Trabecular bone

- · foam-like structure
- · exists at ends of long bones ends have larger surface area than shafts to reduce stress on cartilage at joints; tradecular bare reduces weight
- · also exists in stull, iliac crest (pelvis) forms sandwith structure reducent.
- · also makes up core of vertebrae
- · trabecular bone of interest (1) asteo porosis (2) asteo artistis (3) joint replacement

Osteo parosis

- · bone mass de creases with age; osteo parosis extreme bone loss
- · Most common fractures : hip (proximal femu) Verlebrae
- . at both sites, most of load carried by tradecular bone
- · hip fractures especially serious: 40% of elderly patients (>65ysold) die within a year (often due to loss of mobility -> prenmonia)
- · 300,000 hip fractures/yr in us
- · costs \$ 12 billion in 2005

Trabecular bone



Gibson, L. J., and M. F. Ashby. *Cellular Solids: Structure and Properties*. 2nd ed. Cambridge University Press, © 1997. Figures courtesy of Lorna Gibson and Cambridge University Press.

2

Osteo arthritis

- · degradation of cartilage at joints
- · stress on cartilage affected by moduli of underlying bone
- · cortical bone shell can be thin (e.g. <1 mm)
- · Mechanical properties of tradecular bone can affect stress distribution

on cartilage

Joint replacements

- · if osteoarthritis bad + significant damage to cartilage, may require joint replacement
- · Cut end of bone off + Insert stem of metal replacement into hollow of long section of bone
- · metals used: titanium, cobalt chromium, stainless skel
- · bone grows in response to loads anit trab. bone: density depends an magnitude of or orientation " " direction of principal stresses

- Mismatch in moduli between metal + bone leads to stress shielding E(GRa)
 Co 28CI · Mo
 Zio
 Co + 18
 Ti alloys
 Tio
 Trab. bom
 O.01-2
- after joint replacement, remodelling of remaining bone affected
 - stiffer metal carries more of load, remaining bone carries less
 - bone may result can lead to loosening of posthesis
 - can cause problems after ~ 15 yrs.
 - reason surgeons don't like to to joint replacements on younserpatients

Structure of trabecular bone

- · resembles foam : "trabecula" = little team (latin)
- · relative density typically 0.05-0.50
- lou density trab. bare like open cell foam
- · higher density becomes like perforated plates
- · can be highly anisotropiz, depending on strew field.

Trabecular Bone Structure

Images removed due to copyright restrictions.

Lumbar spine 11% dense 42 year old male Femoral head 26% dense 37 year old male Lumbar spine 6% dense 59 year old male

Ralph Muller, ETH Zurich Micro-CT images

Trabecular Bone Structure



Femoral head

Femoral head

Femoral condyle (knee)

Source: Gibson. L. J. "The Mecahnical Behaviour of Cancellous Bone." *Journal of Biomechanics* 18 (1985): 317-28. Courtesy of Elsevier. Used with permission.

Bone grows in response to loads

- Studies on juvenile guinea foul (Ponzer et al. 2006)
 (c) running on level treadmill
 (b) " "inclined " (201)
 (c) control no running.
- · Measured thee flexion angle at max force on treadmill
- · after ~ 6 uts, sacrificed birds + measured orientation of peak trade cular density (OPTO)
- · Ence flexion angle changed by 13.7° with include vs. level treadmill
- · OPTD " " 13.6 " "
- · orientation of trabeaula changed to match orientation of loading
- · video: Concord Freiz station (Science Friday)

Trabecular architecture and mechanical loading

Figure removed due to copyright restrictions. See Figure 1: Pontzer, H., et al. "Trabecular Bone in the Bird Knee Responds with High Sensitivity to Changes in Load Orientation." *The Journal of Experimental Biology* 209 (2006): 57-65.

Trabecular architecture and mechanical loading

Figure removed due to copyright restrictions. See Figure 7: Pontzer, H., et al. "Trabecular Bone in the Bird Knee Responds with High Sensitivity to Changes in Load Orientation." *The Journal of Experimental Biology* 209 (2006): 57-65.

Video: "Studying Locomotion With Rat Treadmills, Wind Tunnels." March 9, 2012. Science Friday. Accessed November 12, 2014.

