1.021, 3.021, 10.333, 22.00 : Introduction to Modeling and Simulation : Spring 2012

Part II – Quantum Mechanical Methods : Lecture 11

## A Bit More Solar PV, Some V&V and a Few Concluding Thoughts

Jeffrey C. Grossman



Department of Materials Science and Engineering Massachusetts Institute of Technology

# Part II Topics

- It's a Quantum World: The Theory of Quantum Mechanics
- 2. Quantum Mechanics: Practice Makes Perfect
- **3.** From Many-Body to Single-Particle; Quantum Modeling of Molecules
- **4.** Application of Quantum Modeling of Molecules: Solar Thermal Fuels
- 5. Application of Quantum Modeling of Molecules: Hydrogen Storage
- **6.** From Atoms to Solids
- 7. Quantum Modeling of Solids: Basic Properties
- **8.** Advanced Prop. of Materials: What else can we do?
- 9. Application of Quantum Modeling of Solids: Solar Cells Part I
- **10.** Application of Quantum Modeling of Solids: Solar Cells Part II

I. Some PV, Some V&V and Some Concluding Thoughts

## Outline

- Some more PV
- Verification and Validation
- A few more thoughts

#### **Comparison of PV Technologies**

#### **Best Research-Cell Efficiencies**

#### 



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## Fundamental Processes Involved in Solar Photovoltaics: Electron's View



#### Crystalline Silicon Solar PV (80% of current market)

- Light Absorption
  - Band Gap
  - Band Structure



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- Electron/Hole Transport
  - Electron/Hole Mobilities

$$\sigma = e^2 \tau \int \frac{d\mathbf{k}}{4\pi^3} \left(-\frac{\partial f}{\partial E}\right) \mathbf{v}(\mathbf{k}) \mathbf{v}(\mathbf{k})$$

Amorphous Silicon Solar PV (3% of current market)

- Light Absorption (is actually pretty good)
- Electron-Hole Separation (also not a problem)
- Electron/Hole Transport (Holes are Slow!)
  - Hole Mobilities
  - Hole Traps: from total energy differences (Eneutral-Echarged)

## **Organic Solar PV**

2.0

1.5

1.0

0.5

0.0

250

Egap = Eo

500

750

1000

Light Absorption (need to capture more of the solar spectrum) 2.5 Solar Spectral Irradiance (Wm<sup>-2</sup>nm<sup>-1</sup>) Extraterrestial

Band gap

- **Electron-Hole Separation** 
  - Orbital energies



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1250

1500

1750

2000

 $E_{gap} = I.IE_{o}$ 

2250

2500

Terrestial Global Total Terrestial Direct Normal

P3HT absorption

Poly(3-hexylthiophene) (P3HT):  $E_{g,exp} = 2.1 \text{ eV}$ Low-energy photons are not absorbed!



Egap = 0.55Eo

#### Dye Sensitized Solar PV

Transparent Electrode



#### Gratzel and O'Regan (Nature, 1991)

Made up of 3 active materials:
Dye absorbs light.

- •TiO<sub>2</sub> nanoparticles with very large surface area take electron.
- •Liquid electrolyte delivers new electron from cathode to dye.



#### www.energyer.com

#### Dye Sensitized Solar PV



 Biggest problem is a liquid electrolyte.

 Relative energy levels of TiO2 and dye also key.

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#### Going High Efficiency: Fundamental Limits



As band gap increases, the maximum open circuit voltage increases, but the fraction of the solar spectrum absorbed decreases.

#### Multi-Junction Solar PV

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- Light Absorption
  - Band gaps
- Conductivity Across Interfaces
  - Band gaps, Band structures

## Key Mechanism in Organic Solar PV: Charge Separation at the Interface



Charge separation at this interface is highly efficient\*: --Why?

\* N. S. Sariciftci et al., *Science*, 1992, *258*, 1474 B. Kraabel et al., *JCP*, 1996, 104, 4268 C. J. Brabec. et al, *CPL*, 2001, 340, 232



What is the detailed mechanism for this picture?



#### **Excited State**

Charge separated state: essentially degenerate with bridge state.

Bridge state forms: hybridization of P3HT  $\pi^*$  state and C60 t<sub>1u</sub> state.





#### CNT/P3HT: Metallic CNT

Carbon nanotubes instead of C60? Very little success thus far.\*

 $E_f$  near P3HT  $\pi^*$  state

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- Large charge transfer to the metallic CNT (~0.3 electron)
  - Fermi level just above P3HT HOMO state
- No interface states are formed, so no  $E_f$  pinning
- Small built-in potential (0.06 eV), junction-induced exciton dissociation highly unlikely

CNT/Polymer solar cells unlikely to work well with mixed CNT distribution.

