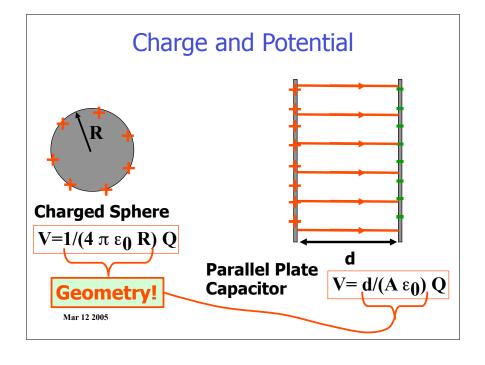
News

- Quiz #2: Monday, 3/14, 10AM
- Same procedure as for quiz 1
 - Review in class Fri, 3/11
 - Evening review, Fri, 3/11, 6-8PM
 - 2 practice quizzes (+ practice problems)
 - Formula sheet

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Charge Density Demo: Application: Lightning rod - Biggest E near pointy tip! $\Rightarrow E \propto \frac{1}{r} \propto \sigma$ Local radius of curvature

Charge and Potential

- For given geometry, Potential and Charge are proportional
- Define

- Measured in [F] = [C/V] : Farad
- C tells us, how easy it is to store charge on it (V = Q/C)

Capacitance $Q \downarrow \text{slope} = C$ $Q_2 \downarrow C \text{ big}$ $Q_1 \downarrow V_0 \quad V$ C bigger -> Can store more Charge! Mar 12 2005

Capacitor

- Def: Two conductors separated by insulator
- Charging capacitor:
 - take charge from one of the conductors and put on the other
 - separate + and charges

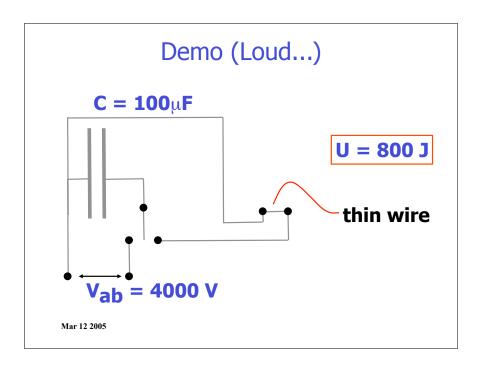
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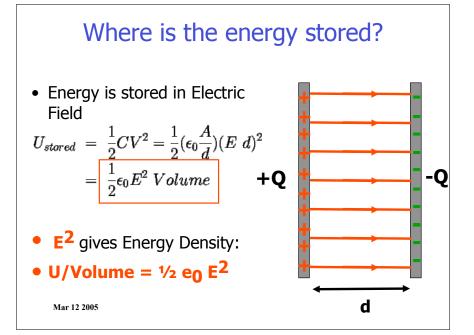
Parallel Plate Capacitor $C = \frac{Q}{V(a) - V(b)} = \frac{Q}{E \ d}$ $= \frac{Q}{\frac{Q}{\epsilon_0} \ d} = \frac{Q}{\frac{Q}{A\epsilon_0} \ d} =$ $= \epsilon_0 \frac{A}{d}$ • To store lots of charge - make A big - make d small

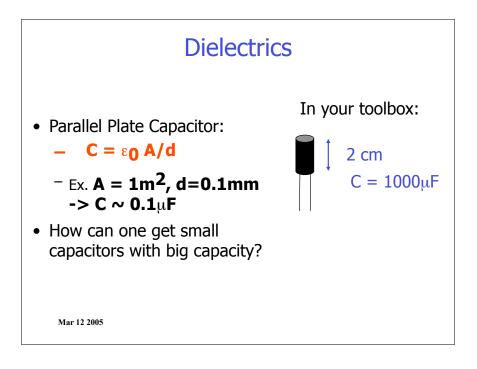
Energy stored in Capacitor

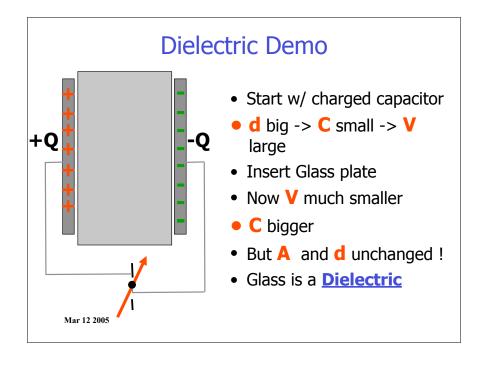
$$egin{array}{ll} W_{tot} &=& \int_{Q_{initial}}^{Q_{final}} V \; dq = \int_{0}^{Q} V \; dq \ &=& \int_{0}^{Q} q/C \; dq = rac{1}{C} \int_{0}^{Q} q \; dq \ &=& rac{1}{C} rac{Q^{2}}{2} \end{array}$$

- Work $W = 1/2 Q^2/C = 1/2 C V^2$ needed to charge capacitor
- Energy conserved
- But power can be amplified
 - Charge slowly
 - Discharge very quickly









Microscopic view

Polarization
$$\vec{P} = \text{const.} \vec{E} = \epsilon_0 \chi \vec{E}$$

Dielectric Constant

- Dielectric reduces field **E**₀ (**K** > **1**)
 - $E = 1/K E_0$
- Dielectric increases Capacitance
 - $C = Q/V = Q/(E d) = K Q/(E_0 d)$
- This is how to make small capacitors with large C!