Properties of solid in trabeculae

- · foam models: require ps, Es ous for the solid
- · ultrasonic wave propagation Es= 15-18 GPa
- · finite element models of exact trabecular architectures from micro CT scans If do uniaxial compression test - can measure Ex + back calculate Es Es = 18 GPa
- · find properties of trabeculae (solid) similar to contical bone
 - $P_s = 1800 \text{ kg/m}^3$ $E_s = 18 \text{ GPa}$ $\delta_{ys} = 182 \text{ MPa} (comp)$ $\delta_{ys} = 115 \text{ MPa} (tension)$

Mechanical Properties of Trabecular Bone

- · compressive stress-strain curve characteristic shape
- · Mechanisms of Leformation + failure
 - usually bending followed by melastic buckling
 - Sometimes, if trabeculae are aligned or very dask: axial deta
 - observations by defermation stage in MCT; also FEA modelling
- · lensile o- E cur: failure at smaller strains; traballer micro cracting
- · data for $E^* \sigma_c^* \sigma_T^*$ (normalized by values for cortical bone) · Spread is large - anisotropy, alignment of tradicular orientation + bading direction, Variations in solid properties, é, species · models - based on open-cell focus comp. $E^* | E_s \propto (p^* / p_s)^2$ bendins data generally consistent $r_{el}^* | E_s \propto (p^* / p_s)^2$ bendins Lith models $r_{el}^* | E_s \propto (p^* / p_s)^2$ bending Lith models also: statistical analysis of data kension $\sigma_T^* | \sigma_{qs} \propto (p^* / p_s)^{3/2}$ plastic hinges E^* , $\sigma_c^* \propto p^2$ note: comp: $E_{el}^* = constant = 0.7\%$

Compressive stress-strain curves

Figure removed due to copyright restrictions. See Fig. 1: Hayes, W. C., and D. R. Carter. "Postyield Behavior of Subchondral Trabecular Bone." *Journal of Biomedical Materials Research* 10, no. 4 (1976): 537-44.

Compression Whale Vertebra

Images removed due to copyright restrictions. See Figure 5: Müller, R. S. C. Gerber, and W. C. Hayes. "Micro-compression: A Novel Technique for the Non-destructive Assessment of Bone Failure." *Technology and Health Care* 6 (1998): 433-44.

Muller et al, 1998



Nazarian and Muller 2004

Source: Narzarian, A., and R. Müller. "Time-lapsed Microstructural Imaging of Bone Failure Behavior." *Journal of Biomechanics* 37 (2000): 1575-83. Courtesy of Elsevier. Used with permission.

Images removed due to copyright restrictions.

Human Vertebral Bone

Mueller, ETH

Tension

Figure removed due to copyright restrictions. See Fig. 5.6: Gibson, L. J., et al. *Cellular Materials in Nature and Medicine*. Cambridge University Press, 2010.

Carter et al., 1980



Gibson, L. J., M. Ashby, et al. *Cellular Materials in Nature and Medicine*. Cambridge University Press, © 2010. Figures courtesy of Lorna Gibson and Cambridge University Press.



Gibson, L. J., M. Ashby, et al. *Cellular Materials in Nature and Medicine*. Cambridge University Press, © 2010. Figure courtesy of Lorna Gibson and Cambridge University Press.

- in some regions, trab. may be aligned e.g. parallel plates
 deformation then axial E* ap (in longitudinal direction) 0* ap
- · Can also summarize data for solid tradeculae + tradecular bone (similar to wood) solid - composite of hydroxy apatite + collagen

Osteo porosis (Latin "porons bones"

- · as age, lose brue mass
- · bone mass peaks at 25 yrs, then decreases 1-2%/yr.
- · women, menopause cessation of estrogen production, increases rate of boxe loss
- · Osteo purosis defined as bone mass 2.5 standard deviations (or more) below young normal mean

· tradeculae thin of then resord completely

Aligned Trabeculae



Femoral Condyle (Knee)

Source: Gibson. L. J. "The Mecahnical Behaviour of Cancellous Bone." *Journal of Biomechanics* 18 (1985): 317-28. Courtesy of Elsevier. Used with permission.



