Weighted Average

The centroid or center of mass of a planar region is the point at which that region balances perfectly, like a plate on the end of a stick. The coordinates of the centroid are given by weighted averages.

The x coordinate of the centroid is $\bar{x} = \frac{\int x \, dA}{\int dA}$, where dA is an infinitessimal portion of area; the weighting function in this average is just x.

Similarly, the y coordinate of the centroid is $\bar{y} = \frac{\int y \, dA}{\int dA}$. Find the centroid (\bar{x}, \bar{y}) of the parabolic region bounded by x = -1, x = 3, $y = (x - 1)^2$ and y = 4.

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