly reviewed the basics of 0:13:58.712 protection and we've seen the sign and verify and encrypt and 0:14:03.949 decrypt primitives, now what I want to do is to 0:14:07.963 talk a little bit about how we can actually start building up, $0: 14: 13.287$ solving this problem of authenticating a user. 0:14:18 When we authenticate a user we have two objectives. 0:14:24.746 One thing we're trying to achieve is to determine who is 0:14:32.166 making a request. 0:14:35 0:14:40 In practice, it's going to turn out, 0:14:43.173 in fact, that we may not officially be able to say 0:14:47.616 exactly the specific person who is being able to make the 0:14:52.694 request. We may only be able to say that $0: 14: 56.23$ the same principle or person or computer as before is making the 0:15:01.943 request, or the same principle who had some special privileged 0:15:07.474 piece of information that the person before had is making this $0: 15: 13.005$ request. We may not be able to actually 0:15:16.453 associate this with a physical person, but at least we're going 0:15:19.456 to be able to know that we've seen somebody who had this same 0:15:22.363 information before. We're trying to make sure that $0: 15: 24.737$ this is sort of consistent with a series of reauests that we've $0: 15: 27.74$ seen in the past. A simple
example is I lot onto 0:15:31.399 Amazon, I create a password. Now, anybody who I give that 0:15:35.879 password to can log onto Amazon. And all the system can say is $0: 15: 40.759$ that it knows that whoever it is who is accessing definitely has 0:15:45.799 my password information and sort of it doesn't know officially 0:15:50.679 that it is actually the same physical person. 0:15:55 The other thing, though, that we want 0:15:57.58 authentication to do is to tell us basically that the message 0:16:01.881 that was sent is equal to the message that was received. 0:16:05.824 We want it to be the case that if Alice sends a message to Bob, $0: 16: 10.268$ that when Bob receives that message, we want him to have $0: 16: 14.211$ some assurance that, in fact, that message was 0:16:17.437 actually the message that Alice tried to send. 0:16:20.663 And we're going to talk about how this is sort of going to 0:16:24.749 relate to the problem of integrity that we talked about 0:16:28.62 before, verifying that a message hasn't been corrupted in 0:16:32.634 transmission. But this is actually a harder 0:16:36.625 requirement because we might need to not only worry about 0:16:39.762 sort of random bits being flipped by the communication 0:16:42.732 channel but we need to worry about some malicious person 0:16:45.814 coming in and physically actively modifying the bytes of $0: 16: 48.896$ the message. Authentication is sort of the $0: 16: 51.193$ first step that we need to have in any secure system because 0:16:54.5 authentication is going to be the key. 0:16:56.573 We have to authenticate a user before we can authorize the 0:16:59.767 user. Before we can say, 0:17:02.211 yes, this user is allowed, we have to figure out who the 0:17:05.911 user is. And, similarly, 0:17:07.459 we can use authentication, this process of figuring out 0:17:11.092 who a user is to help us to build up audit trails. 0:17:14.389 Remember we said audit trails are something that is important. 0:17:18.494 Once we figure out who a user is, we can keep logs of which 0:17:22.396 user it was that connected to our machine. 0:17:25.155 Let's look at a simple model of how authentication works. 0:17:30 0:17:35 The idea is as follows. We have our principle, 0:17:41.83 say, for example, a user who is sending a request 0:17:49.116 to some server. 0:17:52 0:17:57 And this request might be something, for example, 0:18:00.263 like buy Apple stock. And the server's job is to 0:18:03.46 determine whether this request is actually authentic, 0:18:06.996 whether it actually came from the user it claims to come from 0:18:11.076 and whether the message that was received is actually the message $0: 18: 15.428$ that was sent. The way it's going to do this $0: 18: 18.352$ is we're going to introduce something we call a guard that 0:18:22.228 is at the front end of this server that takes in all the 0:18:25.968 incoming requests and is in charge of authenticating them. 0:18:31 And then this guard is going to dispatch results off to any of $0: 18: 34.714$ the services that the server provides. $0: 18: 36.967$ It is going to say if the request is authentic it is going 0:18:40.437 to invoke the service that we need. 0:18:42.508 In other words, this guard is the type of 0:18:44.943 mediator that sits in between all the requests between the 0:18:48.414 principle and the service that it is trying to access and the 0:18:52.067 guard is going to be the thing that does all of our 0:18:55.112 authentication. 