Gibson, L. J., M. Ashby, et al. *Cellular Materials in Nature and Medicine*. Cambridge University Press, © 2010. Figures courtesy of Lorna Gibson and Cambridge University Press.



Gibson, L. J., M. Ashby, et al. *Cellular Materials in Nature and Medicine*. Cambridge University Press, © 2010. Figure courtesy of Lorna Gibson and Cambridge University Press.

Osteoporosis

Figure removed due to copyright restrictions. See Figure 1: Vajjhala, S., A. M. Kraynik, et al. "A Cellular Solid Model for Modulus Reduction due to Resorption of Trabecular Bone." *Journal of Biomechanical Engineering* 122, no. 5 (2000): 511–15.

- · as tradecular thin buckling easier of a (elps)2
- · once trabeculae begin to resorb, connectivity reduced, strength drops
- · Modelling
 - · can't use unit cell or dimensional analysis (need to midel local effects)

Clamatically

Size

- · finite element modelling
- Initially 2D Voronoi honey comb
 20 representation of vertebral bone] Matt Silva
 3D Voronoi form Surekha Vajjbala

Voronoi honey camb

- · random seed points, draw perpendicular disectors
- · use a ninimum separation distance to get cells of approximately uniform
- · FE analysis each tradicala a dean element
- . first calculated elastic moduli
 - · FEA results close to analytical model for random (isotropic) honeycomb (40 models, all some p*1ps, about 25x25 cells in each)
 - . modulus is average of stiffness over entire material

Modelling: 2D Voronoi



Source: Silva, M. J., L. J. Gibston, et al. "The Effects of Non-periodic Microstructure on the Elastic Properties of Two-dimensional Cellular Solids." *International Journal of Mechanical Sciences* 37 (1995): 1161-77. Courtesy of Elsevier. Used with permission.



Source: Silva, M. J., L. J. Gibston, et al. "The Effects of Non-periodic Microstructure on the Elastic Properties of Two-dimensional Cellular Solids." *International Journal of Mechanical Sciences* 37 (1995): 1161-77. Courtesy of Elsevier. Used with permission.

- · Next, calculated compressive strength of Voronoi honey combs
- · each cell wall 1-3 bean elements
- · Model non-linear elasticity + failure behaviour
- · 15 × 15 cells in model (random seeds ~ isotropic)
- · cell wall assumed to be elastic perfectly plastic Tys/E, = 0.01 H= 0.3
- · for this value of GalEs, transition between elastic buckling + plastic collapse stress at p*1/1,= 0.035 in regular Lere. honey camb
- calculated compressive strength of honeycombs with p= 0.015, 0.035,
- · generated 5 different Voronoi honey combs at each p*ps
- · compressive J-E behaviow:

p*/2 > 0.05 - Stain softening, permanent det= on unloading - plastic hinge formation, cell collapse in narrow localized bands p*/2 < 0.035 - non-linear elastic deformation - recoverable strength: 0.6 to 0.8 of 0 periodic

0.05 \$ 0.15



Source: Silva, M. J., and L. J. Gibson. "The Effects of Non-periodic Microstructure and Defects on the Compressive Strength of Two-dimensional Cellular Solids." *International Journal of Mechanical Sciences* 39 (1997b): 549-63. Courtesy of Elsevier. Used with permission.



Silva et al, 1997

Source: Silva, M. J., and L. J. Gibson. "The Effects of Non-periodic Microstructure and Defects on the Compressive Strength of Two-dimensional Cellular Solids." *International Journal of Mechanical Sciences* 39 (1997b): 549-63. Courtesy of Elsevier. Used with permission.



Source: Silva, M. J., and L. J. Gibson. "The Effects of Non-periodic Microstructure and Defects on the Compressive Strength of Two-dimensional Cellular Solids." *International Journal of Mechanical Sciences* 39 (1997b): 549-63. Courtesy of Elsevier. Used with permission.

