

Crease the diagonals


Fold the top edge to the center point, creasing only between the diagonals


Unfold


Repeat on the bottom (fold and unfold)


Turn over, and crease in between the squares in the opposite direction


Final crease pattern
-- - Valley fold
----- Mountain fold


Folding the crease pattern completely forms an "X" shape

Partially opening it forms a hypar

Demaine, Demaine, Lubiw


Courtesy of Jenna Fizel. Used with permission.
[Albers at Bauhaus, 1927-1928] ${ }_{2}$



Courtesy of Erik Demaine, Martin Demaine, Jenna Fizel, and John Ochsendorf. Used with permission.
Virtual Origami Demaine, Demaine, Fizel, Ochsendorf 2006


Virtual Origami
Demaine, Demaine, Fizel, Ochsendorf 2006


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[Demaine, Demaine, Lubiw 1999]

 Fizel, and John Ochsendorf. Used with permission.

Virtual Origami Demaine, Demaine, Fizel, Ochsendorf 2006


Courtesy of Erik Demaine and Martin Demaine. Used with permission.

Peel Gallery, Houston



Demaine \& Demaine 2009


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See also http://erikdemaine.org/curved/Limit/.


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## Waves in Glass

## Erik Demaine Martin Demaine


communication between glass \& paper


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[Demaine, Demaine, Hart, Price, Tachi 2009/2010]


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[Demaine, Demaine, Hart, Price, Tachi 2009/2010]

[Demaine, Demaine, Hart, Price, Tachi 2009/2010]

[Demaine, Demaine, Hart, Price,

Tachi 2009/2010]
Courtesy of Erik D. Demaine, Martin L. Demaine, Vi Hart, Gregory N. Price, and Tomohiro Tachi. Used with permission.

| digits of precision | 16 | 32 | 64 | 128 | 256 | 512 | 1024 | 2048 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $n$ for $\theta=1^{\circ}$ alt. | 3 | 6 | 12 | 24 | 43 | 79 | $\geq 100$ |  |
| $n$ for $\theta=45^{\circ}$ alt. | 3 | 5 | 10 | 18 | 32 | 58 | $\geq 100$ |  |
| $n$ for $\theta=76^{\circ}$ alt. | 2 | 5 | 9 | 16 | 29 | 53 | 95 | $\geq 100_{16}$ |



Courtesy of Erik D. Demaine, Martin L. Demaine, Vi Hart, Gregory N. Price, and Tomohiro Tachi. Used with permission.
[Demaine, Demaine, Hart, Price, Tachi 2009/2010]


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N. Price, and Tomohiro Tachi. Used with permission.

| $\theta=$ | $2^{\circ}$ | $4^{\circ}$ | $6^{\circ}$ | $8^{\circ}$ | $10^{\circ}$ | $12^{\circ}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $n \leq$ | 133 | 67 | 45 | 33 | 27 | 23 |
| $\theta=$ | $18^{\circ}$ | $20^{\circ}$ | $22^{\circ}$ | $24^{\circ}$ | $26^{\circ}$ | $\ldots$ |
|  | $34^{\circ}$ |  |  |  |  |  |
| $n \leq$ | 15 | 13 | 13 | 11 |  | 9 |

[Demaine, Demaine, Hart, Price, Tachi

| $\theta$ | $=$ | $36^{\circ}$ | $\ldots$. | $46^{\circ}$ | $48^{\circ}$ | $\ldots$ | $72^{\circ}$ | $74^{\circ}$ | $\ldots$ | $178^{\circ}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $n \leq$ | 7 | $\ldots$ | 7 | 5 | $\ldots$ | 5 | 3 | $\ldots$ | 3 |  | 2009/2010]



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[Demaine, Demaine, Hart, Price, Tachi 2009/2010]

[Demaine, Demaine, Hart, Price, Tachi 2009/2010]



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## Huffman Family (May 2010)



## Tessellations

## circles



Courtesy of Erik D. Demaine, Martin L. Demaine, and Duks Koschitz. Used with permission.
design by David Huffman; recreated folding by Demaine, Demaine, Koschitz 2010

## Tessellations

## "Arches"


parabolas \& lines


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## "Hexagonal column with cusps"

(†wo variations)


## circles \& lines



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## "Hexagonal column with cusps"


circles
$\&$ lines

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design by David Huffman; recreated folding by Demaine, Demaine, Koschitz 2010

## "4-lobed cloverleaf"

ellipses
\& lines

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## "One column"

## parabolas <br> \& lines



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## "One column"


parabolas
\& lines


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design by David Huffman; recreated folding by Demaine, Demaine, Koschitz 2010

## Huffman Family (May 2010)



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