0:18:57 0:19:07 Now the question is what is it exactly that the guard does? 0:19:10.914 What are the processes that the guard has to go through in order 0:19:15.167 to authenticate a user? And, before we talk about the 0:19:18.677 specific technical solution, I want to sort about two things 0:19:22.66 that are really going on when you're trying to figure out who 0:19:26.71 it is that is requesting and whether you're going to allow 0:19:30.557 that person to do what they want to do. 0:19:34 So the issue is, essentially, $0: 19: 36.044$ as follows. There is this question about is 0:19:39.112 the computer that is making this request actually have the 0:19:43.275 appropriate keys to make this request? 0:19:45.977 Does it have the appropriate password to be allowed to make 0:19:50.213 this request? Then there is this other 0:19:52.915 question which is do I trust this user? 0:19:55.691 Is this somebody who I want using my service? 0:20:00 Suppose that I go to E*Trade and say I want to buy Apple. 0:20:04.137 How does E*Trade decide whether or not it trusts me, 0:20:07.905 whether I'm somebody who is allowed to buy Apple stock from 0:20:12.189 them or not? So they have some process for 0:20:15.218 doing that. You have this mechanical 0:20:17.804 process of authentication. And then we have this sort of 0:20:21.868 psychological process of determining whether or not you 0:20:25.857 trust somebody. So this authentication is going 0:20:30.896 to be a technical thing and we are going to describe this as 0:20:36.409 being psychological. What these things are connected 0:20:41.174 by is some notion of a name. What the authentication says 0:20:46.406 is, for example, Sam wants to buy Apple. 0:20:50.05 It determines that I am, in fact, the person who is 0:20:54.722 making the request, that it is able to verify that $0: 20: 59.3 \mathrm{I} \mathrm{am}$ the one who is actually making the request. 0:21:05 What trust is responsible of doing is determining whether or 0:21:08.485 not Sam should actually be allowed to make this request. 0:21:11.734 And this is not something that we necessarily have a technical 0:21:15.337 solution to. Different computer systems have 0:21:17.877 different ways of determining whether or not they should trust 0:21:21.481 each other. For example, 0:21:22.839 when you go to a service on the Web, you make a decision about 0:21:26.443 whether you trust that service based on some sort of way that 0:21:29.987 you have of evaluating the service. 0:21:33 Maybe your Mom told you that $\mathrm{E}^{\star}$ Trade is the best place to buy $0: 21: 36.157$ stocks on the Internet with. You trust your Mom and so, 0:21:39 therefore, you trust E*Trade. Or maybe you saw an 0:21:41.526 advertisement for E*Trade and you think any company that has 0:21:44.631 enough money to advertise on the side of the freeway must be a 0:21:47.842 trustworthy company and, therefore, I trust you. 0:21:50.315 Similarly, E*Trade, presumably determines that they 0:21:52.947 trust you based on, well, one thing they might do 0:21:55.473 is, you might give them a bank account number, 0:21:57.842 and your bank might say, yes, this person has enough 0:22:00.526 money to make this request. That is a way that they might 0:22:04.788 decide that they trust you. Alternatively, 0:22:07.315 $\mathrm{E}^{\star}$ Trade gives out loans, so maybe they go talk to your 0:22:10.583 credit reporting agency, and the credit reporting agency 0:22:13.974 says, yeah, this guy is trustworthy. 0:22:16.132 He has a high credit score so, therefore, $E^{*}$ Trade will let you 0:22:19.894 borrow $\$ 1,000$ to invest in the stock market or something. 0:22:23.346 This issue of trust is one that we don't have a technical 0:22:26.799 solution to, but it is absolutely an essential part of 0:22:30.067 authenticating and authorizing a user to use a computer system. 0:22:35 So it's worth just bearing this in mind that any time you're 0:22:38.859 building a computer system you need to think about how it is 0:22:42.719 that vou determine whether a user is trustworthv or not. 0:22:46.317 And this aoes both wavs. both
