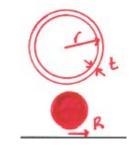
# Lecture 8 Foam Design Notes, 3.054

## Foams: Microstructural Design

- Foam—behavior dominated by cell wall bending
- Foam properties can be increased by increasing EI of cell walls

#### Hollow walls

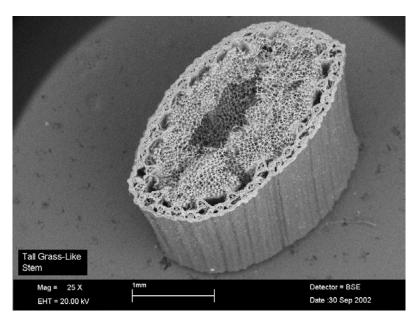


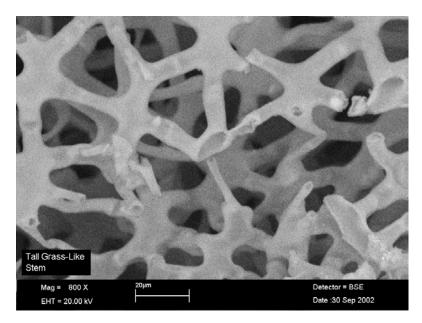
Thin walled tube  $I_t = \pi r^3 t$  Masses equal:  $\pi R^2 = 2\pi r t$ Solid circular section  $I_s = \frac{\pi R^4}{4}$   $R = \sqrt{2rt}$ 

$$\frac{I_t}{I_s} = \frac{4\pi r^3 t}{\pi R^4} = \frac{4r^3 t}{4r^2 t^2} = \frac{r}{t}$$
$$\therefore \quad \frac{E^*_{\text{tube wall}}}{E^*_{\text{solidwall}}} \propto \frac{r}{t}$$

• Can do similar analysis for other properties







## Sandwich cell walls

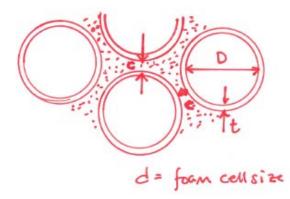
• Sandwich beam — two stiff faces separated by a lightweight core — core typically a honeycomb or foam (or balsa)



I-beam effect - increase in moment of inertia, with little increase in weight

- Faces like flanges of I-beam resist bending
- Core like web of I-beam resist shear
  - Microsandwich foam

#### Microsandwich foam



- Thin walled hollow spheres distributed in a foam
- Have to get geometry right
- Require:

```
Spheres: t \ll D

E_{\text{sphere}} \gg E_{\text{foam}}

V_{\text{f sphere}} \approx 50 - 60\%

Foam: d \ll c
```

## Foams: Microstructural Design

- Another alternative is to use microstructure that induces axial, rather than bending, deformations
- 3D lattice materials: triangulated trusses in 3D — Forces in members all axial; bending negligible
- Various processing methods and geometries possible all triangulated
- Can analyze truss as having pin joints axial forces in members
- Open-cell structures

$$E^* = \frac{\sigma}{\epsilon} \propto \frac{F}{l^2} \frac{l}{\delta} \qquad \delta \propto \frac{Fl}{AE_s} \propto \frac{Fl}{t^2 E_s}$$

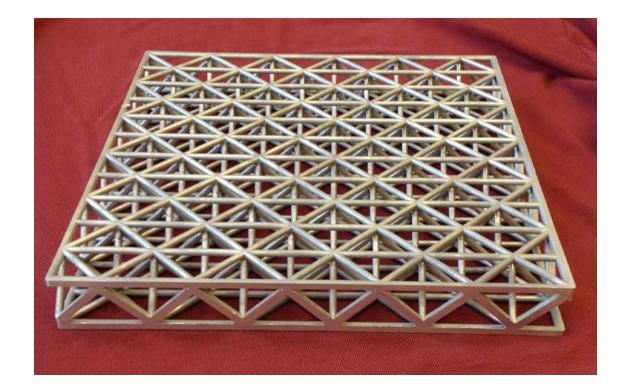
$$E^* \propto \frac{F}{l} \frac{E_s t^2}{Fl} \propto E_s \left(\frac{t}{l}\right)^2 \propto E_s \left(\frac{\rho^*}{\rho_s}\right)$$

$$E^* = C E_s(\rho^*/\rho_s) \qquad C \text{ depends on cell geometry and loading direction}$$

