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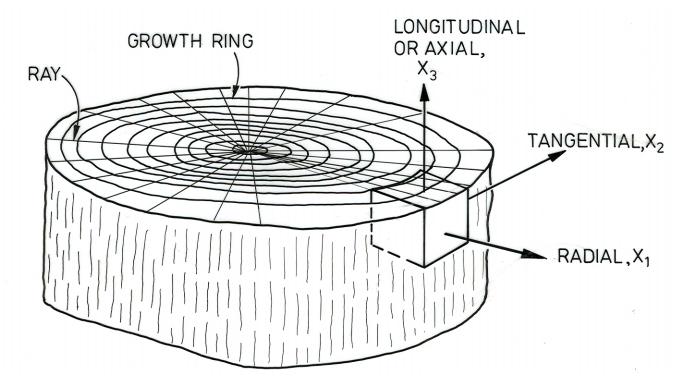
Honeycomb-like materials in nature: wood

- · "materials" derives from Latin "materies, materia" means wood or . trunk of a tree
- · old Irish names of first letters of the alphabet refer to woods
 - A alem = elm B beith = birch C coll = hazel D dair = oak

Vood - structure

- . or the tropiz (if neglect curvature of growth rings)
- · p*(ps ranges from 0.05 (balse) to 0.80 (lignum vitae)
- · trees have cambial layer, beneath bark
- · cell division @ cambial layer · new cells on outer part of cambial layer -> bark · "" " inner " " " " wood

Wood structure



Gibson, L. J., and M. F. Ashby. *Cellular Solids: Structure and Properties*. 2nd ed. Cambridge University Press, © 1997. Figure courtesy of Lorna Gibson and Cambridge University Press.

- living plant cells plasma membrane + protoplast
- · living cells secrete plant cell wall analogous to extra cellular matrix in
- in trees, cells lay down cell wall over a feu weeks, then die animal fissues
- · always retain a cambial layer of cells

Cellular structure : softwoods

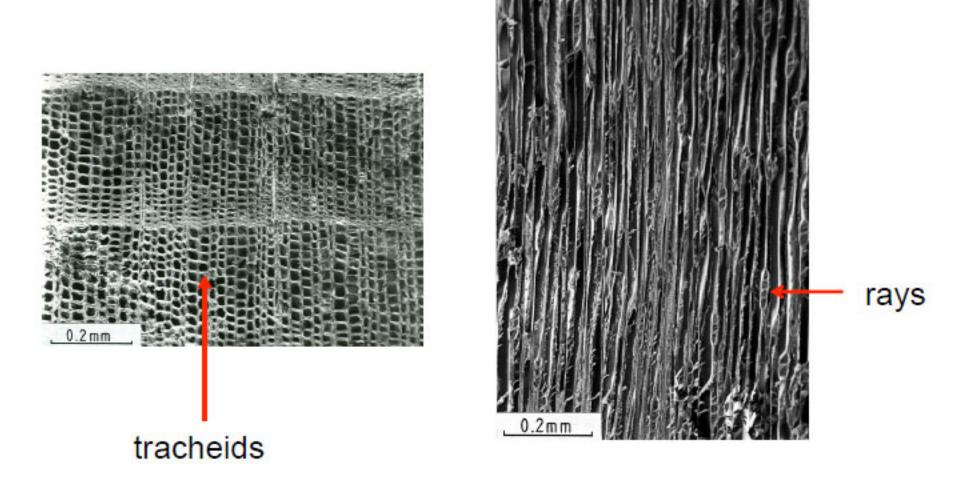
tracheids - bulk of cells (90%), provide structural support
 have holes in cell wall for finid transport (pits)
 ~ 25-7.0 mm long; 22-80 µm across; t=2-7 µm