for the user of the 0:22:49.457 system, how do they determine that you're trustworthy, 0:22:52.925 and for the system, how do you determine that the 0:22:56.065 users are trustworthy? Now the key problem is focusing 0:22:59.532 on this sort of authentication problem. 0:23:03 What is the technical meat of how we're actually going to 0:23:05.871 authenticate a user? 0:23:07 0:23:17 One of these problems is determining that this message 0:23:21.373 that was sent was actually the message that was received. 0:23:25.995 Here is a simply proposal that I might have which is I might 0:23:30.864 compute one of these CRC checks. These checksums that we talked 0:23:35.693 about when we were talking about networking that we used to 0:23:38.967 determine whether or not the message has been corrupted in 0:23:42.185 transmission. It turns out that is not going 0:23:44.612 to work. You might also think the way 0:23:46.645 that you are going to insure that the person who is 0:23:49.467 requesting the message is actually who they claim to be 0:23:52.516 is, for example, using our encryption primitive. 0:23:55.169 If we had a one time pad available to us, $0: 23: 57.427$ we might encrypt the entire stream of data that is going 0:24:00.532 across. And then we would think well, $0: 24: 04.1$ there is no way that somebody on the other end, $0: 24: 07.432$ unless they are authorized to read this, will actually be able $0: 24: 11.85$ to read it. And, therefore, $0: 24: 13.733$ this is going to give us some guaranty about who is making the 0:24:18.151 request. Neither of these things quite 0:24:20.831 works, and let me explain why. Integrity, in the sense that we 0:24:25.25 studied it previously in 6.033, is not equal to authenticity, 0:24:29.595 is not equal to confidentiality. 0:24:33 0:24:38 And the reason is as follows. Let's just look at a simple 0:24:42.2 example. Suppose there is Alice who is $0: 24: 44.974$ sending a message to some server, and suppose this server 0:24:49.174 is something where Alice doesn't really mind if her request is 0:24:53.75 seen in public but she wants to make sure that the server $0: 24: 57.95$ actually receives the request that she made. 0:25:02 So she cares about it being the right request, 0:25:05.425 but she doesn't care about it being a secret request. 0:25:09.383 Maybe Alice says I want to donate $\$ 100$ to Save the Whales. 0:25:13.721 She says I don't care if anybody knows that I want to 0:25:17.679 save the whales. That's a noble and respectful 0:25:21.104 cause. In fact, I am proud of the fact 0:25:23.921 that I want to save the whales. So anybody who wants to can 0:25:28.335 look at this message. But I really only want to give 0:25:33.059 Save the Whales $\$ 100$. I want to make sure that $0: 25: 36.148$ somebody doesn't mess with this message and some Save the Whale 0:25:40.405 activist doesn't change this message to be $\$ 10,000$ so that I $0: 25: 44.455$ don't lose a bunch of money. Let's look at some techniques 0:25:48.368 that we might use to sort of guaranty that this is the case. 0:25:52.418 One thing we might do is, for example, 0:25:54.958 use a one time pad. Suppose Alice and the server 0:25:58.185 share a random bit string. Alice might encode, 0:26:02.283 might xor the message that she transmits, and then the server 0:26:06.337 might apply the xor again with the same bit string and get the 0:26:10.459 message back. The problem with this is that 0:26:13.297 this doesn't prevent some malicious user or Lucifer from 0:26:17.013 coming into the middle of this and interfering with this byte 0:26:21.067 string as it is transmitted. Even though Lucifer cannot 0:26:24.716 actually look at the message, he can manipulate the byes to 0:26:28.635 his heart's content. And he may get lucky and change 0:26:33.296 the bytes so that it says something like donate some 0:26:37.074 different amount of money to save the whales or he may just 0:26:41.37 garble Alice's requests so it cannot be processed. 0:26:45 So one time pad is not going to work. 0:26:47.666 Now, the other alternative I said we can talk about would be 0:26:52.037 something like using a CRC. What Alice would do is send $m$ 0:26:56. 185 followed by the CRC of $m$. The problem with this is that 0:27:00.644 now Lucifer can look at this message as it comes across the 0:27:03.932 wire and the checksum, and he can simply change the 0:27:06.768 message to say whatever he wants and then recomputed the 0:27:09.886 checksum. So the checksums, 0:27:11.36 as we have talked about them so far, are good for handling the $0: 27: 14.819$ case of non-malicious attacks or non-malicious problems like a 0:27:18.278 byte gets changed in transmission or there is some 0:27:21.056 error in transmission, but they don't solve this 0:27:23.721 problem of preventing somebody from tampering with the message 0:27:27.18 and being able to detect when that tampering also effects the 0:27:30.582 CRC. If you think about this for a $0: 27: 34.402$ minute, the property that we want sort of feels like some 0:27:39.041 combination of these two things. Basically, what we want is some 0:27:44.26 checksum-like operation such that we know that the only 0:27:48.733 person who could have possibly written this checksum was 0:27:53.289 somebody who access to some key that Alice has like Alice's 0:27:58.094 private key. We want a checksum that is 0:28:02.314 dependent on a key, and we want this checksum to 0:28:06.497 have some fairly strong properties. 