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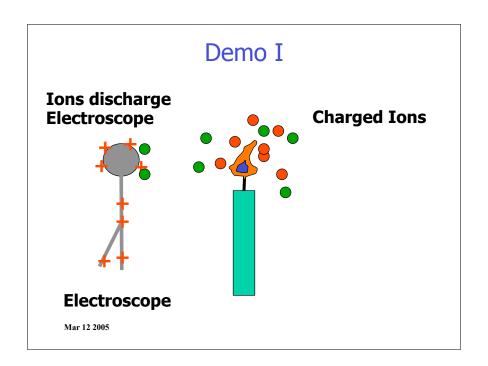
Electric Current

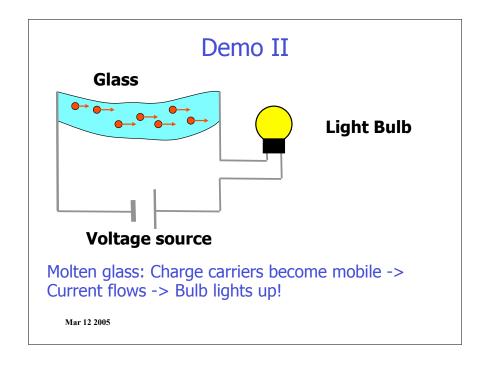
- We left Electrostatics
 - Now: Charges can move in steady state
- Electric Current I:
 - I = dQ/dt
 - Net amount of charge moving through conductor per unit time
- Units:
 - -[I] = C/s = A (Ampere)

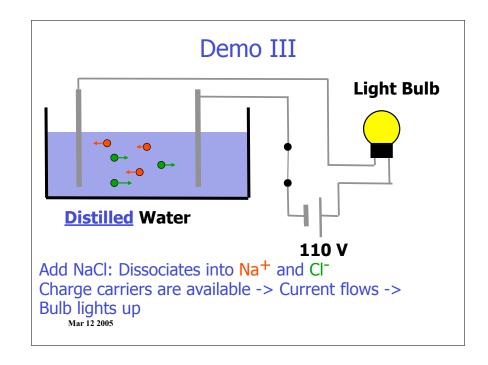
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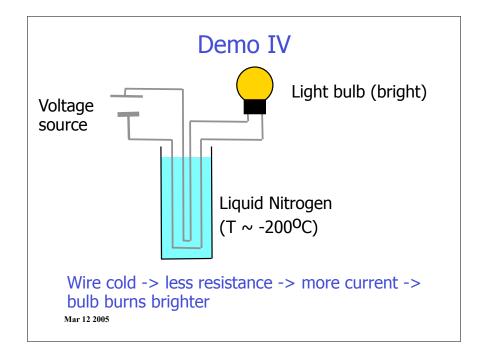
Electric Current

- Current **I** = **dQ/dt** has a direction
 - Convention: Direction of flow of positive charges
 - In our circuits, I carried by electrons
- To get a current:
 - Need mobile charges
 - Need | E | > 0 (Potential difference)









Resistivity

- Interplay of scattering and acceleration gives an average velocity vp
- v_D is called 'Drift velocity'
- How fast do the electrons move?
 - Thermal speed is big: $v_{th} \sim 10^6$ m/s
 - Drift velocity is small: $v_D \sim 10^{-3}$ m/s
- All electrons in conductor start to move, as soon as E> 0

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Ohm's law

$$V = R I$$

- Conductor is 'Ohmic', if R does not depend on V,I
- For real conductors, that is only approximately true (e.g. R = R(T) and T = T(I))
- Approximation
- valid for resistors in circuits
- not valid for e.g. light bulbs

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Resistance

- Define R = V/I : Resistance
- $R = \rho L /A$ for constant cross section A
- R is measured in Ohm $[\Omega] = [V/A]$
- Resistivity ρ is property of <u>material</u> (e.g. glass)
- Resistance R is property of <u>specific conductor</u>, depending on material (ρ) and geometry

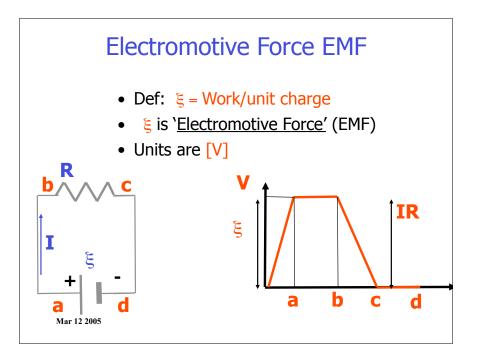
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Electric Power