• Strength: if struts fail by *uniaxial yield*:

 $\sigma_{\rm pl}^* = C \, \sigma_{ys}(\rho^*/\rho_s)$ 

But some struts in compression - may buckle (generally do buckle)



#### Compressive strut buckling

- Elastic buckling  $\sigma_{\rm el}^* = C E_s \, (\rho^* / \rho_s)^2$  (like open-cell foam)
- If interaction between elastic buckling and yield use a reduced modulus (tangent modulus)
- Also: Imperfections such as non-straight struts or misaligned struts reduce buckling resistance "knock-down" factor can be significant  $\sim 50\%$

## **Material Selection**

- How to select the best material for same mechanical requirement?
- Section on wood: derived performance index for minimizing mass of a beam of a given stiffness:  $E^{1/2}/\rho$
- Here, discuss material selection more broadly
- Another example: What material minimizes the mass of a beam of a given failure load,  $P_f$ ? Given  $P_f$ , span l, square cross-section  $t^2$

$$\sigma_{max} = \frac{M y}{I}$$
  

$$\sigma_{max} \propto \frac{P_f l t}{t^4} \propto \sigma_f$$
  

$$t \propto \left(\frac{P_f l}{\sigma_f}\right)^{1/3}$$

 $M = \text{maximum moment in beam} \propto Pl$  $y = \text{maximum distance from neutral axis} \propto t$  $I = \text{moment of inertia} \propto t^4$  $\sigma_f$  = failure stress of beam material

Mass, 
$$m = \rho t^2 l$$
  
 $m \propto \rho \left(\frac{P_f l}{\sigma_f}\right)^{2/3} l$ 

Performing index:  $\sigma_f^{2/3}/\rho$ to be maximized

### Material Selection

- Ashby book-Tables
- Can obtain performance indices for various loading configurations and mechanical requirements
  - If plot data for material properties on log-log scales, performance indices appear as straight lines
  - Shifting lines up and down identifies best material for that performance index
  - Example: modulus-density chart

#### CMNM Fig.7.1

 $E/\rho$ : axially loaded tie of given stiffness

 $E^{1/2}/\rho$ : beam of given stiffness

 $E^{1/3}/\rho$ : plate of given stiffness

## Property charts for foams:

#### Property charts for foams

 $\epsilon_D$  vs  $\sigma^*_{25\%}$ : contours show energy absorption/volume, U

$$U \sim \sigma_{25\%}^* \epsilon_D$$
  

$$\epsilon_D = U/\sigma_{25\%}^*$$
  

$$\sigma_{257}$$
  

$$\sigma_{257}$$
  

$$\epsilon_D = C/\sigma_{25\%}^*$$

Contours have slope of -1 on log-log scales Balsa, metal foams - high values of U

- Can also produce selection charts for other properties e.g. thermal
- $\lambda$  vs  $\sigma_{5\%}^*$  thermal conductivity,  $\lambda$  thermal insulation applications usually have constraint on strength, too
- $\lambda$  vs  $T_{\rm max}$  may have constraint on maximum service temperature, too
- Density plot closed cell foams buoyancy
- Cell size open cell foams filtration and catalysts — surface are/volume increases as cell size decreases
  - e.g. ceramic foams used in filtration of liquid metals

Table removed due to copyright restrictions. See Table B1: Ashby, M. F. *Materials Selection in Mechanical Design*. 2nd ed. Butterworth Heinemann, 1999.

Ashby MF (1999) Materials Selection in Mechanical Design. Second Edition Butterworth Heinemann

#### Material indices 409

Table B2 Strength-limited	design	at	minimum	mass	(cost,	energy,	environ-
mental impact*)							