0:28:09.523 We want this checksum to be resistant to these kinds of 0:28:14.329 attacks that we talked about Lucifer applying. 0:28:18.335 In particular, we want the checksum to be 0:28:21.895 resistant to Lucifer modifying the message. 0:28:25.633 So the checksum should detect that this message was modified, $0: 28: 30.973$ if it was modified. We also want it to be able to $0: 28: 36$ detect other transformations of the message. 0:28:38.965 For example, suppose that rather than 0:28:41.448 modifying $m$, changing something, Lucifer just reorders some of 0:28:45.655 the words in it, keeps exactly the same 0:28:48.275 characters and exactly the same length but just switches some 0:28:52.413 things around. And there are other kinds of 0:28:55.31 things that we might want to be able to resist as well. 0:29:00 For example, taking exactly the same message 0:29:02.648 and sticking a little bit of extra data onto the end of it, 0:29:06.221 appending something to the message. 0:29:08.316 There is a bunch of different sort of properties that we want 0:29:12.012 whatever this thing is that is going to allow us to do 0:29:15.277 authentication to have. Let's look at the sort of model 0:29:18.603 for how our basic authentication system is going to work. 0:29:22.053 It is really pretty straightforward and is going to 0:29:25.133 rely on using our sign and verify primitives that I am 0:29:28.398 erasing. 0:29:30 0:29:35 The idea is as follows. We have Alice over here that is 0:29:39.72 sending a message. That message is going to go 0:29:43.653 into our sign cryptographic primitive, it's going to be 0:29:48.374 transformed and is going to come over here to our verify box, 0:29:53.618 and then it is going to come out on the other side at the $0: 29: 58.513$ server. And the sign is going to have 0:30:01.626 some k 1 that gets fed into it and verify is going to have some 0:30:05.046 k2 that gets fed into it. And the idea is that in 0:30:07.738 addition to signing the message we are also aoina to transmit 0:30:11.102 the messaae itself. So this is aoina to be sort of 0:30:13.85 like this idea
of putting a CRRC on a message, $0: 30: 16.317$ but this thing that we are going to do when we sign is $0: 30: 19.289$ going to provide this sort of better properties than the basic 0:30:22.71 CRC did. The idea is this is a small bit $0: 30: 25.493$ of additional information that gets transmitted with the 0:30:28.144 message that allows the server to be confident that, 0:30:30.602 in fact, the message that was transmitted came from Alice and 0:30:33.493 that it has not been corrupted along the way. 0:30:36 0:30:46 This is the basic idea now k 1 comes in, it gets transmitted, 0:30:49.771 goes through the verify box, and the verify box reports yes 0:30:53.479 or no, this message was correct or was not correct. 0:30:56.675 And the server also has access to the message. 0:31:00 If the server gets yes in the message then it continues to $0: 31: 04.51$ process it. And we have two kinds of ways $0: 31: 07.676$ of doing authentification that correspond to shared key and $0: 31: 12.266$ public key cryptography. If $k 1$ is equal to $k 2$ we say 0:31:16.302 that this little bit of information that we have 0:31:20.021 transmitted is a MAC, a message authenticator. 0:31:23.582 When you are using shared key cryptography that is the bit of 0:31:28.33 additional information that gets transmitted. 0:31:33 And when $k 1$ is not equal to $k 2$, that is if we're using public 0:31:37.792 key cryptography, we call this bit of additional 0:31:41.547 information a signature. To give you a very simple 0:31:45.461 example of what a signature might consist of, $0: 31: 48.976$ suppose we have a message m . In public key cryptography, 0:31:53.369 a simple kind of signature that you can compute is to take the 0:31:58.242 hash of m . And then take that thing and 0:32:02.462 encode it with Alice's private key. 0:32:05.453 This is a simple kind of a signature that we might attach 0:32:10.379 to a message. And this has the properties we $0: 32: 14.162$ want, which is that we believe that only Alice could have 0:32:19.087 actually encoded this message because we belief that only 0:32:24.013 Alice has access to her private key. 0:32:27.092 And so when somebody uses the public key to decode this they 0:32:32.282 get something back which is a hash of the message. 0:32:38 And we call this a cryptographically secure hash. 0:32:43.608 It is some way of combining the bits of the message together $0: 32: 50.501$ such that when the server computes the hash of $\mathrm{m}, 0: 32: 56.109$ the probability that it matches this hash that was in the 0:33:02.652 signature that Alice sent, they will match if the messages 0:33:09.312 are the same. And, if the hash was computed 0:33:13.689 on a different message than the message that the server 0:33:16.834 receives, the probability is very, very low that these two 0:33:20.155 messages are, in fact, the same. 0:33:21.961 So they say it has a low collision probability. 