· rays - radial arrays of smaller parenchyma cells that store sugars

Cellular structure: hardwoods

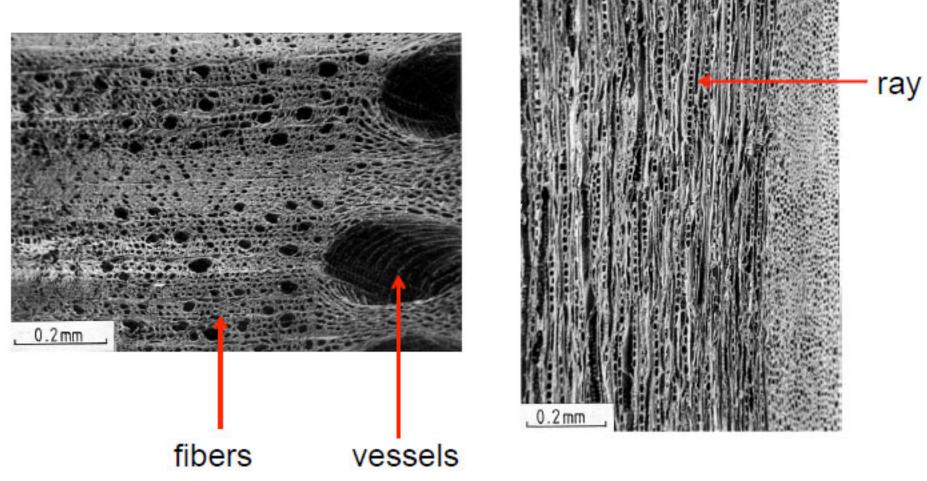
- fibers provide structural support; 35-70% of cells
- · Vessels sap channels conduction of fluids \$6-55% of cells
- · rays store sugars; 10-30% of cells

Softwood: Cedar



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Hardwood: Oak



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Structure: cell wall

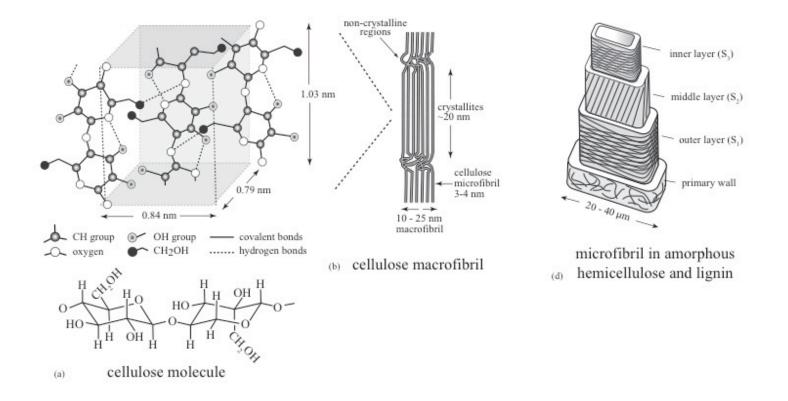
- · fiber reinforced composite
- · cellulose fibers in matrix of lignin/hemicellulose
- · 4 layers, each with fibers at different orientation
- · between 2 cells: middle lamella

Cell wall properties

- · Similar in different species of wood ps = 1500 kg/m³ (Note celluloxe: E ~ 140 GPa
 - EsA = 35 GPa (4 ~ 750 MPa)
 - Est = 10 GPa A = axial direction
 - Gyst = 350 MPa T = transverse direction

5455 = 135 MPa

Wood Structure



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Stress-strain curves

- . J-E curves resemble those for honeycombs
- · mechanisms of deformation most easily identified on low density balsa
- · carves + images for balsa
- · tangential loading: formation of plastic hinges in bent cell walls
- · radial loading: rays act as reinforcing; plastic yielding in cell wells - starts at platens + moves inward
- · axial loading : axial defter of cell halls; then break end caps serrations correspond to each layer of end caps breaking.