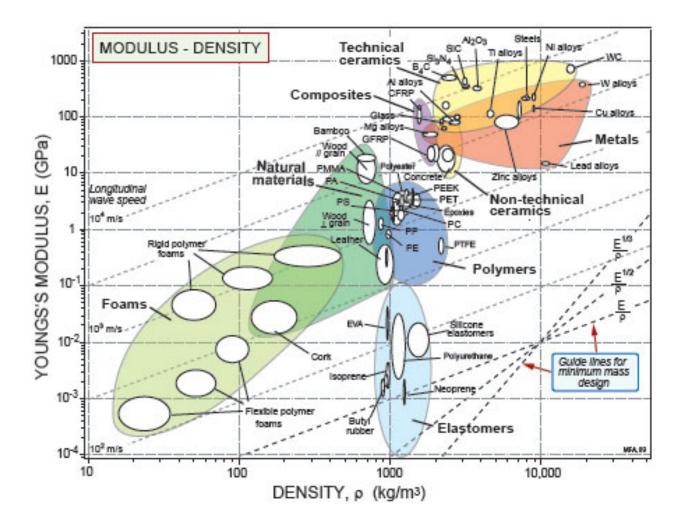
Function and $constraints^{*\frac{1}{r}}$	Maximize
Tie (tensile strut) stiffness, length specified; section area free	$\sigma_f/ ho$
Shaft (loaded in torsion) load, length, shape specified, section area free load, length, outer radius specified; wall thickness free load, length, wall-thickness specified; outer radius free	$\sigma_f^{2/3}/ ho \ \sigma_f/ ho \ \sigma_f^{1/2}/ ho$
Beam (loaded in bending) load, length, shape specified; section area free load length, height specified; width free load, length, width specified; height free	$\sigma_f^{2/3}/ ho \ \sigma_f/ ho \ \sigma_f^{1/2}/ ho$
Column (compression strut) load, length, shape specified; section area free	$\sigma_f/\rho$
Panel (flat plate, loaded in bending) stiffness, length, width specified, thickness free	$\sigma_f^{1/2}/ ho$
Plate (flat plate, compressed in-plane, buckling failure) collapse load, length and width specified, thickness free	$\sigma_f^{1/2}/ ho$
Cylinder with internal pressure elastic distortion, pressure and radius specified; wall thickness free	$\sigma_f/\rho$
Spherical shell with internal pressure elastic distortion, pressure and radius specified, wall thickness free	$\sigma_f/ ho$
Flywheels, rotating discs maximum energy storage per unit volume; given velocity maximum energy storage per unit mass; no failure	$\sigma_f^{\rho}/\rho$

\*To minimize cost, use the above criteria for minimum weight, replacing density  $\rho$  by  $C_m\rho$ , where  $C_m$  is the material cost per kg. To minimize energy content, use the above criteria for minimum weight replacing density  $\rho$  by  $q\rho$  where q is the energy content per kg. To minimize environmental impact, replace density  $\rho$  by  $I_e\rho$  instead, where  $I_e$  is the eco-indicator value for the material (references [1] and [4]).

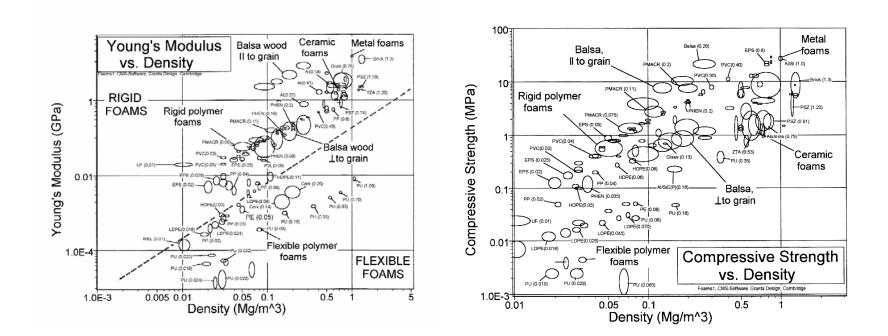
 $\sigma_f = \text{failure strength}$  (the yield strength for metals and ductile polymers, the tensile strength for ceramics, glasses and brittle polymers loaded in tension; the flexural strength or modulus of rupture for materials loaded in bending);  $\rho = \text{density}$ .

<sup>‡</sup>For design for infinite fatigue life, replace  $\sigma_f$  by the endurance limit  $\sigma_e$ .