0:33:24.64 It's very unlikely that some m prime that is not equal to m has $0: 33: 28.252$ the same hash as m . That's what a cryptographically $0: 33: 31.815$ secure hash provides us. And, again, cryptographically 0:33:34.92 secure hashes are another kind of sort of mathematical 0:33:38.025 technique. There is a set of algorithms 0:33:40.251 for driving these things. The appendix talks about a 0:33:43.238 common one which is used called sha-1. 0:33:45.405 And sha-1, it turns out, has recently been shown to have 0:33:48.627 some higher probability of collisions than was previously 0:33:51.907 thought. And there is a new protocol 0:33:53.958 called sha-256 which is still believed to be secure. 0:33:58 But sha-1, the S-HA, which stands for secure hash, 0:34:01.161 is one that is very commonly used in the world today. 0:34:04.449 So this is a simple example of a signature and it allows 0:34:07.926 basically for the server to verify one by decoding the 0:34:11.277 message with Alice's public key that the message actually came 0:34:15.134 from Alice, and this hash allows it to be reasonably assured that 0:34:19.181 the message has not been tampered with. $0: 34: 21.584$ If the message had been tampered with the hash wouldn't 0:34:24.998 match, and if this signature had been tampered with then the 0:34:28.728 receiver wouldn't have been able to decode this thing and get 0:34:32.522 something back that made any sense. 0:34:36 Or, again, the hash probably wouldn't match. 0:34:40.909 This is the basic solution for doing authentication. 0:34:46.732 This screen is too low. Now that we've sort of seen a 0:34:52.669 method for authenticating a message, there are sort of a 0:34:58.948 bunch of little details that we left hanging. 0:35:05 In particular, one of the details that we 0:35:07.636 haven't yet addressed is, suppose we are using some 0:35:10.931 public key based mechanism like this, I haven't yet told you or $0: 35: 15.017$ we haven't talked about how it is that somebody would learn 0:35:18.839 Alice's public key? We sort of just assumed that 0:35:21.936 whoever is receiving the message is able to figure out what 0:35:25.759 Alice's public key is. And one thing you could imagine $0: 35: 29.637$ is that Alice goes around and physically meets everybody who 0:35:32.755 she would ever want to give a key to and she hands them a slip 0:35:35.978 of paper that has her public key written on it. 0:35:38.409 But, obviously, one, that's not how the 0:35:40.416 Internet works clearly because we have some cryptographic 0:35:43.375 protocols that allow us, we don't have to meet everybody 0:35:46.281 and we can still get established secure communication channels. 0:35:49.557 And, two, that just doesn't sound very scalable. 0:35:52.041 It doesn't sound like a great solution. 0:35:55 This is the key distribution problem. 0:35:57.495 This is going to apply mostly for the case of public key 0:36:01.306 cryptography. In the case of shared key 0:36:03.94 cryptography, this method I am going to show 0:36:06.92 you in a minute is not going to apply necessarily to shared key 0:36:11.217 cryptography, but I will show you a way in 0:36:14.059 which we can use public key cryptography to sort of 0:36:17.524 bootstrap or to exchange a shared key which we can then use 0:36:21.544 over our communication channel. This is the key distribution 0:36:25.633 problem for public key cryptographic systems. 0:36:30 0:36:35 One solution, if Alice cannot physically meet $0: 36: 40.617$ with Bob, one thing that you might imagine doing is you could $0: 36: 48.276$ just have Alice send a message to Bob saying here is my public 0:36:56.063 key. Or, better yet, 0:36:58.489 Alice's public key is, A's public key is X. 0:37:05 But this isn't a very good approach because how does B 0:37:08.256 actually know that this was Alice that sent this message? 0:37:11.698 This could have been some Lucifer who said, $0: 37: 14.279$ oh, by the way, Alice's key is this. 0:37:16.43 And now B thinks that Alice's key is, in fact, 0:37:19.195 Lucifer's key. And now Lucifer can decode any 0:37:21.899 message that $B$ wants to send to $A$. 0:37:23.927 So this isn't really a very good approach because if A just, 0:37:27.553 sort of out of the blue, blurts out to be my key is this 0:37:30.932 then it doesn't have any way of actually knowing that this was, $0: 37: 34.743$ in fact, A who reported this key. 0:37:38 That doesn't solve our problem. Instead, we are going to use a $0: 37: 41.279$ technique called certificates. 0:37:43 0:37:48 Certificates work like this. The idea with certificates is 0:37:52.576 that we are going to introduce a third-partv who I have shown 0:37:57.394 here as Charles. Let's supdose that Alice and