- · max. normal strams at nodes in honeycombs (linear elastic)
 - · Voronoi honey combs hormal distribution
 - regular hexagonal honeycambs dashed lines an plot
 - normal strain in vertical cell walls in regular Lex. hovey camb = mean normal strain in Voronoi
 oblique walls bending larger strains
 - · Voranai heney comb 5% of strains outside of range of strain in regular here. honey comb
 - · decrease in strength associated with broader range of strains in Voronoi horey cambs
 - minimum strengthe pt/2 = 0.05
 - · interaction between elastic buckling + plastic yield

plashiz you ld slenderness ratio,

 $\delta_{cf} = \frac{\pi^2 \varepsilon \Gamma}{l^2} = \frac{\pi^2 \varepsilon \pi r^4}{4l^2 \pi r^2} = \frac{\pi^2}{4} \varepsilon \left(\frac{r}{l}\right)^2$

Figure removed due to copyright restrictions. See Figure 5; Silva, M. J., and L. J. Gibson. "The Effects of Non-periodic Microstructure and Defects on the Compressive Strength of Two-dimensional Cellular Solids." *International Journal Mechanical Sciences* 39, no. 5 (1997): 549-63.

Voronoi honeycambs - defects

- · randomly removed cell walls in both Voronoi + reg. here. honeycambs
- analyzed both by FEA
- · dramatic decrease in modulus + strength, compared with equivalent reduction in density by thinning of cell walls
- · p*1ps = 0.15 failure by yie lding
- · p* 1ps = 0.015 " " elastiz buckling
- · Modulus + strength reduction similar for Voronoi + reg. here. honeycombs
- · percolation threshold for 2D network heregonal cells = 35% strute removed

Verlebral tradeaular ban-20 model

- · model adapted to represent tradecular more aligned in vertical + horizontal directions
- · perturbed a squake array of struts to get similar orientation of struts asm
- · looked at reduction in number + thickness of longitudinal + transverse struts (independently)



Source: Silva, M. J., and L. J. Gibson. "The Effects of Non-periodic Microstructure and Defects on the Compressive Strength of Two-dimensional Cellular Solids." *International Journal of Mechanical Sciences* 39 (1997b): 549-63. Courtesy of Elsevier. Used with permission.

Figure removed due to copyright restrictions. See Figure 2: Vajjhala, S., A. M. Kraynik, et al. "A Cellular Solid Model for Modulus Reduction due to Resorption of Trabecular Bone." *Journal of Biomechanical Engineering* 122, no. 5 (2000): 511–15.

Vajjhala et al, 2000



Source: Silva, M. J., and L. J. Gibson. "Modelling the Mechancial Behavior of Vertebral Trabecular Bone: Effects of Age-related Changes in Microstructure." *Bone* 21 (1997a): 191-99. Courtesy of Elsevier. Used with permission.

Figure removed due to copyright restrictions. See Figure 3: Silva, M. J., and L. J. Gibson. "Modelling the Mechancial Behavior of Vertebral Trabecular Bone: Effects of Age-related Changes in Microstructure." *Bone* 21 (1997): 191-99.

Figure removed due to copyright restrictions. See Figure 4: Silva, M. J., and L. J. Gibson. "Modelling the Mechancial Behavior of Vertebral Trabecular Bone: Effects of Age-related Changes in Microstructure." *Bone* 21 (1997): 191-99.

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Source: Silva, M. J., and L. J. Gibson. "Modelling the Mechancial Behavior of Vertebral Trabecular Bone: Effects of Age-related Changes in Microstructure." *Bone* 21 (1997a): 191-99. Courtesy of Elsevier. Used with permission.

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Source: Silva, M. J., and L. J. Gibson. "Modelling the Mechancial Behavior of Vertebral Trabecular Bone: Effects of Age-related Changes in Microstructure." *Bone* 21 (1997a): 191-99. Courtesy of Elsevier. Used with permission.

3D Voronai Model

- · same analysis, now with 3D Voronoi Model
- · periodic 3×3×3 cells, p*/ps=0.1
- · Used beam elements, FEA, linear elastic only
- · percolation threshold ~ Sol. strub removed
- · Comparison of 20+30 results for modulus: in 30, modulus reduction more
- · also for 20+30 modulus reduction similar for regular + Vloronoi structures

3D Voronoi Model

Figure removed due to copyright restrictions. See Figure 6: Vajjhala, S., A. M. Kraynik, et al. "A Cellular Solid Model for Modulus Reduction due to Resorption of Trabecular Bone." *Journal of Biomechanical Engineering* 122, no. 5 (2000): 511–15.

