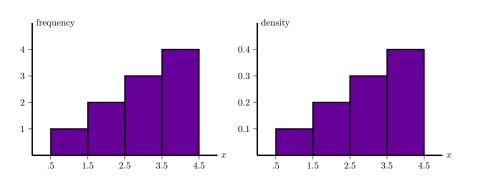
# Studio 3 18.05 Spring 2014 Jeremy Orloff and Jonathan Bloom



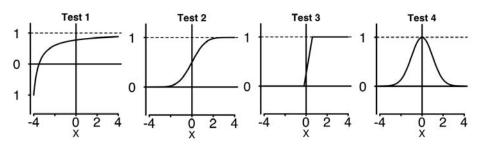
## Concept questions

Suppose X is a continuous random variable.

- a) What is  $P(a \le X \le a)$ ?
- b) What is P(X = 0)?
- c) Does P(X = 2) = 0 mean X never equals 2?

# Concept question

Which of the following are graphs of valid cumulative distribution functions?



Add the numbers of the valid cdf's and click that number.

# **Exponential Random Variables**

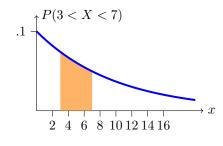
Parameter:  $\lambda$  (called the rate parameter).

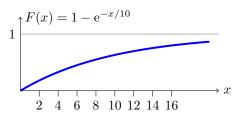
Range:  $[0, \infty)$ .

Notation: exponential( $\lambda$ ) or exp( $\lambda$ ).

Density:  $f(x) = \lambda e^{-\lambda x}$  for  $0 \le x$ .

Models: Waiting time





Continuous analogue of geometric distribution -memoryless!

## Uniform and Normal Random Variables

**Uniform:** U(a, b) or uniform(a, b)

Range: 
$$[a, b]$$
  
PDF:  $f(x) = \frac{1}{b-a}$ 

**Normal:**  $N(\mu, \sigma^2)$ 

Range: 
$$(-\infty, \infty]$$
  
PDF:  $f(x) = \frac{1}{\sigma \sqrt{2\pi}} e^{-(x-\mu)^2/2\sigma^2}$ 

http://web.mit.edu/jorloff/www/18.05/applets/ probDistrib.html

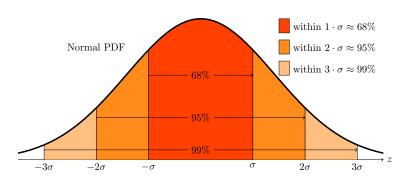
## Table questions

### Open the applet

```
http://web.mit.edu/jorloff/www/18.05/applets/probDistrib.html
```

- 1. For the **standard normal** distribution N(0,1) how much probability is within 1 of the mean? Within 2? Within 3?
- 2. For  $N(0, 3^2)$  how much probability is within  $\sigma$  of the mean? Within  $2\sigma$ ? Within  $3\sigma$ .
- 3. Does changing  $\mu$  change your answer to problem 2?

# Normal probabilities



#### Rules of thumb:

$$P(-1 \le Z \le 1) \approx .68$$
,

$$P(-2 \le Z \le 2) \approx .95$$
,

$$P(-3 \le Z \le 3) \approx .997$$

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# Download R script

Download studio3.zip and unzip it into your 18.05 working directory.

Open studio3.r in RStudio.

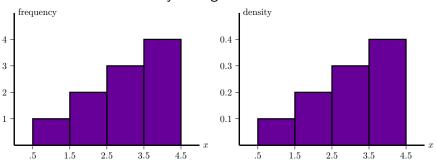
# Histograms

Will discuss in more detail in class 6.

Made by 'binning' data.

**Frequency**: height of bar over bin = # of data points in bin.

**Density**: area of bar over bin is proportional to # of data points in bin. Total area of a density histogram is 1.



# Histograms of averages of exp(1)

- 1. Generate a frequency histogram of 1000 samples from an exp(1) random variable.
- 2. Generate a density histogram for the average of 2 independent  $\exp(1)$  random variable.
- 3. Using rexp(), matrix() and colMeans() generate a density histogram for the average of 50 independent exp(1) random variables. Make 10000 sample averages and use a binwidth of .1 for this. Look at the spread of the histogram.
- 4. Superimpose a graph of the pdf of N(1,1/50) on your plot in problem 3. (Remember the second parameter in N is  $\sigma^2$ .)

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#### 18.05 Introduction to Probability and Statistics

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