0:38:01.508 Bob know and trust Charles. So they have already somehow 0:38:06.436 exchanged information with Charles, exchanged keys with $0: 38: 11.274$ him. The idea is now suppose Alice $0: 38: 14.231$ wants to send a message to Bob. What she does is she sends this 0:38:19.786 message, and she signs the message using her private key. 0:38:24.803 That is what this S parentheses m kApriv means. 0:38:30 Now what Bob is going to do is say, well, I don't know who this 0:38:33.419 Alice is. And rather than simply asking 0:38:35.516 Alice for her public key, which we have already said is 0:38:38.494 not a very good idea, what Bob does is he asks 0:38:40.976 Charles for her public key because he trusts Charles and he 0:38:44.176 knows that Charles probably knows something about Alice. 0:38:47.209 And what Charles responds with is Alice's public key, 0:38:50.078 as well as he needs to make sure that he, 0:38:52.284 himself, signs this message with his own private key so that 0:38:55.539 somebody else cannot intercept the message as it is coming back 0:38:58.959 and overwrite it. He put his signature on this 0:39:03.036 message that he sends back with Alice's public key in it. 0:39:07.109 Now Bob has Alice's public key, and he can go ahead and decode 0:39:11.545 this message, he can go ahead and verify this $0: 39: 14.745$ message that Alice tried to send to him. 0:39:17.581 So, in this, we call this Charles here, 0:39:20.345 sometimes it is called a CA, a certificate authority. 0:39:25 0:39:32 And the idea is that these CAs, a small number of CAs can 0:39:35.547 service a very large number of users. 0:39:37.828 So rather than having to have every user exchange keys with 0:39:41.502 every other user, each user just exchanges keys 0:39:44.416 with a few certificate authorities. 0:39:46.57 And then, those certificate authorities, sort of act like 0:39:50.117 these hubs that propagate keys out into the rest of the users. 0:39:53.981 This is a very simple way in which you might be able to 0:39:57.402 disseminate a public key. We will talk a little bit later 0:40:02.303 on about sort of a more formal way of reasoning about how 0:40:06.464 public keys are disseminated and how these kinds of webs of trust $0: 40: 11.22$ are built up, but this is just a simple way $0: 40: 14.341$ to sort of start thinking about how public keys might be 0:40:18.428 disseminated automatically over the Internet. 0:40:21.698 What I want to do now is just briefly turn, 0:40:24.819 with the last few minutes, to this question of how we 0:40:28.683 actually establish a secure communication channel between 0:40:32.845 two parties. This is going to get at our 0:40:37.548 property, the sort of establishing a confidential 0:40:42.08 communication channel. We are going to talk a little 0:40:46.895 bit about how we establish confidentiality. 0:40:50.86 And so the idea is that we want to find some way that we can 0:40:56.43 encrypt the communication between our two parties. 0:41:02 And what we are going to do is first authenticate the user 0:41:10.221 using a technique like this, and then what we are going to 0:41:18.442 do is use public key to authenticate. 0:41:23.634 This is establishing a secure communication channel. 0:41:32 We are going to use public key to authenticate. 0:41:34.923 But what often happens in practice in the Internet is that 0:41:38.546 you use public key to authenticate, 0:41:40.707 and then what you are going to do is use a shared key 0:41:44.012 cryptography protocol to actually encrypt the information 0:41:47.572 that is flowing back and forth between the two parties. 0:41:51.004 And the reason for that is if you sort of looked at, 0:41:54.245 even though I said that these public key methods like RSA, 0:41:57.868 it's easier to exponentiate than it is to factor. 0:42:02 It turns out that exponentiation in RSA is still 0:42:04.396 relatively expensive because exponentiation requires, 0:42:07.048 these keys are very long, they are thousands of bytes 0:42:09.7 long, so you are taking these long messages and taking them to $0: 42: 12.811$ very large powers. Doing that is computationally 0:42:15.208 expensive. You get these very big numbers 0:42:17.248 that computers are not terribly good at handling. 0:42:19.696 And so it has a big impact on performance if you use public 0:42:22.654 key cryptography all the time. Instead, often times what is 0:42:27.184 done is we use public key cryptography to sort of, 0:42:31.008 as I said, bootstrap the process of exchanging a shared 0:42:35.221 key between two servers. That is what we are going to 0:42:39.279 see. We are going to see how we can 0:42:41.932 then exchange a shared key which we can then use to encrypt the 0:42:46.77 communication between two parties. 