Vajjhala et al, 2000

3D Voronoi Model

Figure removed due to copyright restrictions. See Figure 7: Vajjhala, S., A. M. Kraynik, et al. "A Cellular Solid Model for Modulus Reduction due to Resorption of Trabecular Bone." *Journal of Biomechanical Engineering* 122, no. 5 (2000): 511–15.

Vajjhala et al, 2000

Metal toans as bone substitute materials

- · metals used oin orthopaedic implants leg. hip, buil
- · Co-Cr, Ti, Ta stainless steel alloys
- · biocompatible, corrosian resistant
- . but moduli of metals > modulus of bom
- e.g. E_{Ti} = 110 GPa E_{contral} = 18 GPa E_{trab.bone} = 0.01 2 GPa · Stress shielding can lead to Done resorption.
- · to improve mechanical interaction between implant + bone
- porous sintered metal boads used to coat implants promote bore mgrowth
 also, wire mesh coatings have been developed, primarily for flat implant
 recently, interest in using metal forms as coatings
 longer term, interest in using in replacement Vertebral bodies
 Variety of processes for making metal form implant coatings

Metal Foams: Microstructure

Ta, replicating PU foam with CVD

Ti, replication of PU foam by slurry infiltration and sintering

Ti, fugitive phase

Ti, foaming agent

Ti, expansion of Ar gas

Images removed due to copyright restrictions. See Figure 8.1: Gibson, L. J., M. Ashby, and B. A. Harley. *Cellular Materials in Nature and Medicine*. Cambridge University Press, 2010. http://books.google.com/books?id=AKxiS4AKpyEC&pg=PA228

Ti, freeze-casting (freeze-drying)

Ti, selective laser sintering

Image sources given in Cellular Materials in Nature and Medicine Ni-Ti, high temperature synthesis (powders mixed, pressed and ignited by, for example, tungsten coil heated by electrical current)

(4)

Processing

(a) replicate open cell polymethane form

- · pyrolize ph foan -> 2% dense vitreous carbon
- · coat with Ta by CVD => struts 99%. Ta, 1%. c
- · cell size 400-600 pm; cocting thickness 40-60 pm p*1ps = 0.15-0.25
- · "Trabecular metal" (Zimmer) trade name.
- . Ta forms surface oxide Ta os does not band to bare
- · but, if treat with diluke NaOH, then heat to 300°C + cool, then Submerge in simulated body fluid (ion conc. matches human blood plasmo) => get apatite coating # on form struts, which bands to bare
- (b) infiltrate slurry of titanium hydride into open cell foam
 - · heat treat to decompose Tittz
 - · sinter remaining Ti (also removes mitial form)

(c) fugitive phase methods

- · Mix Tiz powder + fugitive phase powder
- · heat to T, (~200°c) to decompose filler, then to Tz (1200°c) to sinte Ti powder

Metal Foams: Processing



EXPANSION OF A FOAMING AGENT



Foaming agent evolves gas at temperature at which polymer is liquid

FREEZE-CASTING



RAPID PROTOTYPING



Gibson, L. J., M. Ashby, et al. *Cellular Materials in Nature and Medicine*. Cambridge University Press, © 2010. Figures courtesy of Lorna Gibson and Cambridge University Press.

Processes

- (d) expansion of foaming agent
- (e) freeze casting (freeze styring)
- (P) rapid prototyping (3D Printing, selective laser sintering)
- J-E curves similar to other forms
- date for Ex, or

Ti Foam: Stress-strain



Source: Wen, C. E., M. Mabuchi, et al. "Processing of Biocompatible Porous Ti and Mg." *Scripta Materialia* 45 (2001): 1147-53. Courtesy of Elsevier. Used with permission.



Gibson, L. J., M. Ashby, et al. *Cellular Materials in Nature and Medicine*. Cambridge University Press, © 2010. Figures courtesy of Lorna Gibson and Cambridge University Press.

