Derivative of $e^{x \tan^{-1} x}$

Finally, in the first lecture I promised you that you'd learn to differentiate *anything*— even something as complicated as

$$\frac{d}{dx}e^{x\tan^{-1}x}$$

So let's do it!

$$\frac{d}{dx}e^{uv} = e^{uv}\frac{d}{dx}(uv) = e^{uv}(u'v + uv')$$

Substituting,
$$\frac{d}{dx}e^{x\tan^{-1}x} = e^{x\tan^{-1}x}\left(\tan^{-1}x + x\left(\frac{1}{1+x^2}\right)\right)$$

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