

Turbulent Flow and Transport

1 Review of Fundamental Laws and Constitutive Equations

- 1.1 Fundamental laws governing continuum flow, expressed in terms of (i) material volumes (closed systems) and (ii) control volumes.
- 1.2 Mass conservation equation; integral and differential forms.
- 1.3 The equation of motion in terms of the stress tensor. Integral and differential forms. Stress tensor for a Newtonian fluid. The Navier–Stokes equation.
- 1.4 The energy equation (First Law) in integral and differential forms. The equations for the kinetic, potential, and internal energies. Physical significance of the various terms. The viscous dissipation function.
- 1.5 The Second Law of thermodynamics.
- 1.6 The equation for entropy production (Gibbs' equation). The Second Law as a statement that the viscous dissipation function is greater than or equal to zero.
- 1.7 The thermodynamic equations of state: differential expressions for all the thermodynamic properties of a fluid in terms of three measurable properties which are functions of pressure and temperature—the coefficient of thermal expansion, the isothermal compressibility, and the specific heat at constant pressure.
- 1.8 The differential equation for temperature and heat flux. Example: thermal effects due to viscous heating in Couette flow.
- 1.9 Some low–speed approximations: (i) "incompressible flow," (ii) the neglect of the isentropic compression term in the temperature equation. Criteria for validity.
- 1.10 The conservation equation for a molecular species. Mass transfer.
- 1.11 Introduction to the molecular basis of viscosity, heat conduction and diffusion in terms of a simplified kinetic theory of gases. (This serves as an important but relatively simple analogy for the random–walk transport that also occurs in turbulence.)

References:

Sec. 1.1–1.4: Sonin. *Fundamental Laws of Motion: Particles, Material Volumes,*

And Control Volumes. Sonin. *The Equation of Motion for Viscous Fluids.* available at <http://web.mit.edu/2.25/www/> ; White. *Viscous Fluid Flow*, 2nd ed. (1991): 59–89, 96–100; Pope. Ch. 2; or other books.

Secs 1.4 – 1.6: Class notes plus summaries handed out by Sonin.

For Sec. 1.7–1.8: Handout: Sonin. "The Thermodynamic Constitutive Equations and the Equation for Temperature."

Sec. 1.10: Class notes.

Sec. 1.11: See for example Bird, Curtis, and Hirschfelder. *Molecular Theory of Gases and Liquid*, (1954): 8–16, or Vincenti & Kruger. *Introduction to Physical Gas Dynamics*. 1965:15–20.