#### Using Computational Quantum Mechanics to Design New Mechanisms



#### **Amorphous Silicon PV: The Slow Holes**





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This type of bond switch can be as bad for hole mobility as dangling bonds.



#### Hole Traps: Dangling Bond vs. Strain



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L.K. Wager and JCG, Phys. Rev. Lett. 101, 265501 (2008).

#### New Microscopic Picture of Holes in a-Si



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# Computational quantum mechanics shows that pressure can mitigate these traps!



## Another Thin-Film PV Example: Hyper-Doped Silicon

Absorptance 1.0 Silicon doped with chalcogen atoms (sulfur, selenium, hyper-doped tellurium) to non-equilibrium 0.8 silicon concentrations. sub-bandgap 0.6 IR absorption Strong optical response at photon energies where silicon is typically 0.4 transparent. silicon 0.2 Promise as a photovoltaic substrate material? wavelength (µm)

l'Ilii

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#### **Evolution of Density of States**



#### Needing to Know Structure and Chemistry



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## Needing to Know Structure and Chemistry



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## Validation

#### How do we know when a simulation is right?

# Example: Rayleigh-Taylor Instability

From Leo P. Kadanoff, "The Good, the Bad, and the Awful Scientific Simulation and Prediction"



# Example: Rayleigh-Taylor Instability

- Idea: occurs anytime a dense, heavy fluid is accelerated into a light fluid or lesser density
- Slight perturbations to plane parallel interfaces are unstable ...fingers grow into sets of interpenetrating fingers
- Observed in weather inversions, salt domes, star nebulae
- How to model this process? Requires solving hydrodynamics equations.

## Example: Rayleigh-**Taylor Instability**

#### The Raleigh Taylor Instability.

Small deviations from perfect surface flatness triggers an instability. The two fluids penetrate into one another. Analysis (dimensional and RG arguments) suggest a penetration distance

 $h = \alpha A q t^2$ 

with A being the Atwoods number (density contrast) and  $\alpha$  being dimensionless---and also Universal (!?).

Computer Simulations V2.9--For Berkeley

Kai Kadau...Berni Alder, "Nanohydrodynamics simulation of 10-5-07 R-T Instability", '04. 1.3-108 particles 16

 $h = \alpha A q t^2$ 

About 15 groups have measured or calculated  $\alpha$ . Their results are important for us (a DOE supported astrophysics group) because the instability occurs on the surface of an exploding star.

Computer Simulations V2.9--For Berkeley

10-5-07

![](_page_26_Figure_10.jpeg)

Fluid Mechanics Simulation of RT instability. "On Validating an Astrophysical Simulation Code". A. C. Calder, et al. Astrophys.J.Supp. 143 201-230 (2002). The value of  $\alpha$  differs from previous picture by a factor of two.

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## Example: Rayleigh-Taylor Instability

![](_page_27_Figure_1.jpeg)

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## Validation and Verification

Verification and validation (V&V) are processes that help to ensure that models and simulations are correct and reliable.

Verification: "Did I build the thing right?" Have the model and simulation been built so that they fully satisfy the developer's intent?

Validation: "Did I build the right thing?" Will the model or simulation be able to adequately support its intended use? Is its fidelity appropriate for that?

# We've learned a lot!

## Some of the key remaining challenges

The electron correlation problem. Only seriously affects a fraction of materials, but that fraction tends to contain interesting physics and technological potential. At this point there is no logical follow-up on LDA/GGA

## Some of the key remaining challenges

The time-scale problem. Short (MD) and long (thermo) is not a problem. Intermediate is a problem. e.g. phase transformations.

# Some of the key remaining challenges

The knowledge problem. To study an engineering property/behavior with atomistic-scale modeling, one needs to understand somewhat what controls that property (in order to include the relevant boundary conditions).

e.g. If a property is controlled by impurities then intrinsic calculations will be irrelevant (Si conductivity).

## Some of the key remaining challenges

The structure problem. Even though the structure-property relation is a key tenet of Materials Science, we have only very limited ability to predict structure (crystal structure, amorphous, microstructure, ...)

#### Theory of Properties: The Multi-Scale Materials View

![](_page_34_Figure_1.jpeg)

#### Theory of Properties: The Multi-Scale Materials View

![](_page_35_Figure_1.jpeg)

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## Computations should not substitute for lack of knowledge

# Computational modeling is very powerful, but **be smart!**

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