Use moving charges to deliver power

```
Power = Energy/time = dWdt
= (dq V)/dt = dq/dt V = \underline{I V} = I^2R = V^2/R
```

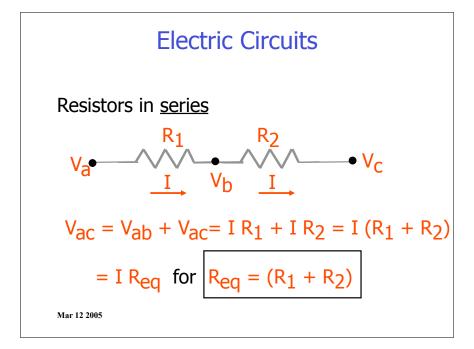
Resistor Capacitor Capacitor Source of EMF



Internal resistance

- Sources of EMF have internal resistance r
- Can't supply infinite power

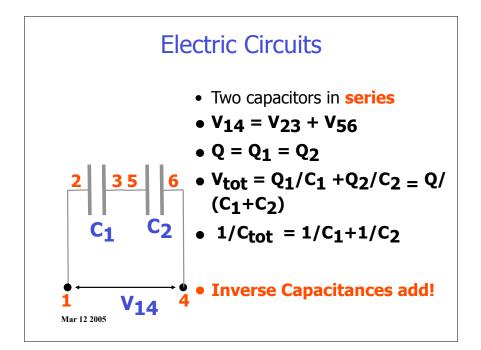
Battery $V_{ab} = \xi - I r$ $V_{ab} = \xi - I r$

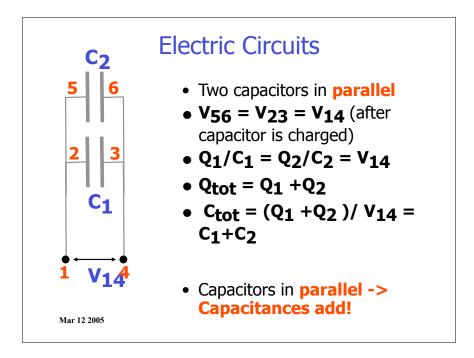


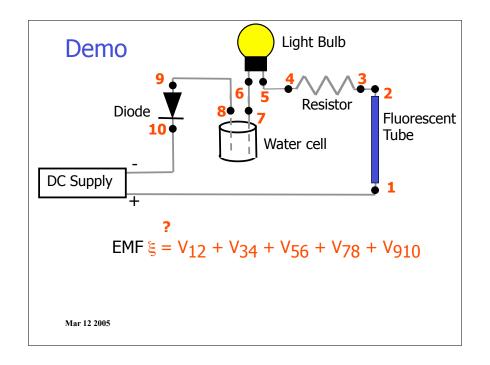
Electric Circuits

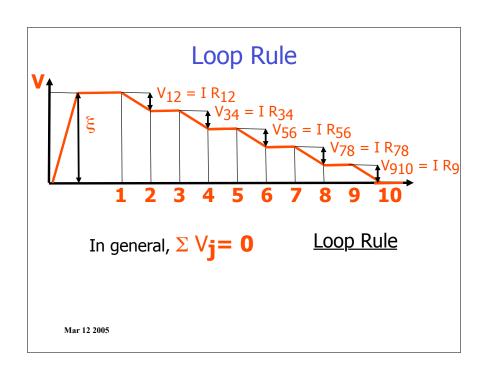
Resistors in parallel

$$V_a$$
 V_b
 I
 R_2
 $I = I_1 + I_2 = V_{ab}/R_1 + V_{ab}/R_2 = V_{ab}/R_{eq}$
 V_b
 $I = I_1 + I_2 = V_{ab}/R_1 + V_{ab}/R_2 = V_{ab}/R_{eq}$
 V_b
 $I = I_1 + I_2 = V_{ab}/R_1 + V_{ab}/R_2 = V_{ab}/R_{eq}$









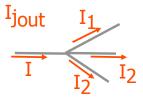
Kirchoff's rules

• Junction rule

Loop rule

At junctions:

$$\Sigma I_{iin} = \Sigma$$



△ V for both EMFs and Voltage-drops

Around closed loops: $\sum \Delta V_{\dot{1}} = 0$

Charge conservation

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ige conservation

Energy conservation

Kirchoff's rules

- Kirchoff's rules allow us to calculate currents for complicated DC circuits
- Main difficulty: Signs!
- Rule for resistors:



 $\Delta V = V_b - V_a = -IR$, if we go in the direction of I (voltage drop!)

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Kirchoff's rules

- Kirchoff's rules allow us to calculate currents for complicated DC circuits
- Main difficulty: Signs!
- Rule for EMFs:

$$V_a \stackrel{-}{\longrightarrow} V_b$$

 $\Delta V = V_D - V_a = \xi$, if we go in the direction of I