0:42:49.344 This is a little puzzle for you guys. 0:42:52.154 What I am going to put up now is a broken protocol and see if 0:42:56.835 you can figure out, in the next few minutes, 0:43:00.19 how it is broken. It is not very broken but it is 0:43:04.505 broken in kind of a subtle way. This is a protocol called 0:43:07.224 Denning-Sacco. And when it was originally 0:43:09.167 proposed, the original proposers of it actually got it wrong, 0:43:12.08 too. And they presumably thought $0: 43: 13.586$ about it for a while before they got it wrong. 0:43:15.771 This is meant to be an illustration that designing 0:43:18.151 cryptographic protocols is hard and it needs to be something 0:43:21.016 that you need to think about very carefully. 0:43:23.104 Here is the protocol. Suppose that Alice wants to 0:43:25.435 send a message between Alice and Bob and we have our certificate 0:43:28.494 authority. Alice says to the certificate 0:43:32.226 authority, I would like to do some communication with Bob. 0:43:36.602 And my name is Alice. What Bob sends back is one of $0: 43: 40.44$ these certificates, a signed message that has $0: 43: 43.818$ Alice's public key in it and Bob's public key. 0:43:47.272 We call these signed messages certificates. 0:43:50.496 These come from the certificate authority. 0:43:53.644 And they basically are a way that if Alice trusts the 0:43:57.636 certificate authority she can decode Bob's public key and be 0:44:02.165 reasonably assured that this is, in fact, Bob's public key. 0:44:08 She is also going to get a certificate for herself that she 0:44:11.959 can send to Bob so that Bob doesn't have to go contact the 0:44:15.849 certificate authority again. She is going to send this thing 0:44:19.877 that has been signed the certificate authority which is 0:44:23.563 going to allow Bob to authenticate her. 0:44:26.156 So she does that. What she sends to Bob is her 0:44:30.359 own certificate which is this little thing shown here on the 0:44:35.331 left. And then she also sends to Bob 0:44:38.28 a proposed shared key. This is kAB. 0:44:41.146 And she signs that proposed key with her own private key. 0:44:45.865 When she signs this key with her private key that means that 0:44:50.837 Bob can be assured that this is an authentic message, 0:44:55.219 in fact, from Alice. And then she encrypts it with 0:44:59.874 Bob's public key so that only Bob can be the one who can 0:45:03.43 decode it. So only Bob will actually see 0:45:05.951 the contents, see what this key is. 0:45:08.149 And these Ts that I have shown here are simply timestamps, 0:45:11.834 and I will explain to you why those are important in a minute. 0:45:15.777 We need timestamps that go along with these things. 0:45:19.01 So this proposed kev has been both sianed with her private kev 0:45:22.953 and encrvoted with Bob's public kev.
$0: 45: 25.216$ And now Bob can go ahead and send messages back to Alice. 0:45:30'And he can encrypt those messages using kAB, 0:45:33.049 using a shared key encryption mechanism which, 0:45:36.241 as we said, is more efficient. So these guys can exchange a 0:45:40.354 bunch of information with each other in this way. 0:45:43.758 This is an example of a cryptographic protocol. 0:45:47.021 I said there was a bug. Let's try and debug it a little 0:45:50.851 bit. And, to get at that, 0:45:52.553 let's talk about what some of the properties of cryptographic 0:45:56.808 protocols that we would like. 0:46:00 0:46:05 One property we would like is what is called freshness. 0:46:09.545 What freshness means is that I am reasonably assured that this 0:46:14.68 message is recent. It came from recent history. 0:46:18.552 And this is what we need the timestamps for. $0: 46: 22.171$ We need to make sure that this message is, in fact, $0: 46: 26.38$ a message that is relatively new. $0: 46: 30$ It is not an old message that I generated before that is now $0: 46: 34.214$ being sent back to me again. That is what we are going to 0:46:38.214 use the timestamps here for. We also want to make sure that 0:46:42.357 the message is appropriate. And, by appropriate, 0:46:45.714 I am actually the intended recipient of this message and 0:46:49.642 the sender of this message is actually who the sender of this 0:46:53.928 message claimed to be. This message actually should be 0:46:57.714 applied right now. This message makes sense. 0:47:01.87 And then, finally, the third property we want is 0:47:05.386 something called forward secrecy. 