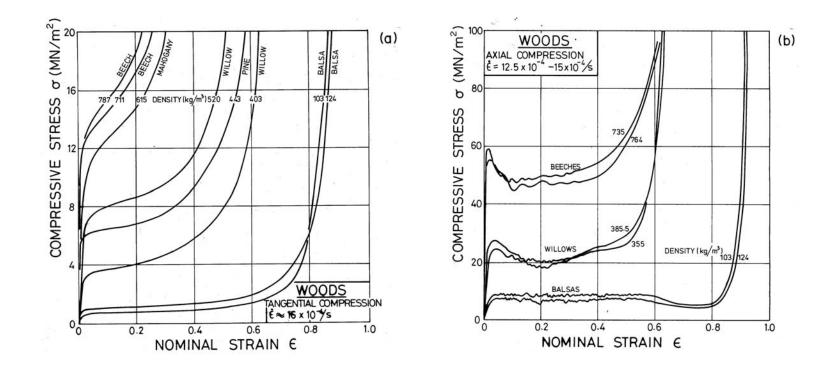
failure by plastic buckling + formation of kink bands also observed

· denser species

Douglas fir - tangential, radial compression

Norvay spince - axial compression

Stress strain curves



Gibson, L. J., and M. F. Ashby. *Cellular Solids: Structure and Properties*. 2nd ed. Cambridge University Press, © 1997. Figure courtesy of Lorna Gibson and Cambridge University Press.

Balsa

Figure removed due to copyright restrictions. See Figure 3: Easterling, K. E., R. Harrysson, et al. "On the Mechanics of Balsa and Other Woods." *Proceedings The Royal of Society. A* 383, no. 1784 (1982): 31-41.

Balsa: Tangential

Figure removed due to copyright restrictions. See Figure 4: Easterling, K. E., R. Harrysson, et al. "On the Mechanics of Balsa and Other Woods." *Proceedings The Royal of Society. A* 383, no. 1784 (1982): 31-41.

Figure removed due to copyright restrictions. See Figure 7: Easterling, K. E., R. Harrysson, et al. "On the Mechanics of Balsa and Other Woods." *Proceedings The Royal of Society. A* 383, no. 1784 (1982): 31-41.

Balsa: Radial

Figure removed due to copyright restrictions. See Figure 5: Easterling, K. E., R. Harrysson, et al. "On the Mechanics of Balsa and Other Woods." *Proceedings The Royal of Society. A* 383, no. 1784 (1982): 31-41.

Balsa: Axial

Figure removed due to copyright restrictions. See Figure 6: Easterling, K. E., R. Harrysson, et al. "On the Mechanics of Balsa and Other Woods." *Proceedings The Royal of Society. A* 383, no. 1784 (1982): 31-41.

Douglas Fir: Tangential Comp

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Douglas fir: Radial comp.

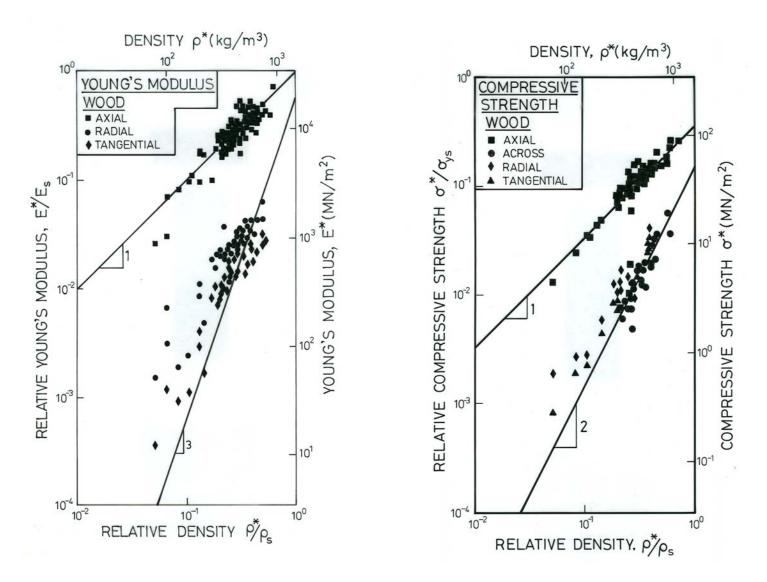
Figure removed due to copyright restrictions. See Bodig, J., and B. A. Jayne. *Mechanics of Wood and Wood Composites*. Van Nostrand Reinhold, 1982.