Bone in Evolutionary Studies

Bone structure in evolutionary studies

- · phylogenetic chart big picture structural biomaterials (mineralized)
- · sponges first multicelled animal
 - · calcarca: Ca (03 spicules (needles)
 - · hexachinellida: Sioz "glass sponges"
 - demospongiae: most sponges some have Sioz spicules - spongin (type of collagen)
- · cnidarians eq. colals, jellyfish
 - · covals CaCoz
- · Mollusca bivelves, shails, octopus
 - · If Mineralized Galoz
- · arthropods eq. hexapoda (insects), arachnide (spidus), crustacears (shring,

(obster)

- · Oxoskeleton of insects + spides: chitin
- · crusticeans: chitin may be mineralized with Ca Coz

Vertebrates

cyclostomata - jauless fish - lampreys hagfish
- no verkebra - notochord
- no bone
Chondrichthy es - Sharks, rays, skales
- Carfilagenous skeletan - some mineralization, but not the ban
· actino ptery gii - ray finned fish
- true bone
- 450 million yens ago (MYA)

Bone structure + loading

- · bone grows in response to loading
- bone structure reflects mechanical loading + function e.g. quadruped us projed
- . evolutionary studies have looked at tradecular Done architecture + density.



Fig. 2 A timetree of metazoan phyla. Divergence times are shown in Table 1. *Abbreviations*: Cz (Cenozoic), Mp (Mesoproterozoic), and Mz (Mesozoic).

Hedges and Kumar, 2009

From: *The Timetree of Life.* Hedges, S. B., and S. Kumar (eds.) © 2009 Oxford University Press. All rights reserved. This content is excluded from our Creative Commons license. For more information, see http://ocw.mit.edu/help/faq-fair-use/.



Venus Flower Basket (*Euplectella aspergillum*)

- Hierarchical structure
- Remarkably stiff, tough
- Joanna Aizenberg (Harvard)
- Aizenberg et al (2004) Biological glass fibers: correlation between optical and structural properties. PNAS



Fig. 2 A timetree of vertebrates. Times of divergence are averages of estimates from different studies listed in Table 1. Abbreviations: C (Carboniferous), Cm (Cambrian), CZ (Cenozoic), D (Devonian), J (Jurassic), K (Cretaceous), Np (Neoproterozoic), O (Ordovician), P (Permian), Pg (Paleogene), PR (Proterozoic), S (Silurian), and Tr (Triassic).

Common ancestor of all boned vertebrates roughly 450 MYA



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Trabeaular bone studies in human evolution

Oreopithecus bambalii (Rook et al, 1999)

- ·7-9 MYA late Miocene hominid, found in Italy
- · quadruped or biped?
- · compared tradecular architecture in ilium in apes, O. Dambolii, hu mans
- · only had 2 fragments of ilin left + right
- · took radiographs of both + digitally reconstructed a single ilium

Comparisons

- (a) posterosuperior margin marginal handles thicker than apro
- (b) anterio superior margin iib bundle relatively structured compared to apes
- (c) anteriorinterior margin well developed a i spine not seen in apos
- (d) supra acetadoular area high density region
- · Collectively, observations suggest 0. bambolii trab. architecture in ilium More smillar to humans than apos
- · suggests habitual bipedal locomotion (humans obligatory bipeds)

Oreopithecus bambolii: Ilium

Rook et al. (1999)



Image is in the public domain. Source: Wikimedia Commons.

http://en.wikipedia.org/wiki/Iliac_crest

Trabecular architecture: Ilium

Figure removed due to copyright restrictions. See Figure 1: Rook L., et al. "Oreopithecus was a Bipedal Ape after All." *Proceedings of the Natural Academy of Sciences* 96 (1999): 8795-99.

Digitally reconstructed ilium

Figure removed due to copyright restrictions. See Figure 2: Rook L., et al. "Oreopithecus was a Bipedal Ape after All." *Proceedings of the Natural Academy of Sciences 96* (1999): 8795-99.

Comparison of trabecular architecture

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3.054 / 3.36 Cellular Solids: Structure, Properties and Applications Spring 2014

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