# Session 12 (In preparation for Class 12, students are asked to view Lecture 12.)

## Topics for Class 12

**Tensegrities:** dot products, springs, software, sculpture. **Project discussion**.

## **Detailed Description of Class 12**

This class addresses a few topics about rigidity/tensegrity:

- More intuition for the dot-product condition of infinitesimal rigidity.
- Why use springs to construct bars?
- More examples of tensegrity sculpture
- Tomohiro Tachi's Freeform Tensegrity software
- Make your own tensegrity following George Hart's instructions

The focus is then an improvised discussion with everyone about their ideas for projects. We will discuss what's known/been done on specific problems, brainstorm what would be most interesting for a project, etc.

### Topics for Lecture 12

**Rigidity theory:** Infinitesimal rigidity, rigidity matrix.

**Tensegrity theory:** tensegrities, equilibrium stress, duality, polyhedral lifting, Maxwell-Cremona Theorem.

Locked linkages: Carpenter's Rule Theorem.

### **Detailed Description of Lecture 12**

This lecture continues our tour through rigidity theory, introducing two more big ideas: infinitesimal rigidity and tensegrities. Infinitesimal rigidity is a nice way to capture the generic case using linear algebra, and it nicely generalizes (and is efficiently computable) in any dimension. Tensegrities (a term coined by Buckminster Fuller) allow the addition of struts (which prevent compression) and cables (which prevent expansion) in addition to bars (which prevent both—which is what we've mostly been thinking about). A nice special case of tensegrities are "spider webs", which turn out to relate to the algorithmic design of origami tessellations.

Although not obviously related, the rigidity tools we build up allow us to prove the existence of actual folding motions between any two configurations of "chain linkages" (whose graphs are paths or cycles) whose edges aren't allowed to cross. This Carpenter's Rule Theorem (which was essentially my PhD thesis) kicks off our coverage of understanding when linkages can "lock".

6.849 Geometric Folding Algorithms: Linkages, Origami, Polyhedra Fall 2012

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