Norway spruce: Axial comp

Images removed due to copyright restrictions. See Figure 5.14: Dinwoodie, J. M. *Timber: Its Nature and Behaviour.* Van Nostrand Reinhold, 1981.

Modelling wood properties

- · Very simplified model first order
- does not altempt to capture finer details (eg. softwoods us. hardwoods)
- · cell wall has been modelled as fiber composite; it is itself anisotropic
- . We normalize all properties with respect to Es, oys axial
- · constant of proportionality also reflects cell wall anisotropy



Gibson, L. J., and M. F. Ashby. *Cellular Solids: Structure and Properties*. 2nd ed. Cambridge University Press, © 1997. Figure courtesy of Lorna Gibson and Cambridge University Press.

Model for wood microstructure

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Linear elastic moduli
• tangential loading - Model as honeycomb - cell wall bending

$$E_T^* / E_S \propto (p^*/p_s)^3$$

• rays, end caps act to stiffen wood - date lie slightly above $(p/s)^3$
• radial loading - rays act as reinforcing plates + are higher density than the
 $V_E = volume fraction of rays$
 $E_F^* = V_E R^3 E_T^* + (1-V_E) E_T^*$
 $R = (p^*/p_s) rays / (p^*/p_s) fibes = 1.1 to 2$
 $E_E^* slightly larger than E_T^*; \propto (p/p_s)^3$

· axial loading

· axial deformation in cell wall

Et IEs ~ (p*(ps)

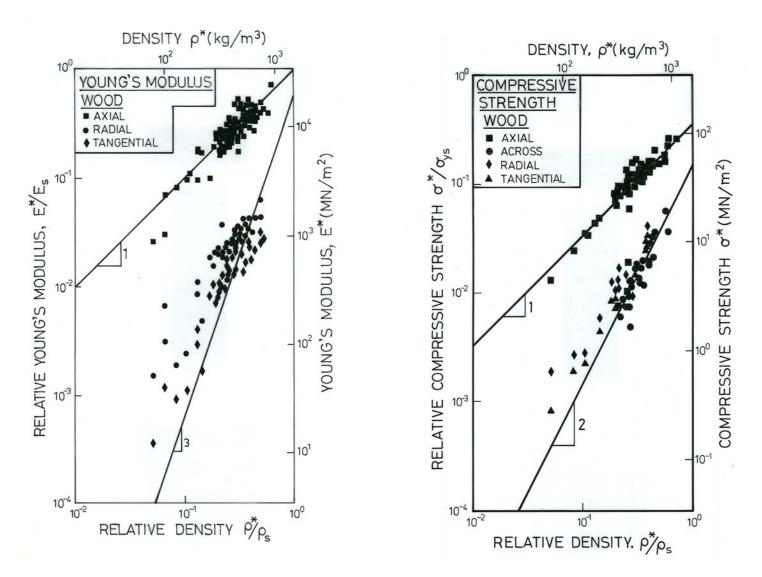
· explains, to first order, · density dependence · anisotropy

Modelling - Poisson's rat	zon	
<u> </u>	Model	
VET = 0.5-0.8	t	constraining effect of rays + end caps
VT2 = 0.2 - 0.6	X	rays + end caps
V RA = 0.02-0.07	0	
$V_{TA}^* = 0.01 - 0.04$	0	
V# = 0.25-0.5	\mathcal{V}_{s}	data close to 0.4 ~ ?s
NAT = 0.35-0.5	Vs	