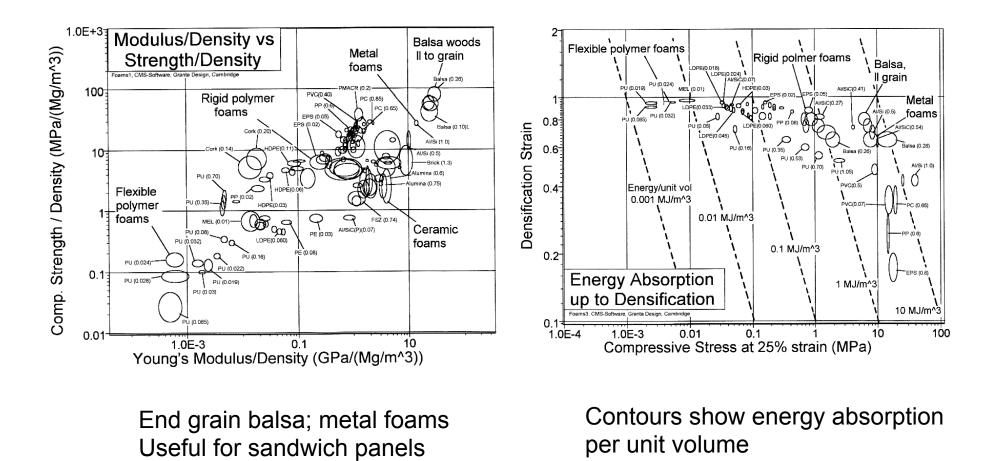
## Ashby MF (1999) Materials Selection in Mechanical Design. Second Edition Butterworth Heinemann



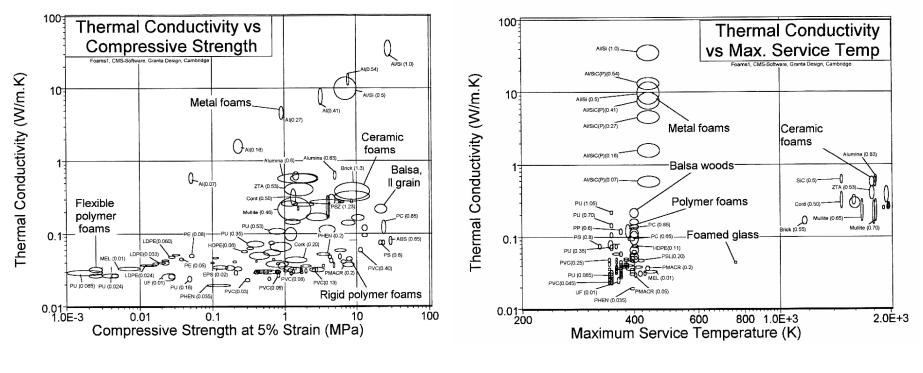
Ashby plot of Young's Modulus - Density © Granta Design. All rights reserved. This content is excluded from our Creative Commons license. For more information, see <a href="http://ocw.mit.edu/help/faq-fair-use/">http://ocw.mit.edu/help/faq-fair-use/</a>.



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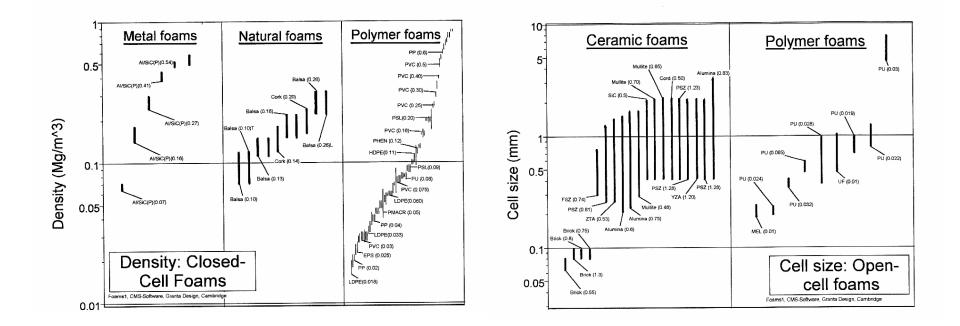
Gibson, L. J., and M. F. Ashby. *Cellular Solids: Structure and Properties*. 2nd ed. Cambridge University Press, © 1997. Figures courtesy of Lorna Gibson and Cambridge University Press.



## Thermal insulation applications; Usually a constraint on strength, too

May also have a constraint on maximum service temperature

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## Buoyancy

## Filtration and catalysis

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3.054 / 3.36 Cellular Solids: Structure, Properties and Applications Spring 2015

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