0:47:07.78 What this says is essentially we should be able to change the 0:47:12.269 cryptographic keys that we are using at some point in the 0:47:16.458 future. Say, for example, 0:47:18.254 if our keys become compromised, we should be able to change the 0:47:22.892 keys and our method should continue to work. 0:47:26.109 This approach is pretty clearly true. 0:47:30 Alice could request a new key. And then you could imagine some 0:47:33.297 way in which Alice could create a new key and send that new key 0:47:36.648 to Bob and we can sort of start all over again. 0:47:39.135 The two properties that are really interesting are this 0:47:42.054 freshness property and this appropriateness property, 0:47:44.864 and they are the two properties that I want to talk about a 0:47:48 little bit more. And if you think about what the 0:47:50.54 kinds of attacks are that somebody could apply on this 0:47:53.405 thing, well, one attack they could apply would be an attack 0:47:56.54 on the sort of cryptographic transform itself. 0:48:00 A brute force attack where you try and factor the keys, 0:48:03.936 we said that is hard. Another attack that they could 0:48:07.653 apply would be a so-called replay attack. 0:48:10.569 There is a crypto attack and so-called replay attack. 0:48:14.359 This is that somebody might sort of reuse a message that 0:48:18.369 they saw transmitted over the network before. 0:48:21.576 Some Eve or Lucifer might overhear a message and then 0:48:25.366 might try and resend that message in order to get the 0:48:29.157 server to do something. Suppose there is a message that 0:48:33.501 tells the server to take some action in the outside world, 0:48:36.262 open a door, so you might save up a message 0:48:38.297 that somebody else had sent before that said open the door. 0:48:41.107 And then you might resend it in order to get the door open when 0:48:44.11 you wanted it to open. We want to prevent that. 0:48:46.339 And we are going to use timestamps to do this. 0:48:48.519 And getting the timestamps to work out is a little bit tricky. 0:48:51.474 If the sender and the receiver have perfectly synchronized 0:48:54.235 clocks, you might just say as long as the timestamp is within 0:48:57.141 the first few milliseconds that is fine. 0:49:00 But if that is not true then you need to do something a 0:49:03.103 little bit more sophisticated. There is a protocol called 0:49:06.321 Kerberos that works this out in detail. 0:49:08.505 And that, again, is described in the notes. 0:49:10.919 But the idea is just you put the timestamp in every message 0:49:14.252 that you send. And then when you sign the 0:49:16.551 message, when the person on the other end decodes that message, 0:49:20.114 they know that this message was generated as of a particular 0:49:23.505 time. But the third kind of attack we 0:49:25.574 might be worried about is a so-called impersonation attack. 0:49:30 And this is the attack that this protocol is susceptible to. 0:49:34.252 Does anybody see what the bug in this protocol is? 0:49:38 0:49:48 STUDENT: Charles does not authenticate that Alice is 0:49:53.186 Alice. Charles does not authenticate? 0:49:58.459 Well, Alice does send this key that says -- 0:50:05 Charles doesn't actually care because all Charles saw was a 0:50:09.252 message that said I want Alice's public key and B's public key. 0:50:13.797 There is nothing wrong with that message getting corrupted. 0:50:18.049 Alice might get something back, but if it comes back it has 0:50:22.302 been signed with Charles' private key and so she will know 0:50:26.48 exactly what it was that was in there. 0:50:30 STUDENT: Only Alice knows Charles private key? 0:50:33 I mean can't someone else impersonate Alice and do that 0:50:36.599 whole process and then be seen as Alice by Bob? 0:50:40 But notice that the key has been signed with Alice's private 0:50:44.719 key. This proposed key has been 0:50:47.119 signed with Alice's private key. STUDENT: Alice is sending 0:50:53.012 something encoded in Charles' private key, is that right? $0: 51: 00$ No. Well, all this means is that $0: 51: 01.737$ the thing that is encoded with Charles' private key, $0: 51: 04.594 \mathrm{Bob}$ is going to be able to decode that thing using Charles' 0:51:07.844 public key. And he is going to have some $0: 51: 10.03$ assurance, in fact, about what Alice's public key $0: 51: 12.719$ is. I think that is OK. $0: 51: 13.952$ Anybody else want to take a guess? $0: 51: 15.801$ OK. Well, since we are out of time, $0: 51: 17.706$ I will talk about this the first thing next time and will 0:51:20.844 show you what the problem with this protocol is. 0:51:23.478 I will see you on Monday. One announcement before you 0:51:27.498 guys go. I have a little gift for you 0:51:29.497 guys which is that we are going to cancel class next Wednesday 0:51:32.883 before the design project is due. $0: 51: 34.659$ So there is no class next Wednesday, but there is class on $0: 51: 37.823$ Monday so make sure you come here.