Modelling - compressive strength

•

7



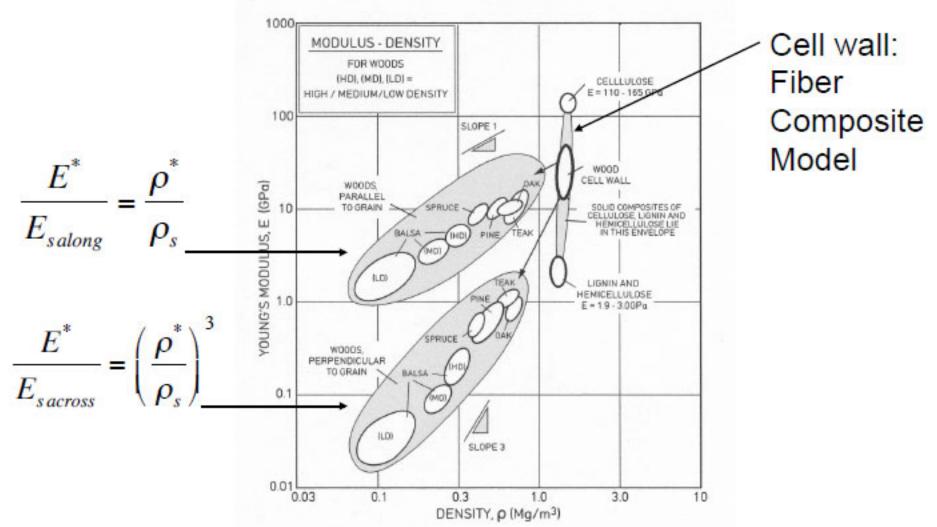
Gibson, L. J., and M. F. Ashby. *Cellular Solids: Structure and Properties*. 2nd ed. Cambridge University Press, © 1997. Figure courtesy of Lorna Gibson and Cambridge University Press.

Modelling: cell wall + cellular structure

- · cell wall can be modelled as a fiber composite cellulose E ~ 140 GPa lignin/hemicellulose E ~ 2GPa composite upper + lower boundo give en velope at right of figure measured values for Es Axial = 35GPa Estranovere = 10 GPa
- · can also show cellular solido model an same plot
- · overall, plot shows how wood hierarchical structure, density variation give wood moduli that vary by a factor of 1000

· Can make similar plot for strength

Wood: Honeycomb Models



Gibson, L. J., and M. F. Ashby. *Cellular Materials in Nature and Medicine.* 2nd ed. Cambridge University Press, © 2010. Figure courtesy of Lorna Gibson and Cambridge University Press.

Wood: Honeycomb Models

Diagram removed due to copyright restrictions. See Figure 5b: Gibson, L. J. "The Hierarchical Structure and Mechanics of Plant Materials." *Journal of the Royal Society Interface* 9 (2012): 2749-66.

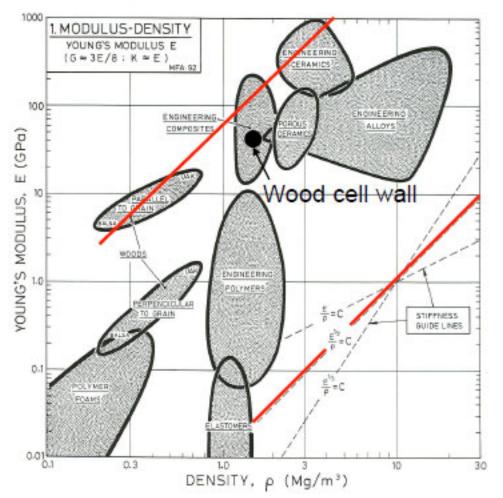
9

Material selection

- for a beam of a given stiffness, P/S, length, L, square cross-section with edge length, t, what material minimizes the massing the beam? $M = \rho t^2 l$ $\delta = \frac{Pl^3}{CEI} = \frac{CEt^4}{\delta^3} = t^2 = \left[\left(\frac{P}{\delta}\right) \frac{l^3}{cE}\right]^{1/2}$ $M = \rho \left[\left(\frac{P}{\delta}\right) \frac{l^3}{cE}\right]^{1/2} l$ to minimize mass, choose material with min. $\rho E^{1/2}$ or maximize $E^{1/2}/\rho$.
- · material selection chart : plot log E vs log p
- · line of constant E'2/p shown in red on plot
- materials with largest values of E"2/p at upper left of plot
- . Woods have similar values of E"21p as engineering composites
- . note that the trunks branches, loaded primarily in bending.
- also note, from models, $\frac{(E^*)^{1/2}}{p^*} = \frac{E_s^{1/2}}{P_s} \cdot \left(\frac{f_s}{p}\right)^{1/2}$

· similarly for strength. In bending

Wood in Bending: E^{1/2}/p

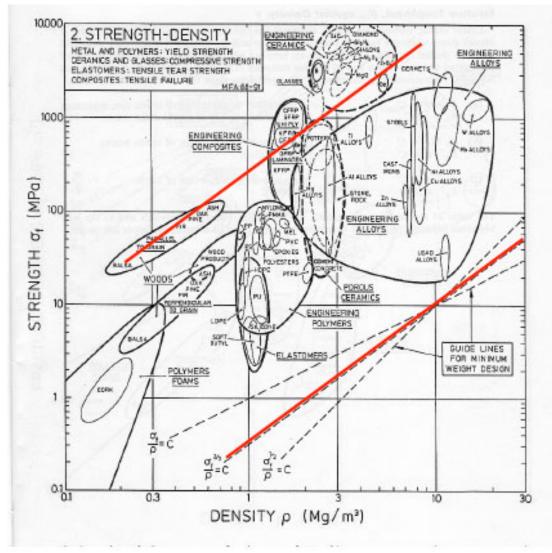


 $\frac{\left(E^{*}\right)^{1/2}}{\rho^{*}} = \frac{\left(E_{s}\right)^{1/2}}{\rho_{s}} \left(\frac{\rho_{s}}{\rho^{*}}\right)^{1/2}$

Stiffness performance index for wood in bending is similar to that for best engineering composites

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Wood in Bending: $\sigma_f^{2/3}/\rho$



$$\frac{\left(\sigma_{f}^{*}\right)^{2/3}}{\rho^{*}} = \frac{\left(\sigma_{ys}\right)^{2/3}}{\rho_{s}} \left(\frac{\rho_{s}}{\rho^{*}}\right)^{1/3}$$

Strength performance index for wood in bending is similar to that for best engng composites

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Wood Use in Design

Historical example: 17th century wooden ships

- · colonial times, importance of navies to colonial powers
- · used particular species for different parts of ship, based on their properties
- · Oak used for much of the hull, ribs, knees, planking = 0 dense wood; still + strong -"straight oak" - straight pieces, cut fran trunk - "Compass oak" - curved pieces fran trunk + branch, so that grain mus along curved, aut piece = > max E, ot - used for knews, wing transon - curved pieces of shiphuli.
- · Eastern white pine British Royal Navy used for Masts, Imported from New - England had run out of tall straight trees for mast England - strategic resource. - ship speed, size depanded an size of mast + sail area
 - Eastern white pine known for straight, tall trunks; Some over 1001 tall

10

- lignum vitae - densest wood; acts as own lubricant

- used in block + tackle

- 14 1759 lost Sseconds in Bidays ctaca - John Harrison's chronometer - Storn of Longitude, Dava Subel

Figure removed due to copyright restrictions. See *The international book of wood*. Bramwell, M, ed. Artists House, 1982. pp 186-87.

Modern example: glue laminated timber

- · glue long pieces of wood, typically 1-2" thick, together
- · select ships to avoid defects (eg. buts)
- · glu-lan has better mechanical properties than sawn lumber.
- · also, can make chrued members by using chrund molds & clamps during bonding process
 - => grain runs along the curve exploits high stiffness + strength of wood => architecturally attractive along the grain

Image of graceful glued-laminated timber arch bridge removed due to copyright restrictions. See Figure 13: *Engineered Wood Products: A Guide for Specifiers, Designers and Users*. Smulski, S., ed. PFS Research Foundation, 1997.

Engineered Wood Products: A Guide for Specifiers, Designers and Users, S. Smulski Ed. PFS Research Foundation, 1997 3.054 / 3.36 Cellular Solids: Structure, Properties and Applications Spring 2014

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